

Testing the Effectiveness of Educational Tools and Games With and Against the ASSISTments System

An Interactive Qualifying Project Report

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Abstract

This report, prepared for the creators of ASSISTments, addresses the concept of improved learning from educational computer games and describes the methods used to incorporate these games into the ASSISTments learning system. These methods include searching for and selecting the most relevant existing educational computer games, constructing new problem templates for use within the ASSISTments system, and creating custom learning experiences with and without educational games for experimentation.

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We would also like to thank Eric Corriveau, who selflessly dedicated his free time to develop a program to organize experiment data for facilitated analysis.

Authorship

Ian Lonergan was responsible for the creation of the experiment structure within the ASSISTments system as well as the programming of variablized templates. Additionally he contributed to the search for valuable educational games and the teaching strategies for the experiments.

Shane Daley was responsible for building the experiments within the established structure. Additionally he was responsible for finding and testing high-quality educational games and tools and co-designing the teaching strategies and experience of the experiments. He will be responsible for testing and recording the results of the experiments later this year.

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Introduction



Fig 1.1: The ASSISTments logo

The ASSISTment System was founded in 2003 for the purpose of educating students in a variety of subjects while providing concise and important feedback to instructors. The software is intended to be intuitive and easy for teachers to use while still providing considerable educational and analytical power. The ASSISTment System has continued to grow since its conception and is easily capable of facilitating and hosting learning experiments. For our Interdisciplinary Qualifying Project we aim to test the effectiveness of the ASSISTment System versus educational games, specifically games related to Algebra, from outside sources as well as the effectiveness of augmenting the ASSISTment system with learning tools and games.

1.1 Purpose

The primary purpose of this project was to examine the difference in short-term and deep-learning between educational third-party math games and ASSISTment tutored problem sets. Additionally, the project is intended to highlight the differences between traditional learning and traditional learning augmented with educational math tool software. The project was approached in three phases— finding existing educational math games, content construction and experimental study.

The purpose of the searching phase was to find educational games that taught math at a high-school level. The games found would need to fit well with ASSISTments and be able to theoretically teach in a brief period of time.

During the content construction phase the intent was to create experiments that tested two approaches to teaching. Since the ASSISTment System offers in-depth teacher feedback, the effectiveness of either teaching process can be measured numerically and allow an objective analysis.

The experimental study will be conducted later this year on high school students. Their performance will be analyzed so the benefits of the two approaches can be compared.

1.2 Hypothesis

It is expected that the students who complete the experiments with games or software will experience greater short and long-term learning than the students exposed to the control. Students who play games are asked to play them for at least five minutes before submitting their high score to ASSISTments, whereas students in the control group are asked to practice doing relevant problems for at least five minutes. The results can be interpreted accurately because ASSISTments allows the instructor to view how long a student spent on one “problem” (in this case a game or series of problems). It is expected that students will be more interested in their work when playing games and using educational software because it is an unusual teaching approach. Additionally, knowing that their high score is recorded may provide extra incentive to become proficient at the subject material.

The inverse is also possible. The games may prove to be confusing or overwhelming to students that are not yet proficient with the material. The online learning tool may be harder to use or understand than expected, even with guidance. Furthermore, the visual nature of the games and software may prove useful only to students who are visual learners, and be a

hindrance to those that are not. The rote nature of practicing problems could prove to be efficient, even if it is more “boring”.

1.3 Methodology

The first step in building our experiment was to populate a database of existing games and tools. We created and used an exhaustive method for searching for new games and game sites. We took advantage of some advanced qualifiers on google. To find game sites, with appropriate games, we used the following:

Methodology A

1. Go to Common Core Standards for Algebra
2. Select a standard from the list
3. Search for games through google using important terms from the common core standard list (e.g. <http://www.corestandards.org/Math/Content/HSA/APR/A/1> might search for “polynomial arithmetic game”)
4. Possible to narrow down selection to sites in .org and .edu domains by appending “site:.org” or “site:.edu” to query
5. Search the site itself using Methodology B

Methodology B

1. Search for games containing the word algebra (e.g. to search <http://www.example.org> for algebra games, search “algebra site:www.example.org” or “algebra games site:www.example.org”)
2. If this doesn’t turn up results, attempt searching without the term algebra, but rather with important terms selected from the common core standard list

By following these methodologies we were able to get a list of over thirty games

Each of the four experiments has been developed with the same basic structure—the students begin by answering three questions (a pre-test) relevant to the subject material (and in some cases specifically tailored to address multiple facets of the same concept) before moving on to one of two possible steps. These steps are variablized through code in the ASSISTment system and a student has a fifty percent chance of encountering either step after they have completed the pre-test. The possible steps vary from experiment to experiment:

Students are asked to complete problems provided by ASSISTments for at least five minutes and enter how many they completed
Students are asked to play a “good” game for at least five minutes before entering the highest score they achieved
Students are asked to play a “bad” game for at least five minutes before entering the highest score they achieved
Students work through a series of problems intended to help understand the subject material with explanations and an embedded educational online math tool
Students work through a series of problems with less prior knowledge building and no tool

Table 1.1

The experiments can be explained like this:

Experiment 1: Plain ASSISTments versus a “good” game	Students are given a pre-test followed by either a series of similar questions or a relevant, high-quality game, followed by a post test
Experiment 2: Plain ASSISTments versus a “bad” game	Students are given a pre-test followed by either a series of similar questions or a relevant, low-quality game, followed by a post test
Experiment 3: A “good” game versus a “bad” game	Students are given a pre-test, followed by either a high-quality game or a low-quality game, followed by a

	post-test
Experiment 4: Scaffolded problems augmented with online tool versus scaffolded problems without tool	Student are given a pre-test, then a scaffolded series of problems designed to build a more complete understanding of the subject material (augmented with educational software tool) or a series of scaffolded problems designed to replicate a text-book's teaching methods (without tool), followed by a post-test.

Table 1.2

After the students work through one of the possible steps they are brought to another three relevant problems, or the “post-test.” The results of the post-test will be compared with the results of the pre-test to examine if any short-term learning occurred. The pre-test is important because it gives the us an idea of the student’s proficiency previous to the experiment. If a student spends little time on the pre-test and answers all of the questions correctly their results will not be demonstrative, unless the student performed notably worse on the post-test. The analysis will be focused on the students who did not perform well on the pre-test. This makes it easy to see if one method results in no notable learning and another method does.

Of course, it would not be scientific or accurate to compare students only on their results on the pre and post-tests. Fortunately, ASSISTments allows instructors and testers to look at students’ completion times problem-to-problem. Additionally, we can see how many problems students completed and how well they did on those problems and what high score they achieved in the games they played. If a student spends a long time on every problem but answers incorrectly consistently it is clear that the student has a very limited understanding of the material and that likely neither teaching method would be enough to cause notable learning as measured by the post-test. On the other hand, if a student demonstrates incomplete understanding but shows improvement over the course of the experiment and answers more of the post-test questions correctly we can deduce that that student experienced short-term learning.

2 Background

2.1 ASSISTments

2.1.1 What is ASSISTments?

ASSISTments is a non-profit research project that blends tutoring “assistance” with “assessment” reporting to teachers.¹ ASSISTments allows teachers and researchers to generate and assign problem sets, along with creating content for those problem sets. ASSISTments gives feedback to the students as they answer questions, but also lets instructors and researchers know how students performed.

2.1.2 Assistments

An assistment is a problem (possibly with multiple parts), with all associated answers and feedbacks. Incorrect answers can have feedback messages included, to deal with hints on common errors. Assistments can accept answers in several forms, including simple entry forms (answer must be entered exactly), algebra (answer will be evaluated and compared to correct answer), multiple choice, open response essay,

Assistments also have hints, a form of tutoring, which can have one or more messages to help a student answer a question. The final hint is known as the Bottom Out Hint, and generally gives the answer to the question. An assistment set to test mode will disable all tutoring and feedback. This is useful for testing students in a standard fashion to determine current knowledge.

¹ <http://teacherwiki.assistment.org/wiki/About>

Assistments can have multiple main problems, each with their own sets of hints.

There is a special type of assistment, known as a variablized template, which allows content creators to generate randomized numbers for usage in the problem. This allows for the generation of many problems of a single type by randomizing the exact numbers that are used.

2.1.3 Problem Sets

Problem sets are groups of assistments and/or sub sections, which are similar to problem sets but can only exist in other sets. Linear order problem sets are completed by performing each assistment in order. When using a random order set, every assistment within must still be completed, but the order at which they are given is randomized for each student. A choose condition problem set randomly picks one child to run, and only that child assistment or sub section gets run.

It must be noted that assistments and sub sections of different types can be mixed within a problem set. So, it is possible to have a choose condition problem set with several linear sub sections (in which case a single linear sub section would be run, randomly chosen).

2.2 Games

2.2.1 What is a game?

What constitutes a game has undoubtedly been a subject of discussion since soon after their conception. However, Ludwig Wittgenstein (1889-1951) was possibly the first notable and

academic philosopher to offer considerable wisdom on the subject. Wittgenstein challenged his readers in his book, *Philosophical Investigations*, to define game and presented the “problems” of competition and amusement that would occur when trying to do so. For example, a competitive chess, go, or *Starcraft* player feels a completely different sort of amusement, if she does indeed feel amusement, when playing her game of choice than a young boy feels when playing *Chutes and Ladders*. Furthermore, if two friends cooperate to defeat the artificial intelligence in a computer game the idea of competition is not present. It is by this reasoning that any all-encompassing definition of the word “game” could not include either competition or amusement. Wittgenstein’s implied conclusion (based on his philosophy of language as a whole) is that games do not need to be defined because people inherently understand the meaning of the word, strict and technical definition or not. However, it is entirely possible to arrive at an inclusive definition if only for the sake of precision.

To interact with a game in the traditional sense, one has to play it. The idea of play is the basest way to understand a game. Mark Twain aptly described play as intentional action separate from “work.” This means that reading a book or taking a walk qualify as play, because they are not strictly work, typically. Of course, these things alone could never reasonably be described as games on their own. This leads to the concept of interactivity, something crucial in any game. If one is engaging in play by interacting with something—a ball, for example—that thing can be classified as a *plaything* or toy. A toy always has rules and restrictions, whether they are imposed by the laws of physics in the case of the ball, or are part of the code in the case of a computer game. However, playing with a ball does not constitute a game in and of itself. What every game shares that has not been included thus far is one or multiple goals. While bouncing a ball is not a game, passing it back and forth, a.k.a. playing catch, is because there is an implied goal (throw the ball from player to player without dropping it). Some games, like chess,

have an overt goal (put the other player into checkmate). With these three components in mind, a game becomes a non-work related action with rules, restrictions and an objective, or more simply, playing with a toy with rules.

In our search for valuable educational games we came across many things that would be considered toys. This in itself is not necessarily a bad thing—but for the purposes of our project we typically wanted to expose students to educational software that encouraged them to perform well. This is why every game that we use keeps track of and displays the player's score and why we ask students for the highest score they achieved.

2.2.2 Educational Games

The concept of using software as a means of education has been around since computer games became popular. Computing systems were used in the military to train pilots as early as World War II. The Plato IV system, which was released in 1972, featured primitive bitmap graphics and sound and *Oregon Trail* was developed in 1974 by the Minnesota Educational Computing Consortium (MECC). However, educational games didn't gain popularity in schools and institutions until the 1980s—notable examples include *Oregon Trail*, which enjoyed incredible success and popularity from the mid 80s into the 90s, and The Learning Company's *Reader Rabbit* (1986), which aided in teaching students to read and spell.



Fig 2.1: *Oregon Trail* tasks students to guide their party of settlers from Missouri to Oregon and features harsh pioneer conditions like dysentery, starvation, and even death.

2.2.2.1 Educational Math Games

With the boom of the popularity of educational games in the 1980s, games designed to teach students math began to see use in schools and institutions.² *Number Munchers*, also developed by MECC, was extremely successful. The game taught students how to recognize specific categories of numbers. The company later developed *Math Munchers* in the mid-90's which went on to sell over two million copies—a record that many high-budget non-educational games fail to reach even today.³

² *Educational Game*, http://en.wikipedia.org/wiki/Educational_game.

³ *Munchers*, http://en.wikipedia.org/wiki/Munchers#Number_Munchers

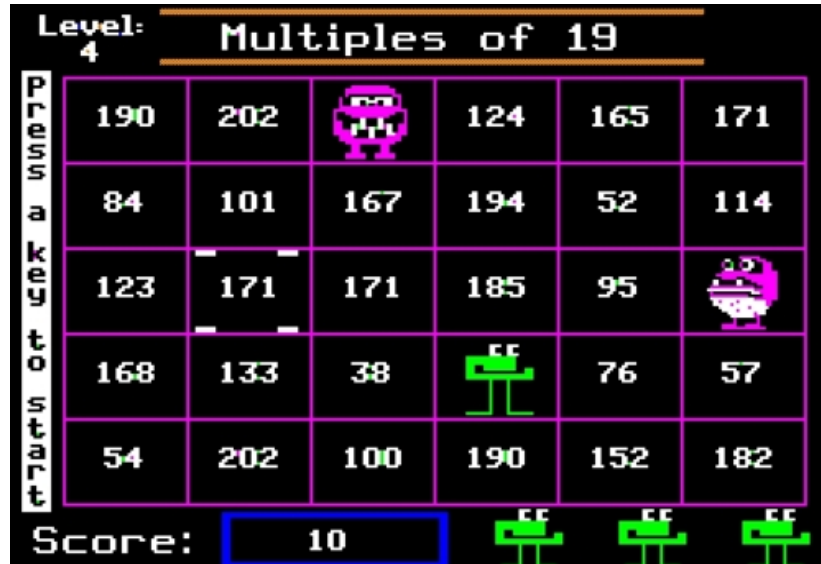


Fig 2.2: Students play as the green character and must “munch” numbers within a category (in this case multiples of 19) if they don’t want to be eaten by the purple monsters in *Number Munchers*.

Treasure Mountain!, which was released in 1990 and was also developed by The Learning Company, was very educational and popular. *Treasure Mathstorm!*, an iteration that was released in 1996, became an iconic game that countless students looked fondly upon more than ten years later. The game featured better graphics than the previous examples did and taught students about counting numbers and money, balancing weights, and telling time. Additionally, the player had goals to strive for, like buying new nets to catch elves, finding secret items, and progressing up the mountain.⁴

⁴ *Treasure Mountain!*, http://en.wikipedia.org/wiki/Treasure_Mountain!



Fig 2.3: *Treasure Mathstorm!* was notably more complicated than previous educational math games. Players can capture elves, must avoid or defeat evil snowballs, and must solve various math problems to earn money and progress through the game.

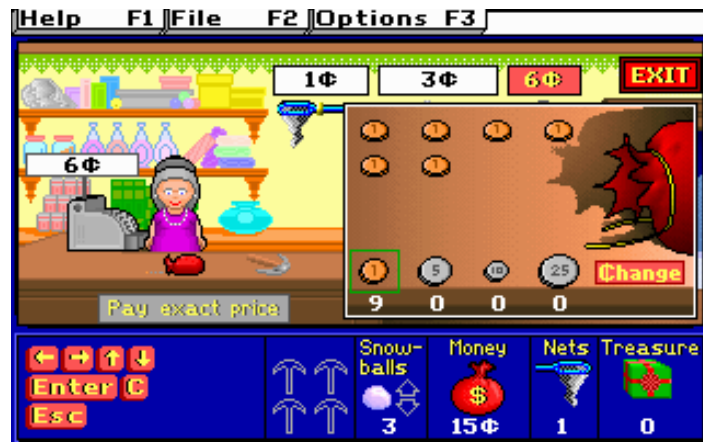


Fig 2.4: The player can spend money in the shop on various items. This gives players a better understanding of how to add and subtract change.

2.2.2.2 Effectiveness of Educational Games

Many have questioned the validity of using computer games and simulations to teach students in a classroom environment. As a result, numerous studies have been conducted on the subject, and the findings have been positive: the cumulative results of a research review that examined 68 studies that directly or indirectly tested the difference between simulations/games and conventional teaching methods are pictured and discussed below:

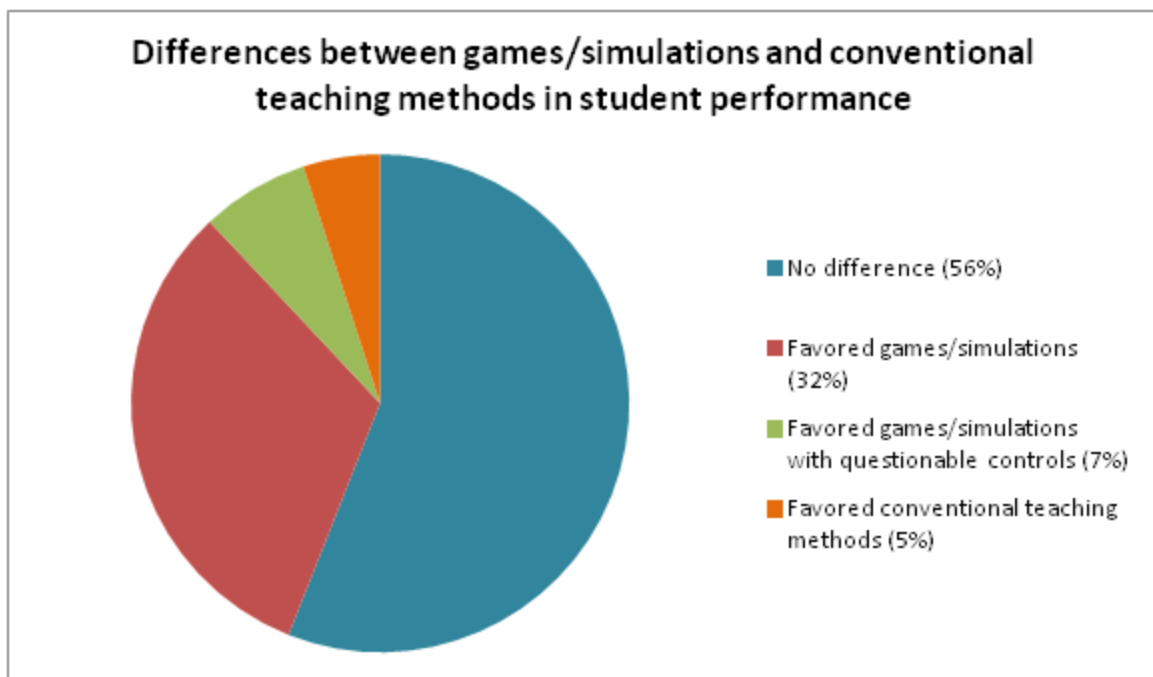


Fig 2.5⁵

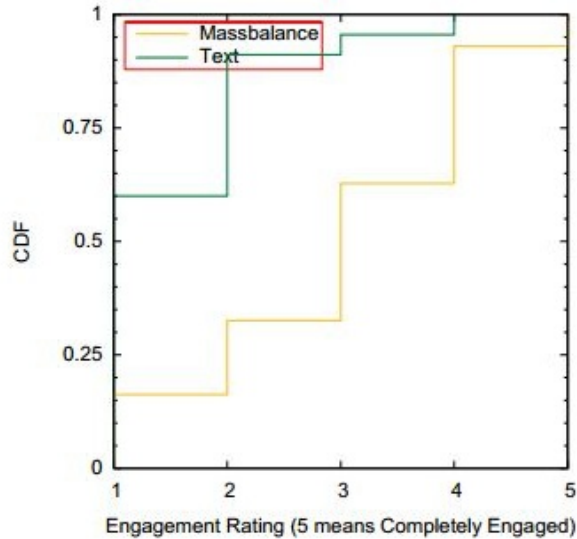
It is important to note that the majority of these studies (46) examined the effectiveness of games in the area of social sciences. According to the research review, 33 of these studies “showed no difference in student performance between games/simulations and conventional

⁵ “The effectiveness of games for educational purposes: a review of the research.”
<http://seayj.people.cofc.edu/cb/findsim.html?referrer=webcluster&>

instruction.” Additionally, the social science games did not generally use a computer, while the other areas (math, physics, and language arts) did.

Despite using a computer, of the 6 studies dedicated to language arts, 5 demonstrated that games were ineffective. However, of the 8 studies involving math, 7 found that games and simulations were more effective at “improving math achievement” than conventional teaching methods were. According to the research review, “Subject matter areas where very specific content can be targeted and objectives precisely defined are more likely to show beneficial effects for gaming.” Furthermore, the research review found that games and simulations demonstrated greater learning retention than conventional teaching methods. Games and simulations also tended to interest students more. 14 of the studies recorded student feedback. In 12 of these studies the students “reported more interest in simulation and game activities than in more conventional activities.”

In an interactive qualifying project also done at Worcester Polytechnic Institute titled, “An Analysis of the Effectiveness of an Interactive, Educational Game”, Michael P. Lundy reported that of the experimental group (asked to learn with an “interactive budget simulation tool” called Massbalance for 10 minutes) and the control group (asked to study a “static source” for 10 minutes), the experimental group spent an additional 2 minutes longer than they were asked to, and the control group spent 1 minute less than they were asked to. Although both groups tended to score similarly on the post-quiz, the experimental group was more entertained and engaged than the control group (graph courtesy of Michael P. Lundy):



(b) “How engaged were you by the source?”

Fig 2.6

Students answered these questions in a post-survey after they attempted to learn the material with the game or the static source. The two questions reveal that the majority of experimentees answered above a “3” for both entertainment and engagement after playing the game, while the majority answered below a “2” for the same question after studying text. It seems that students consistently enjoy and are more engaged by educational games, regardless of their effectiveness. Lundy’s report suggests that engagement is directly tied to how likely students are to continue to pursue related learning on their own. Other reports that studied the effectiveness of educational games and software came to similar conclusions.

2.2.2.3 The Future of Educational Games

Educational games show considerable promise. Video games as a medium have progressed

astronomically in the last ten years, and as higher quality entertainment video games are developed, higher quality educational games become a distinct possibility. Studies continually reveal that educational games and software can and have been effective teaching tools. As a result, the interest in them has been growing.

President Obama has been an advocate of educational computer games from the start, and has tasked his administration to study the benefits of video games. According to Obama, he wants to create “educational software that’s as compelling as the best video game.” Additionally he wants game players “to be stuck on a video game that’s teaching you something other than just blowing stuff up.” While Obama’s goals are lofty, they are possible with enough funding and support.⁶

On that note, there have been at least two notable educational games that have received or are asking for funding on www.kickstarter.com, a site where entrepreneurs ask for a certain amount of money to fund their projects. Mindblown Labs’ *Mindblown Life*, a social mobile game that develops money management skills, recently received \$77,522 dollars in funding from 695 backers-- more than \$17,000 more than they were asking. Even Bill Nye has worked closely with developers to produce a rough build of an educational physics game call *Aero*, which is also in the process of receiving funding.

⁶ “Obama: Games can make education relevant for young people.”
<http://www.gamesindustry.biz/articles/2013-02-19-obama-games-can-make-education-relevant-for-young-people>



Fig 2.7: In *Aero*, players play as a seagull and have to take things like drag, lift, and gravity into account.



Fig 2.8: Players can use an apparatus designed to represent wings to control their seagull.

3 The Experiments

We aimed to find and test the effectiveness of educational math games that taught subject material at a high school level because there are fewer studies and educational games focused on high school material. After compiling a list of over 30 educational games at or around a high school level we decided on 4 games (2 “good” and 2 “bad”) and 1 piece of educational software.

3.1 Experiment #1

Factoring Quadratics: Wrecks Factor vs ASSISTments



Fig 3.1: The main menu of *The Wrecks Factor*

The Wrecks Factor was chosen for this experiment because it was of high quality and seemed

both educational and fun. The *Wrecks Factor* is a game hosted on managahigh.com about factoring quadratics that is played by rescuing ships in trouble. A player rescues a ship and earns points by dragging a box around it that represents the factored quadratic.

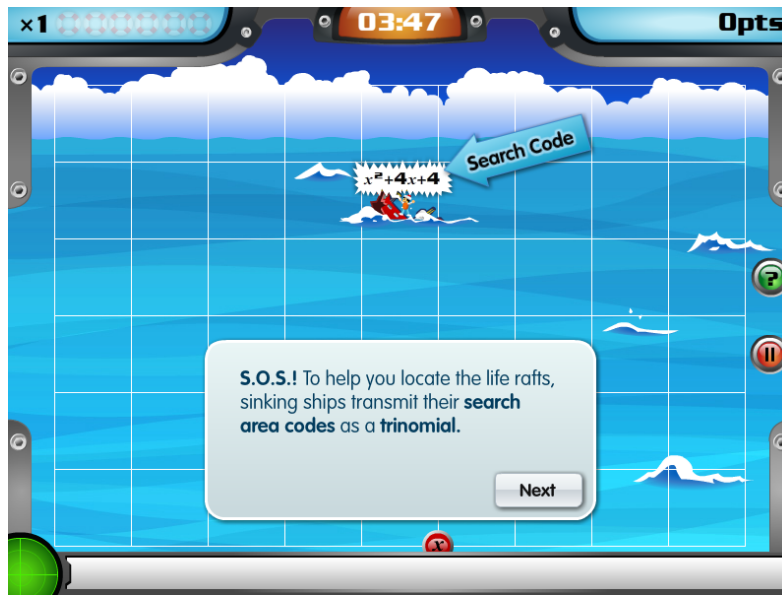


Fig 3.2: *The Wrecks Factor* provided a concise tutorial to help new players

The game screen is a grid where each unit right and up and left and down represent +1 and -1, respectively. For example, a box dragged two units to the right and two units up represents $(x+2)(x+2)$, which would correctly factor this trinomial.



Fig 3.3: Players drag boxes that represent factored quadratics to help ships in need

Ships in need of rescuing appear progressively more quickly and the player is tasked with quickly and efficiently solving numerous quadratics. Points are awarded for doing well at the game and are totaled up after the timer has run out on any given level. Players can choose the amount of assistance they would like, with lower assistance levels awarding more points for completed factorizations.

Students participating in the experiment who were tasked to play *The Wrecks Factor* were asked to spend at least five minutes playing the game and to post their high scores when they were done. Additionally, they were presented the following choices for feedback about the game:

- The game was educational and fun
- The game was boring but educational
- The game was fun but not educational
- The game was not educational or fun
- I had technical difficulties

Approximately half of the students were presented with a link to a series of pre-set problems where they were asked to factor quadratics for at least five minutes. They were asked to record how many problems they had answered in the time that they had spent.

The tables of the results of the first experiment are pictured below. Green represents a correct answer, and red represents an incorrect answer. Students were not asked for feedback on the problem set.

ASSISTments Problem Set									
Student	Pre-Test			Post-Test			Questions Answered/HighScore	Feedback	Time Spent
	1	2	3	4	5	6			
	84255/160222	84262/160229	84278/160245	84249/160216	84191/160158	84285/160252	378226/607096	377506/606224	
1	1	1	1	1	0	1	7		7.2
2	0	0	0	1	1	1	26		11.8
3	1	1	1	1	1	1	84		35.3
4	1	1	1	1	1	1	10		18
5	1	1	1	1	1	1	83		17.8
6	1	1	1	1	1	1	12		6.4
7	1	1	1	1	1	1	10		27.4
8	1	1	1	1	1	1	7		7.5
9	1	1	1	1	1	1	22		10.9
10	1	1	1	1	1	1	30		14.8
11	0	0	0	1	1	1	13		10.7
12	0	0	0	1	1	1	28		23
13	1	1	1	1	1	1	5		6.5
14	1	1	1	1	1	1	47		13.8
15	0	0	0	1	1	1	54		12.4
Wrecks Factor									
16	1	1	1	1	1	1	7500	Educational and fun	3.1
17	1	1	1	1	1	1	101500	Educational and fun	7
18	1	1	1	1	1	1	112000	Educational and fun	8.6
19	1	1	1	1	1	1	338000	Educational and fun	N/A
20	0	0	0	0	0	0	75000	Educational and fun	7.4
21	1	1	1	1	1	1	456500	Educational and fun	16.3
22	0	0	0	0	0	0	1000	Educational and fun	N/A
23	1	1	1	1	1	1	33000	Educational and fun	N/A
24	1	1	1	1	1	1	27000	Educational and fun	7.8
25	0	0	0	0	0	0	400	Educational and fun	4.6
26	1	1	1	1	1	1	285000	Educational and fun	2
27	0	0	0	1	1	1	3000	Boring but educational	N/A
28	0	0	0	0	0	0	4000	Educational and fun	6

Table 3.1: A table of students and their resulting data in each half of the experiment

	Average Difference	Standard Deviation	Average Time Spent	Significance
ASSISTments	0.733333333	1.437590577	14.9	
Wrecks Factor	0.230769231	0.832050294	7	
				p = 0.138967833

Table 3.2: A table that shows the average pre and post-test differences, the standard deviation of the data, the average time students spent on the task assigned to them, and the statistical significance of the data

Students who simply did practice problems seemed to learn more than students who played *The Wrecks Factor*. 4 out of 15 students who used ASSISTments showed improved performance on their post-tests. Only 1 of the 13 students who played *The Wrecks Factor* showed any improvement on their post-test. Interestingly, every student who showed improvement in either side of the experiment went from getting none of the questions on the pre-test correct to

answering every post-test question correctly. Only one student performed more poorly on the post-test, but this is plausibly an anomaly.

Of the 15 students asked to practice factoring quadratics, the least time spent was 6.4 minutes. The most time spent was 35.3 minutes. The average time spent was 14.9 minutes. Students answered questions at different rates, but none answered less than 5, and one student answered 84, which was the total number of questions offered. The average amount of questions answered was 29, far more than expected. 3 of the 4 students who showed improvement answered less slightly than the average, but student 15 notably answered 54 questions. Students who showed improvement spent no less than 11 minutes answering questions, double what was asked of them. One of these students spent 22 minutes answering questions. The average improvement from pre-test to post-test was .73, which means that students did 24% better on average.

Of the students that played *The Wrecks Factor*, and whose times were recorded, the least time spent playing was just over two minutes. The most time spent playing was 16.3 minutes. The average time spent playing was 7 minutes. 6 scored over 75000, which was considered a good score. One student reported scoring 400 points, even though this is not possible. Several students reported scoring between 1000 and 4000 points, even though 1000 points are rewarded just for completing the tutorial. All but one of the students thought that the game was “Educational and fun.” The one student that did not find the game fun still believed it to be educational. This conflicts with pre and post-test results-- while no students performed more poorly on the post-test than they did on the pre-test, only one of the students improved after playing the game, even though there were more opportunities for students to show improvement in this half of the experiment. It should be added that that student reported obtaining a score of

only 3000 which would suggest that they did not play the game enough or at a high enough skill level to have learned very much. It is possible that they received help or consulted a source to augment their learning. The average improvement from pre-test to post-test was .23, which means that students did 7% better on average.

The data above suggests that not only did students tend to learn more from practicing relevant problems, they also were compelled to spend more time doing so. Even though students spent less than half the average time students spent practicing problems playing *The Wrecks Factor*, they still tended to spend two minutes more than was asked of them. It is notable, however, that three of the nine students whose times were record spent less than the time asked playing the game. As can be seen in the second table above, there was a high standard deviation among the results of the students who completed the ASSISTments portion of the experiment, and lower but still notable deviation in the results of the students who played *The Wrecks Factor*. Unfortunately, the statistical significance of the results was .14, somewhat higher than the desired .05. This was due to a relatively small sample size.

3.2 Experiment #2

Translation, Reflection, and Rotation: Transformation Golf vs Transtar



Fig 3.4: Transformation Golf

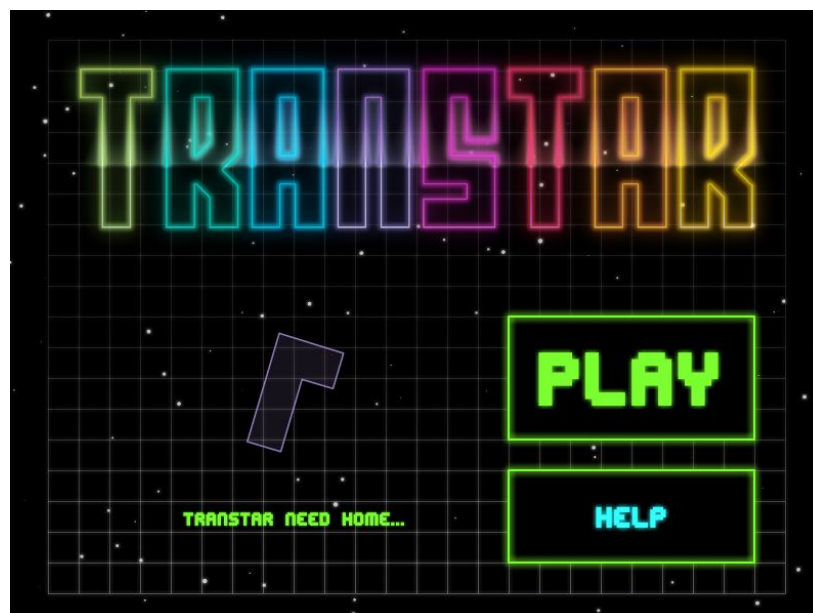


Fig 3.5: Transtar

Transformation Golf, a game hosted on nationalstemcentre.org, and *Transtar*, a game hosted on mangahigh.com, were chosen for this experiment because they were believed to represent a “bad” game and “good” game respectively. *Transformation Golf* demonstrates concepts much in the same way *Transtar* does, but it is not nearly as polished, visually pleasing, or “fun.” Both of these games teach students how to translate, reflect, and rotate within a coordinate system. *Transformation Golf* does so with one point, serving as a golf ball, and *Transtar* does so with a shape that represents a space ship.

Unfortunately, *Transformation Golf* has since become inaccessible, so it will not be pictured below.

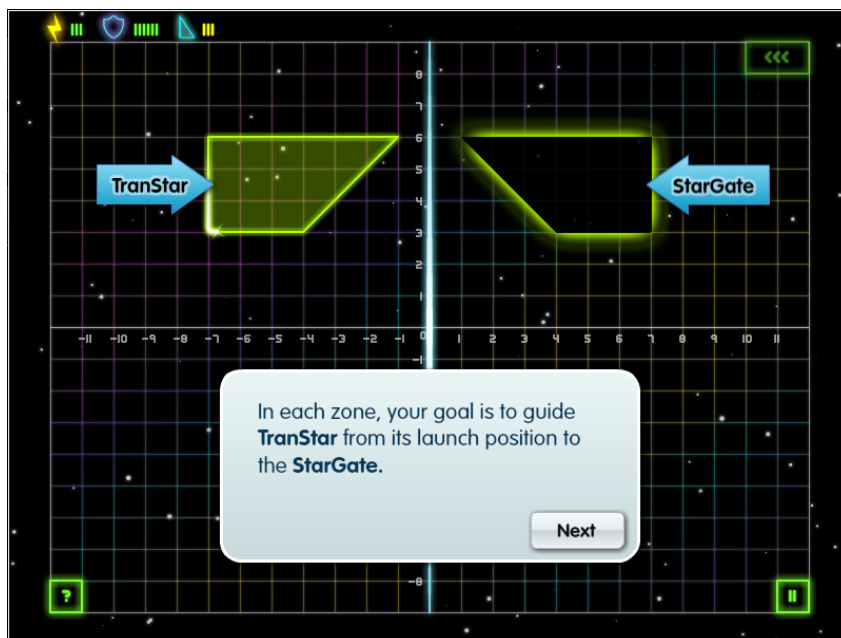


Fig 3.6: Like *The Wrecks Factor*, *Transtar* offers a brief tutorial

Students click dividing lines to reflect specific shapes into “StarGates.” They have a limited number of moves and tries, and are rewarded for efficiently guiding their shape to its goal.

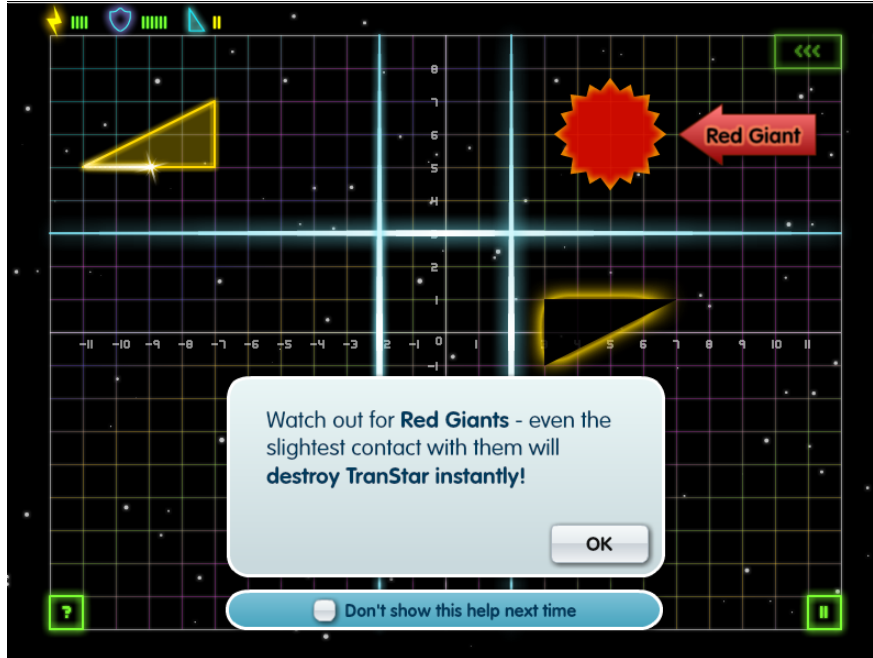


Fig 3.7: *Transtar* sets itself apart from other online educational games by introducing a variety of fun and challenging mechanics

There are a variety of interesting mechanics in *Transtar*. For example, players must watch out for Red Giants while reflecting their ship across the coordinate system. It was unknown if this would benefit or hinder the learning process.

Students participating in the experiment were asked to spend at least five minutes playing *Transformation Golf* or *Transtar* and to post their high scores when they were done. Additionally, they were presented the following choices for feedback about the games:

- The game was educational and fun
- The game was boring but educational
- The game was fun but not educational
- The game was not educational or fun
- I had technical difficulties

The tables of the results of the first experiment are pictured below. Green represents a correct answer, and red represents an incorrect answer.

Transformation Golf										
Student	Pre-Test			Post-Test			High Score	Feedback	Time Spent	
	1	2	3	4	5	6				
	369011/595124	368994/595107	378509/607486	369005/595118	368988/595101	378513/607490	377508/606226	377506/606224		
1	0	0	0	0	0	0	43	Educational and fun	5.4	
2	0	0	0	0	0	0	12	Educational and fun	N/A	
3	1	1	0	0	0	1	34	Educational and fun	10.4	
4	1	1	1	0	0	1	31	Educational and fun	3.7	
5	0	1	1	0	1	0	33	Educational and fun	2.4	
6	1	1	1	1	1	0	37	Educational and fun	2.4	
7	1	1	0	1	0	1	125	Educational and fun	3.9	
8	1	1	1	1	0	1	35	Educational and fun	3.4	
9	1	1	0	1	1	0	56	Educational and fun	2.4	
10	0	1	1	1	1	0	33	Educational and fun	6.9	
11	1	1	0	1	1	0	46	Educational and fun	2.4	
12	1	1	1	1	1	1	13	Boring but educational	7.2	
13	0	1	1	1	1	1	49	Boring but educational	8.7	
14	1	1	1	1	1	1	41	Boring and not educational	7.2	
15	1	1	1	1	1	1	33	Educational and fun	4.2	
Transtar										
16	1	1	1	0	0	0	76000	Educational and fun	7.5	
17	0	0	0	0	0	0	97000	Educational and fun	5.2	
18	0	0	0	0	0	0	N/A	N/A	N/A	
19	0	0	0	0	0	0	222765	Educational and fun	15.4	
20	0	0	0	0	0	0	51000	Boring but educational	4.4	
21	0	0	0	1	0	0	N/A	Educational and fun	N/A	
22	1	0	1	1	1	0	0	I had technical difficulties	3.8	
23	1	1	1	1	0	1	0	I had technical difficulties	2.3	
24	0	0	0	0	1	1	0	I had technical difficulties	2.9	
25	0	1	0	1	1	0	0	I had technical difficulties	N/A	
26	1	1	0	1	1	1	88	I had technical difficulties	5.1	
27	1	1	1	1	1	1	0	I had technical difficulties	5.2	
28	1	1	1	1	1	1	5600	Educational and fun	7.5	
29	1	1	1	1	1	1	83000	Fun but not educational	7.5	

Table 3.3: The results of experiment #2

	Average Difference	Standard Deviation	Average Time Spent	Significance
Transformation Golf	-0.27	1.29830602	5	
Transtar	0.07	1.2860195	7.1	
				p = 0.416468389

Table 3.4: The average difference in pre and post-tests, the standard deviation, the average time spent, and the statistical significance of experiment #2's data

4 of the 15 students who played *Transformation Golf* did more poorly on their post-test than they did on their pre-test. Most demonstrated the same performance from pre to post-test. 2 of the 14 students who played *Transtar* performed worse on their post-tests and most did not demonstrate different performance. Only one student who played *Transformation Golf* showed improvement from pre to post-test, compared to the four students that improved after playing *Transtar*.

13 of the students who played *Transformation Golf* obtained “good” scores at above 30. Most of the students reported the game as “educational and fun” but 3 thought it was “boring” and 1 thought it was “not educational.” Even though multiple students spent only 2.4 minutes playing the game, none spent less. The most time spent was 10.4 and the average time spent was 5 minutes-- the time they were asked to spend.

Many students reported experiencing “technical difficulties” when attempting to play *Transtar*. Those that played with no problem tended to score “well,” or above 50000, with only one student scoring below. Most of the students who played the game said that it was “educational and fun” with one student believing it be only “fun” and another only believing it be “educational.” No students spent less than 2.3 minutes playing *Transtar* but none spent more than 7.5. The average time spent playing was 7.1 minutes.

Unfortunately, the data on *Transtar* is less complete than the data on *Transformation Golf* because most students reported technical difficulties. The reason for this is unknown-- the link in the experiment is functioning and *Transtar* has not been taken down like *Transformation Golf* was soon after the experiment was completed. Possible reasons might include browser or firewall issues. Additionally, *Transtar*'s initial load time might have been substantial on

low-performance machines, though it would likely not have exceeded a minute. Some students may have thought that the game was not loading and given up.

The average difference between pre and post-tests of students who played *Transformation Golf* is $-.27$, meaning that, on average, students performed worse after playing the game. The average difference of students who played *Transtar* is $.07$, meaning students tended to demonstrate some statistically insignificant improvement. However, if students who reported technical difficulties are factored out, the average difference was $-.25$ which is similar to the difference above. Unfortunately, the statistical significance of the results was $.42$, significantly higher than the desired $.05$. This was due to a relatively small sample size, which was made smaller due to a small amount of unusable data not analyzed here.

Experiment #3

Multiplying Binomials: ASSISTments vs Rags to Riches

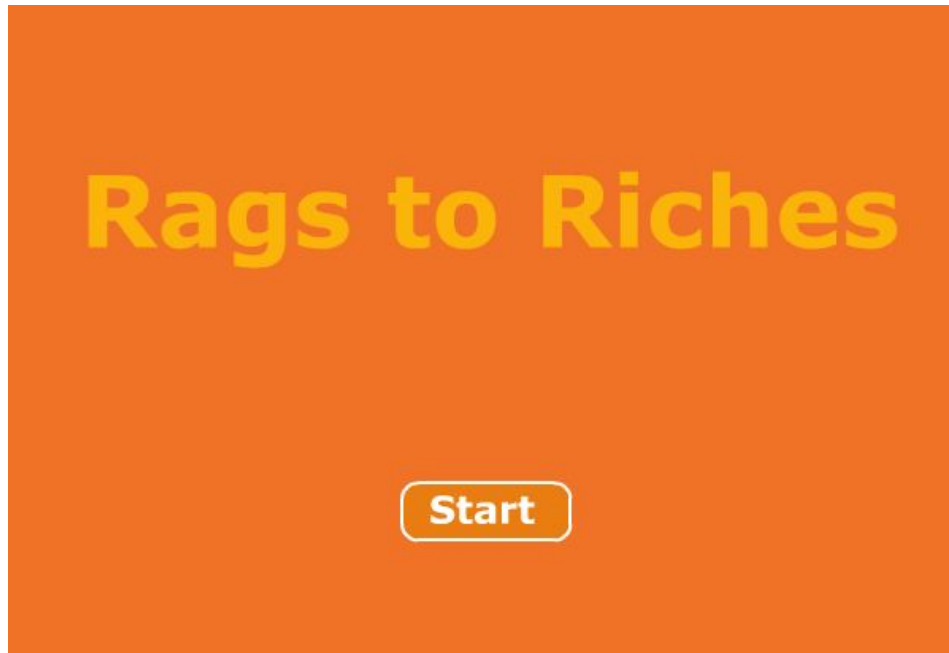


Fig 3.8: *Rags to Riches: Multiplying Binomials*

Rags to Riches: Multiplying Binomials, a game hosted on quia.com, was chosen for this experiment because it was believed to be a “bad” game. It lacks many of the features and visual flair of the other games, and is simply not much different from a series of relevant problems.

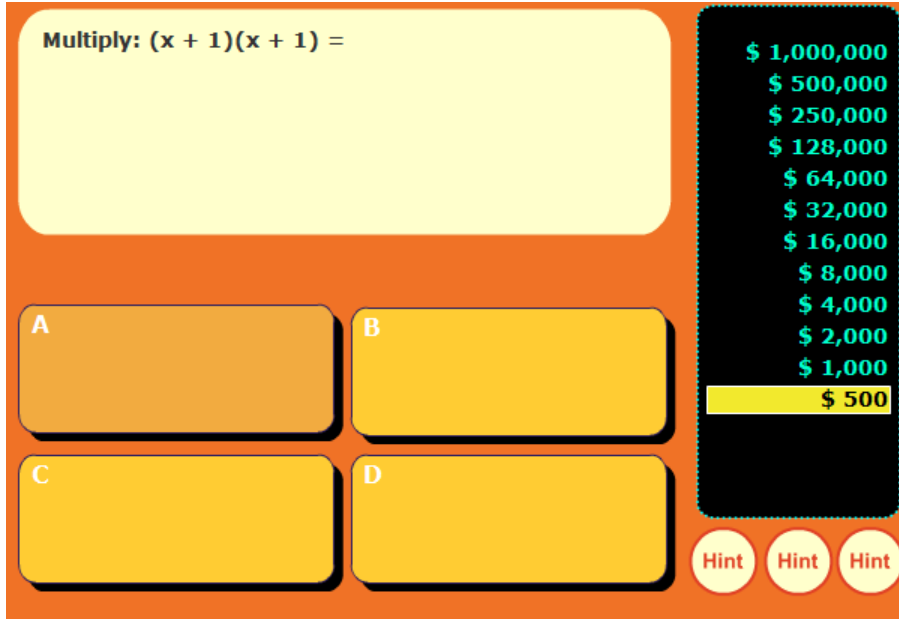


Fig 3.9: Players earn money as they get more questions correct

Players are given a problem, and choose from four possible answers. As they progress through the game they earn more money until they earn one million dollars or get a single question wrong.

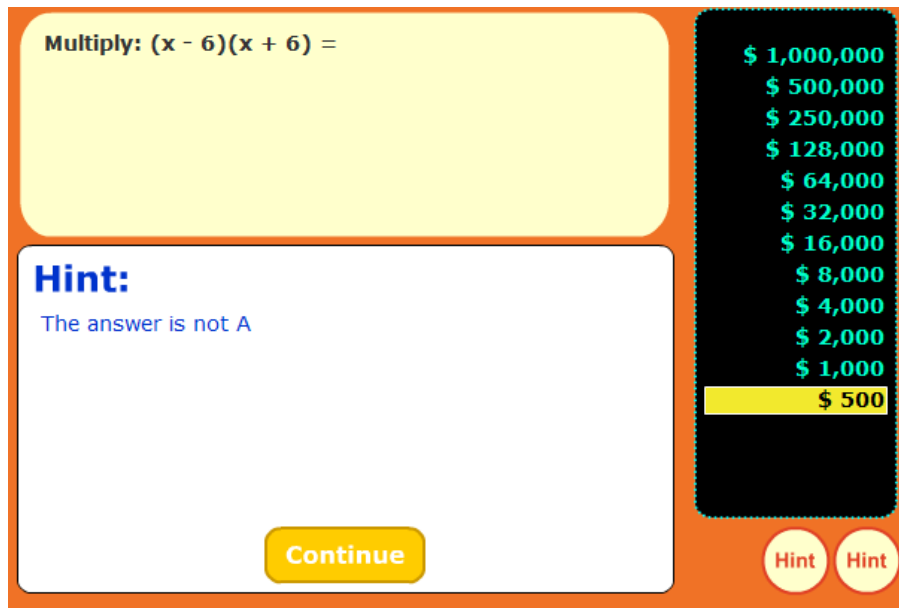


Fig 3.10: The hints do not attempt to tutor, instead they eliminate possible answers

Players are given a total of three hints to use across the course of the entire game. These hints simply tell the player which answers are incorrect, and offer nothing in the way of tutoring like ASSISTments. *Rags to Riches* did not seem particularly educational.

Students participating in the experiment who were tasked to play *Rags to Riches* were asked to spend at least five minutes playing the game and to post their high scores when they were done. Additionally, they were presented the following choices for feedback about the game:

- The game was educational and fun
- The game was boring but educational
- The game was fun but not educational
- The game was not educational or fun

Approximately half of the students were presented with a link to a series of pre-set problems where they were asked to multiply binomials for at least five minutes. They were asked to record how many problems they had answered in the time that they had spent.

At the time of this report, no meaningful data has come from this experiment.

Experiment #4

Parabolas: ASSISTments augmented with the pHet equation grapher vs

ASSISTments

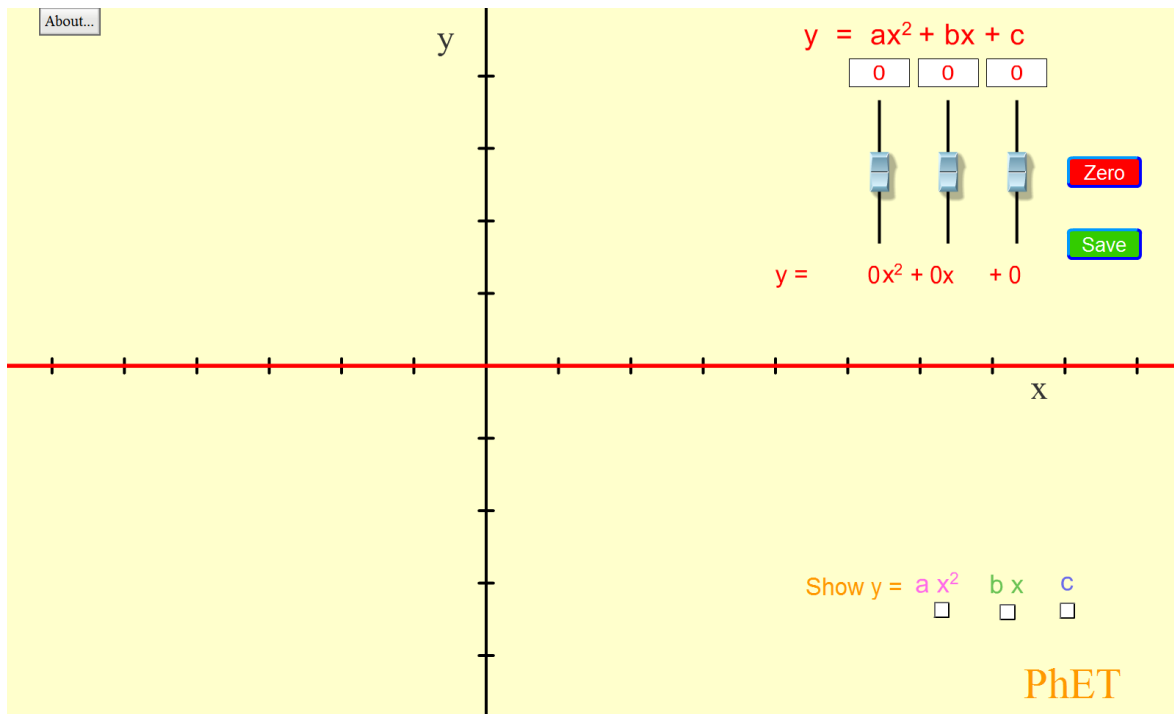


Fig 3.11: The pHet equation grapher is an in-browser tool where students can graph equations in real time

The pHet equation grapher was chosen for this experiment because it offers a visual and exploratory element otherwise not present in ASSISTments. Students using the equation grapher can enter values for a , b , and c and see in real time how the graph of their equation changes.

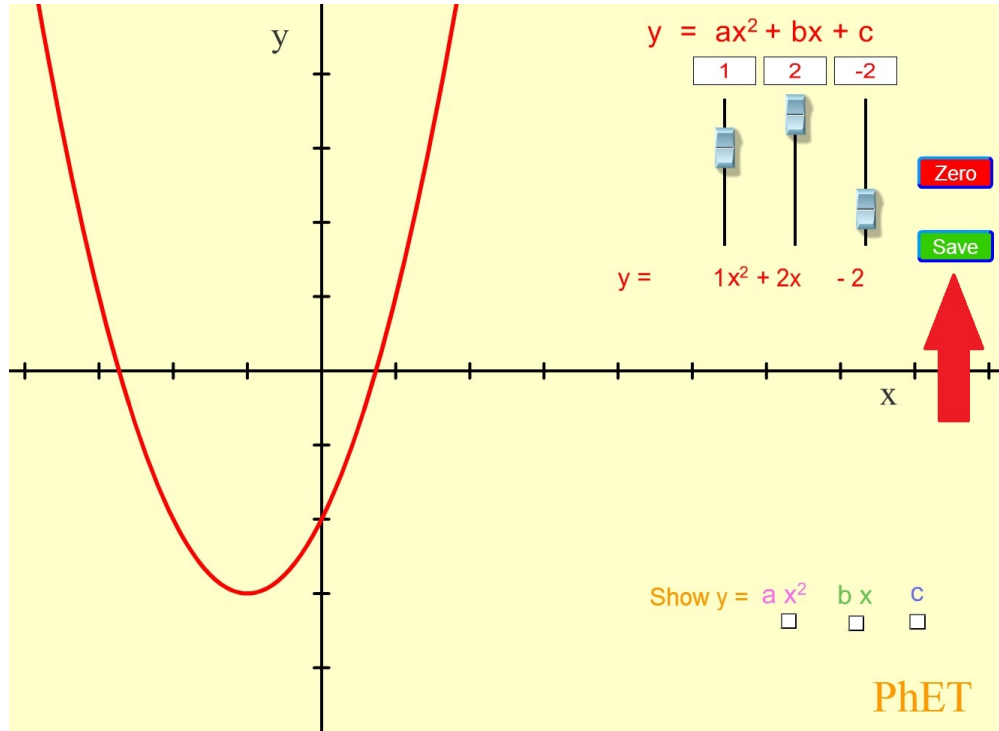


Fig 3.12: An example of a tutorial image used to brief students on how to use the equation grapher

Students can enter values manually into the a, b, and c text fields or adjust the sliders below. They can also save a graphed equation to compare it to a new function, both of which are displayed in different colors simultaneously on the screen. All of the functions and features of the equation grapher were made clear to students with access to it through concise visual tutorials.

ASSISTments Teacher Student Builder

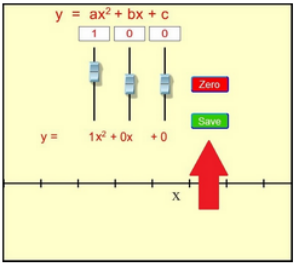
Need help on this page? About

Problem: 1 / 1

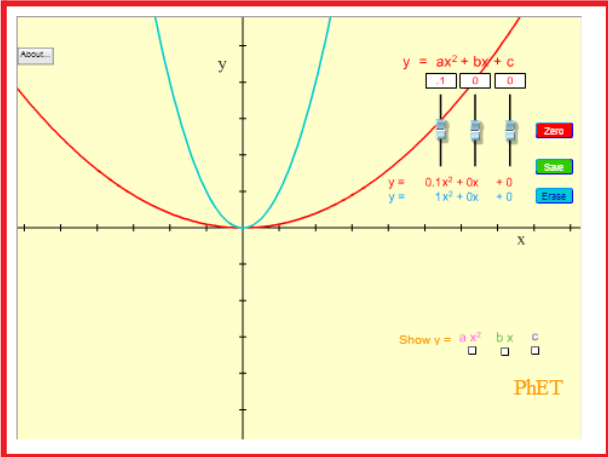
Assignment: Assistent #375736

Assistent ID: 375736

Scroll down to the equation grapher and enter the value 1 for a. Click the **Save** button. Your parabola should turn blue.



Enter the value .1 for a. You should see two parabolas. Which one is wider, the **red** one (a = .1) or the **blue** one (a = 1)?



Select one:

Red (a = .1)

Blue (a = 1)

Submit Answer

Fig 3.13: The pHet tool is directly embedded into the ASSISTments system for easy access, as shown by the red box (not normally present in the problem set)

One of the benefits of the pHet equation grapher was that it could be directly embedded into problems within the ASSISTments system. This theoretically greatly facilitates the learning process as students learn about parabolas.

The experiment was designed so that students who did not get directed to the equation grapher

version of the problem set received an extremely similar version with the same problems, albeit without the equation grapher or equation grapher tutorial. Students who have access to the equation grapher have the opportunity to practice a few problems with the assistance of the tool, but both groups are given the same, unassisted pre and post-tests.

4 Conclusion and Final Thoughts

From the start, our project team sought to test the viability and effectiveness of educational math games and tools at a roughly high school level. Educational math games have demonstrated their ability to teach and engage younger students, but higher level math students rarely use such software. Furthermore, such software is rare, and relevant software of a high quality is even rarer. ASSISTments is a perfect platform to test the responses to educational games and tools because it offers a variety of features like tutoring, custom hints, and variablized templates, as well as recording detailed data for teachers and experimenters to use and analyze.

Of the four experiments that were built, only two yielded meaningful results. The third experiment was used by a single teacher, and many of the students seemingly quit halfway through. The fourth and most complicated experiment has not yet been used by any teachers, but teachers have expressed interest.

Of the two experiments that yielded meaningful results, it seems that games may not be an

effective method of learning in this context. While students generally reported that the games were fun and educational, the results disagree. Most students who played the games did not demonstrate improvement, and in some cases did more poorly afterwards. Students seemed more willing to spend a long time practicing problems directly, rather than learning how to play a game and attempting to get a high score. In fact, no students spent less than the requested time attempting to solve problems, while several across both experiments spent as little as two minutes playing games. It is unclear if this is due to student preference, the perceived quality of the games, or a combination of both factors. It is worth noting that many students reported technical difficulties on one game, and that another game has been taken down since the experiment was completed. Avoiding long load times may be prudent, and if the fluidity of the internet is also a factor.

In the end, practice problems within the ASSISTments system were shown to be more effective than the games picked for the experiment. More testing is needed, however-- these experiments are far from offering definitive proof. Games and software may have an important role in high school math education, and more experiments should be conducted to determine the nature of that role.

Appendices

Problem Set "Factoring Quadratics Experiment" id:[77824]**1) Assistment #84255 "84255 - 43056"**

Factor the following polynomial:

$$x^2 + 12x + 27$$

Once you have the polynomial factored enter one of the two factors

Algebra:

✓ (x+3)

✓ (x+9)

✓ (-x-3)

✓ (-x-9)

Hints:

- Factoring means you want to get the polynomial in this form

$$(__x + __)(__x + __)$$

(Note: The signs may change.)

The question is asking for only one of factors: (x + ___).

- We have: $x^2 + 12x + 27$

Since the product of the last terms must be 27, and 27 has three prime factors (3, 3, and 3).

The last terms could be:

27 and 1, because $27 \cdot 1 = 27$

-27 and -1, because $-27 \cdot -1 = 27$

3 and 9, because $3 \cdot 9 = 27$

-3 and -9, because $-3 \cdot -9 = 27$

9 and 3, because $9 \cdot 3 = 27$

-9 and -3, because $-9 \cdot -3 = 27$

3 and 9, because $3 \cdot 9 = 27$

-3 and -9, because $-3 \cdot -9 = 27$

- To find which set is right, we need to determine which results in b. Because the coefficient of x^2 is one, only the sum of the last terms need to add to b.

Thus we must look at all possible combinations until we find the one that will result in b. 12

Thus we must look at all possible combinations until we find the one that will result in 0, 12.

$$(x + 27)(x + 1) : (x * 1) + (x * 27) = 28x$$

$$(x - 27)(x - 1) : (x * -1) + (x * -27) = -28x$$

$$(x + 3)(x + 9) : (x * 9) + (x * 3) = 12x$$

$$(x - 3)(x - 9) : (x * -9) + (x * -3) = -12x$$

$$(x + 3)(x + 9) : (x * 9) + (x * 3) = 12x$$

$$(x - 3)(x - 9) : (x * -9) + (x * -3) = -12x$$

$$(x + 9)(x + 3) : (x * 3) + (x * 9) = 12x$$

$$(x - 9)(x - 3) : (x * -3) + (x * -9) = -12x$$

- Only $(x + 3)(x + 9)$ results in the correct b value

Type either $(x+3)$ or $(x+9)$.

2) Assistment #84262 "84262 - 43056"

Factor the following polynomial:

$$x^2 + 6x + 8$$

Once you have the polynomial factored enter one of the two factors

Algebra:

✓ $(x+2)$

✓ $(x+4)$

✓ $(-x-2)$

✓ $(-x-4)$

Hints:

- Factoring means you want to get the polynomial in this form

$$(___x + ___)(___x + ___)$$

(Note: The signs may change.)

The question is asking for only one of factors: $(x + ___)$.

- We have: $x^2 + 6x + 8$

Since the product of the last terms must be 8, and 8 has three prime factors (2, 2, and 2).

The last terms could be:

8 and 1, because $8 \cdot 1 = 8$

-8 and -1, because $-8 \cdot -1 = 8$

2 and 4, because $2 \cdot 4 = 8$

-2 and -4, because $-2 \cdot -4 = 8$

4 and 2, because $4 \cdot 2 = 8$

-4 and -2, because $-4 \cdot -2 = 8$

2 and 4, because $2 \cdot 4 = 8$

-2 and -4, because $-2 \cdot -4 = 8$

- To find which set is right, we need to determine which results in b. Because the coefficient of x^2 is one, only the sum of the last terms need to add to b.

Thus we must look at all possible combinations until we find the one that will result in b, 6.

$$(x + 8)(x + 1) : (x \cdot 1) + (x \cdot 8) = 9x$$

$$(x - 8)(x - 1) : (x \cdot -1) + (x \cdot -8) = -9x$$

$$(x + 2)(x + 4) : (x \cdot 4) + (x \cdot 2) = 6x$$

$$(x - 2)(x - 4) : (x \cdot -4) + (x \cdot -2) = -6x$$

$$(x + 2)(x + 4) : (x \cdot 4) + (x \cdot 2) = 6x$$

$$(x - 2)(x - 4) : (x \cdot -4) + (x \cdot -2) = -6x$$

$$(x + 4)(x + 2) : (x \cdot 2) + (x \cdot 4) = 6x$$

$$(x - 4)(x - 2) : (x \cdot -2) + (x \cdot -4) = -6x$$

- Only $(x + 2)(x + 4)$ results in the correct b value

Type either $(x+2)$ or $(x+4)$.

3) Assistment #84278 "84278 - 43056"

Factor the following polynomial:

$$x^2 + 18x + 45$$

Once you have the polynomial factored enter one of the two factors

Algebra:

✓ $(x+3)$

✓ $(x+15)$

✓ $(-x-3)$

✓ $(-x-15)$

Hints:

- Factoring means you want to get the polynomial in this form

$$(__x + __)(__x + __)$$

(Note: The signs may change.)

The question is asking for only one of factors: ($__x + __$).

- We have: $x^2 + 18x + 45$

Since the product of the last terms must be 45, and 45 has three prime factors (5, 3, and 3).

The last terms could be:

45 and 1, because $45 \cdot 1 = 45$

-45 and -1, because $-45 \cdot -1 = 45$

5 and 9, because $5 \cdot 9 = 45$

-5 and -9, because $-5 \cdot -9 = 45$

15 and 3, because $15 \cdot 3 = 45$

-15 and -3, because $-15 \cdot -3 = 45$

3 and 15, because $3 \cdot 15 = 45$

-3 and -15, because $-3 \cdot -15 = 45$

- To find which set is right, we need to determine which results in b. Because the coefficient of x^2 is one, only the sum of the last terms need to add to b.

Thus we must look at all possible combinations until we find the one that will result in b, 18.

$$(x + 45)(x + 1) : (x \cdot 1) + (x \cdot 45) = 46x$$

$$(x - 45)(x - 1) : (x \cdot -1) + (x \cdot -45) = -46x$$

$$(x + 5)(x + 9) : (x \cdot 9) + (x \cdot 5) = 14x$$

$$(x - 5)(x - 9) : (x \cdot -9) + (x \cdot -5) = -14x$$

$$(x + 3)(x + 15) : (x \cdot 15) + (x \cdot 3) = 18x$$

$$(x - 3)(x - 15) : (x \cdot -15) + (x \cdot -3) = -18x$$

$$(x + 15)(x + 3) : (x \cdot 3) + (x \cdot 15) = 18x$$

$$(x - 15)(x - 3) : (x \cdot -3) + (x \cdot -15) = -18x$$

- Only $(x + 3)(x + 15)$ results in the correct b value

Type either $(x+3)$ or $(x+15)$.

4) Assistment #377868 "377868 - Wrecks Instructions"

In the next step you are going to play **Wrecks Factor**, a game about factoring quadratics, for at least five minutes. Be sure to remember your **high score** when you are done playing!

The game will guide you through a brief tutorial. If you want further help you can click the Help button on the main menu.

Please leave all of the settings on default.

When you are done, return to this window and continue.

What are you going to do?

Multiple choice:

- ✓ Continue and play Wrecks Factor for at least five minutes.
- ✗ Go shopping
 - No, you are going to continue and play Wrecks Factor for at least five minutes.
- ✗ Write a poem
 - No, you are going to continue and play Wrecks Factor for at least five minutes.

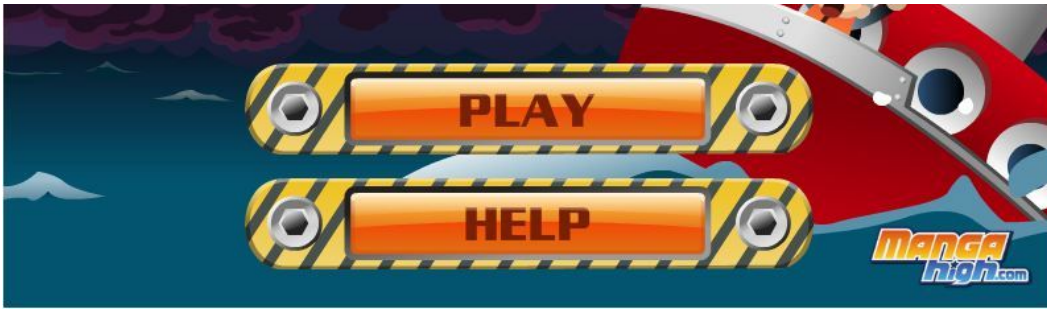
Hints:

- The answer is

5) Assistment #377869 "377869 - Wrecks Game"

Click the picture below and play the game for at least five minutes (you can play more if you want to!). Remember to keep track of your score!





When you are done, enter your highscore below and continue.

Fill in:

✓ 17

Hints:

- The answer is

6) Assistment #377506 "377506 - Game Survey"

Did you think the game was:

Multiple choice:

- ✓ Educational and fun?
- ✓ Fun but not educational?
- ✓ Boring but educational?
- ✓ Boring and not educational?
- ✓ I had technical difficulties.

Hints:

- The answer is

7) Assistment #378227 "378227 - ASSISTments Instruction"

In the next step you are going to answer a series of questions on **ASSISTments**.

When you click the ASSISTments image, a new window will open and you will answer questions for at least five minutes, but you may continue as long as you want.

When you are done, you will enter your score and then continue.

What are you going to do on the next page?

Multiple choice:

- ✓ Click the ASSISTments link, use it for at least five minutes, then enter your score
- ✗ Go shopping
 - No, you are going to continue and play Wrecks Factor
- ✗ Write a poem
 - No, you are going to continue and play Wrecks Factor

Hints:

- The answer is

8) Assistment #378226 "378226 - ASSISTments Test Drive"

Please click on the picture below and answer questions for at least five minutes.



When you're done enter how many questions you answered below.

Fill in:

✓ 17

Hints:

- The answer is

9) Assistment #84249 "84249 - 43056"

Factor the following polynomial:

$$x^2 + 12x + 35$$

Once you have the polynomial factored enter one of the two factors

Algebra:

✓ (x+7)

✓ (x+5)

✓ (-x-7)

✓ (-x-5)

Hints:

- Factoring means you want to get the polynomial in this form

$$(__x + __)(__x + __)$$

(Note: The signs may change.)

The question is asking for only one of factors: (x + ___).

- We have: $x^2 + 12x + 35$

Since the product of the last terms must be 35

The last terms could be:

35 and 1, because $35 \cdot 1 = 35$

-35 and -1, because $-35 \cdot -1 = 35$

7 and 5, because $7 \cdot 5 = 35$ OR

-7 and -5, because $-7 \cdot -5 = 35$

- To find which set is right, we need to determine which results in b. Because the coefficient of x^2 is one, only the sum of the last terms need to add to b.

Thus we must look at all possible combinations until we find the one that will result in b.

$$(x + 35)(x + 1) : (x \cdot 1) + (x \cdot 35) = 36x$$

$$(x - 35)(x - 1) : (x \cdot -1) + (x \cdot -35) = -36x$$

$$(x + 7)(x + 5) : (x \cdot 7) + (x \cdot 5) = 12x$$

$$(x - 7)(x - 5) : (x \cdot -7) + (x \cdot -5) = -12x$$

- Only $(x + 7)(x + 5)$ results in the correct b value

Type either $(x+7)$ or $(x+5)$.

10) Assistment #84191 "84191 - 43056"

Factor the following polynomial:

$$x^2 + 6x + 9$$

Once you have factored the polynomial, please enter one of the factors below.

Algebra:

✓ $(x+3)$

✓ $(-x-3)$

Hints:

- Factoring means you want to get the polynomial in this form

$$(__x + __)(__x + __)$$

Since $x^2 + 6x + 9$ has no coefficient to x^2 , neither of the x's in the factored form have a coefficient, meaning you only have to find the values of the two blanks.

$$(x + __)(x + __)$$

The question is only asking for only one of the factors: $(x + __)$

- We have: $x^2 + 6x + 9$

Since the product of the last terms must be 9

The last terms could be:

3 and 3 , because $3*3=9$

-3 and -3, because $-3*-3=9$

9 and 1, because $9*1 = 9$ OR

-9 and -1, because $-9*-1 = 9$

So you either have:

$$(x + 3)(x + 3)$$

$$(x - 3)(x - 3)$$

$$(x + 9)(x + 1)$$

$$(x - 9)(x - 1)$$

- To determine which of the four is correct, you must re-expand each and find a match to the original problem.

When you multiply you get:

$$(x + 3)(x + 3) = x^2 + 3x + 3x + 9 = x^2 + 6x + 9$$

$$(x - 3)(x - 3) = x^2 - 3x - 3x + 9 = x^2 - 6x + 9$$

$$(x + 9)(x + 1) = x^2 + 9x + x + 9 = x^2 + 10x + 9$$

$$(x - 9)(x - 1) = x^2 - 9x - x + 9 = x^2 - 10x + 9$$

- This one is correct:

$$(x + 3)(x + 3) = x^2 + 3x + 3x + 9 = x^2 + 6x + 9$$

Type (x+3).

This means the original polynomial is a special polynomial. If the polynomial is of the form $x^2 + (2*c^{1/2})x + c$ (b is 2 times the square root of c) then the answer will always be $(x + [\text{The square root of } c])^2$.

11) Assistment #84285 "84285 - 43056"

Factor the following polynomial:

$$x^2 + 26x + 105$$

Once you have the polynomial factored enter one of the two factors

Algebra:

✓ (x+5)

✓ (x+21)

✓ (-x-5)

✓ (-x-21)

Hints:

- Factoring means you want to get the polynomial in this form

$$(\underline{\quad}x + \underline{\quad})(\underline{\quad}x + \underline{\quad})$$

(Note: The signs may change.)

The question is asking for only one of factors: ($\underline{\quad}x + \underline{\quad}$).

- We have: $x^2 + 26x + 105$

Since the product of the last terms must be 105, and 105 has three prime factors (7, 3, and 5).

The last terms could be:

105 and 1, because $105 \cdot 1 = 105$

-105 and -1, because $-105 \cdot -1 = 105$

7 and 15, because $7 \cdot 15 = 105$

-7 and -15, because $-7 \cdot -15 = 105$

21 and 5, because $21 \cdot 5 = 105$

-21 and -5, because $-21 \cdot -5 = 105$

3 and 35, because $3 \cdot 35 = 105$

-3 and -35, because $-3 \cdot -35 = 105$

- To find which set is right, we need to determine which results in b. Because the coefficient of x^2 is one, only the sum of the last terms need to add to b.

Thus we must look at all possible combinations until we find the one that will result in b, 26.

$$(x + 105)(x + 1) : (x \cdot 1) + (x \cdot 105) = 106x$$

$$(x - 105)(x - 1) : (x \cdot -1) + (x \cdot -105) = -106x$$

$$(x + 7)(x + 15) : (x \cdot 15) + (x \cdot 7) = 22x$$

$$(x - 7)(x - 15) : (x \cdot -15) + (x \cdot -7) = -22x$$

$$(x + 3)(x + 35) : (x \cdot 35) + (x \cdot 3) = 38x$$

$$(x - 3)(x - 35) : (x \cdot -35) + (x \cdot -3) = -38x$$

$$(x + 21)(x + 5) : (x \cdot 5) + (x \cdot 21) = 26x$$

$$(x - 21)(x - 5) : (x \cdot -5) + (x \cdot -21) = -26x$$

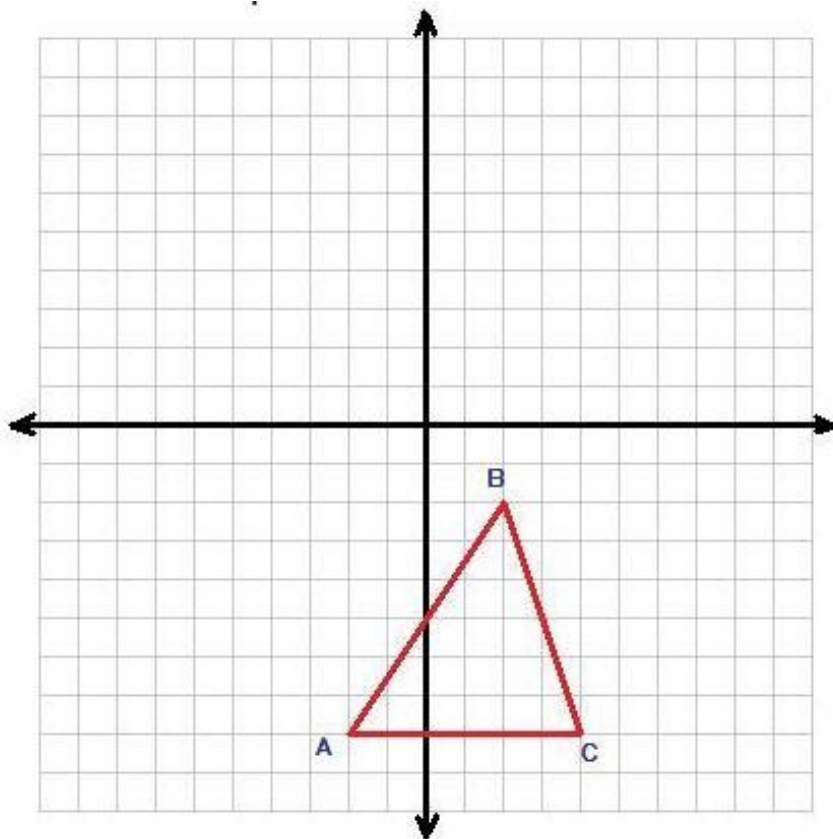
- Only $(x + 5)(x + 21)$ results in the correct b value

Type either $(x+5)$ or $(x+21)$.

Problem Set "Translations and Reflections Experiment" id:[79354]

1) Assistment #369011 "369011 - Triangle Reflection"

Reflect the triangle across the **x axis**. What are the coordinates of point **A** after the reflection?



Fill in:

- ✓ (-2,8)
- ✓ (-2 ,8)
- ✓ (-2, 8)
- ✓ (-2 , 8)
- ✓ -2,8
- ✓ -2, 8
- ✓ -2 ,8
- ✓ -2 , 8

Hints:

- To reflect, you need to flip the shape over the **x axis**.
- The current coordinates of point **A** are **(-2,-8)**
- The **x-value...**
stays the same when reflect across the **x-axis**
is multiplied it by **-1** when reflecting across the **y-axis**

is multiplied it by -1 when reflecting across the y-axis.

The y-value...

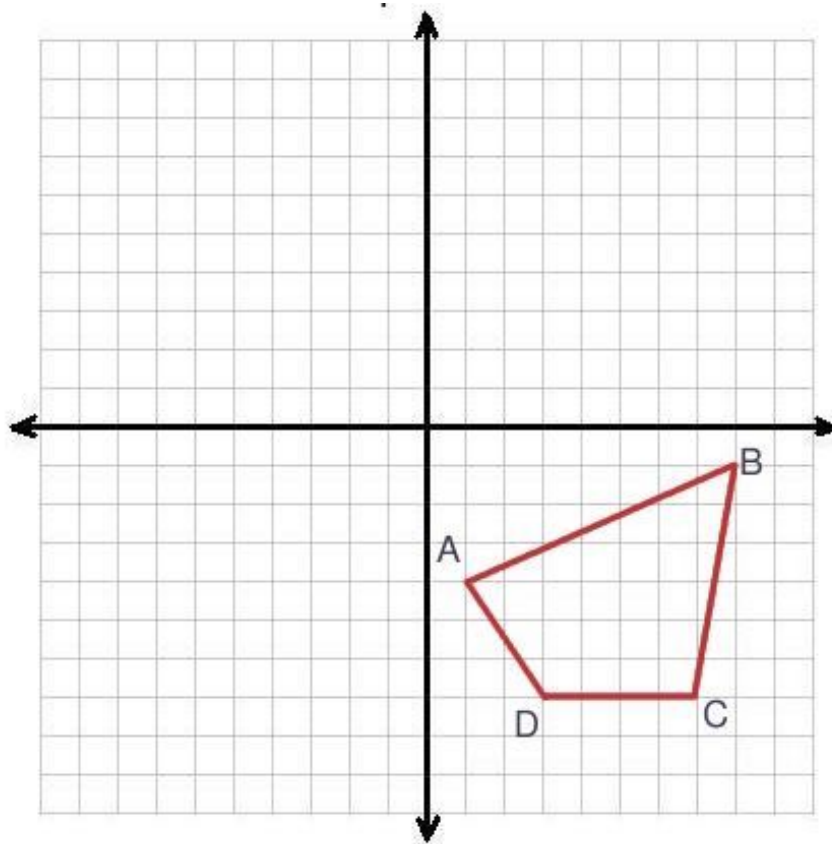
stays the same when reflect across the y-axis

is multiplied it by -1 when reflecting across the x-axis.

Type in (-2,8)

2) Assistment #368994 "368994 - Quadrilateral Translation"

Translate the quadrilateral left 4 units and up 5 units. What are the coordinates of point **B** after the translation?



Fill in:

✓ (4,4)

✓ (4,4)

✓ (4,4)

✓ (4,4)

✓ 4,4

✓ 4,4

✓ 4,4

✓ 4,4

Hints:

- To translate, you need to start at each point and count 4 to the left and then 5 up.

- The current coordinates of point **B** are (8,-1)
- From (8,-1) you will move to (4,4).

Type in (4,4)

3) Assistent #378509 "378509 - Triangle Rotation"

Rotate the triangle clockwise about the origin 180 degrees. What are the coordinates of point **B** after the rotation?

Fill in:

- ✓ (-7,2)
- ✓ (-7 ,2)
- ✓ (-7, 2)
- ✓ (-7 , 2)
- ✓ -7,2
- ✓ -7, 2
- ✓ -7 ,2
- ✓ -7 , 2

Hints:

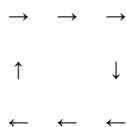
- Redraw the triangle on a seperate sheet of paper.

Rotating about the origin means that (0,0) on the graph will be the center of the rotation.

- 90 degree rotation is a quarter turn.

180 degree rotation is a half turn.

Clockwise means the direction that a clock moves.



Rotate your drawing 180 degrees.

- The current coordinates of the point B are (7,-2)

When you rotate 90 degrees the x and y values reverse. Also the sign will change on one of the two numbers.

When you rotate 180 degrees the sign will change on x and y values.

- The x-value of point B will change from 7 to -7 when you rotate 180 degrees.

The y-value will change from -2 to 2.

Type in (-7,2)

4) Assistment #377820 "377820 - Transtar Instructions"

In the next step you are going to be playing **Transtar**, a game about translations, reflections, and rotations, for at least five minutes. Be sure to remember your **high score** when you are done playing!

The game will guide you through a brief tutorial. If you want more help you can click the Help button on the main menu.

When you are done, return to this window and [continue](#).

What are you going to do?

Multiple choice:

Go to bed

- No you're going to play Transtar for at least five minutes before returning to this window.

Learn to knit

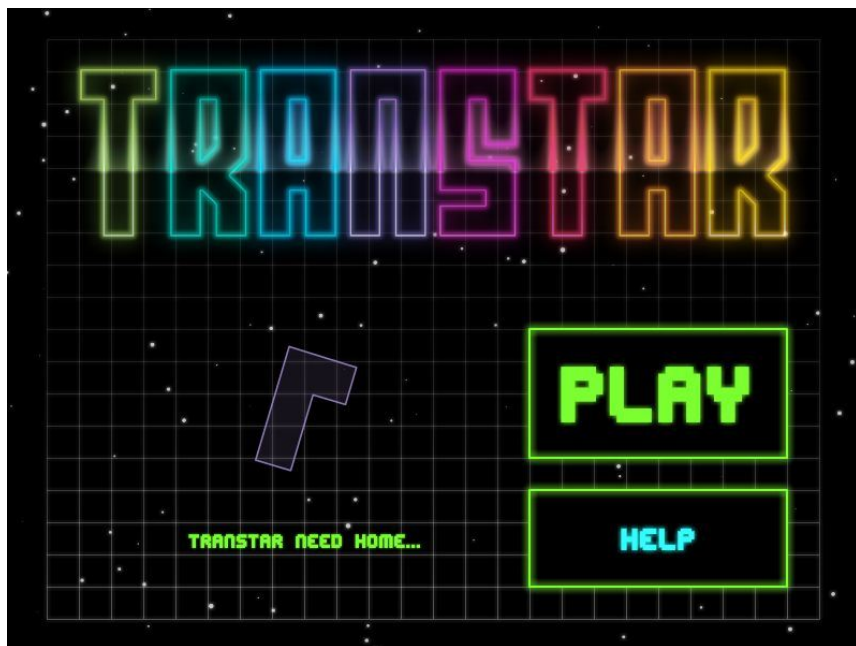
- No you're going to play Transtar for at least five minutes before returning to this window.

Continue and play Transtar for at least five minutes before returning to this window.

Hints:

5) Assistent #377821 "377821 - transtar2"

Please click the picture below and play the game for at least five minutes. Remember to keep track of your score!



When you are done, enter your highscore below and continue.

Fill in:

✓ 17

Hints:

- The answer is

6) Assistent #377506 "377506 - Game Survey"

Did you think the game was:

Multiple choice:

- ✓ Educational and fun?
- ✓ Fun but not educational?
- ✓ Boring but educational?
- ✓ Boring and not educational?
- ✓ I had technical difficulties.

Hints:

- The answer is

7) Assistment #369091 "369091 - Please click the ..."

In the next step you will be playing **Transformation Golf**, a game about rotations, reflections, and translations, for at least five minutes. Be sure to remember your **high score** when you are done playing!

The goal of the game is to translate, reflect, and rotate the golf ball into the hole.

When you are done, return to this window and continue.

What are you going to do?

Multiple choice:

- Draw a picture
 - No, you are going to continue and play Transformation Golf for at least five minutes before returning to this window.
- Learn to knit
 - No, you are going to continue and play Transformation Golf for at least five minutes before returning to this window.
- Continue and play Transformation Golf for at least five minutes before returning to this window.
- Help around the house
 - No, but that's considerate of you.

8) Assistment #377508 "377508 - transgolf"

Please click the picture below and play the game for at least five minutes (you can play more if you want to!). Remember to keep track of your high score!

Transformation Golf

hole number
1

par for this hole
3

Score
3

Par score
0

3 shots on this hole

see your scorecard

next hole
 yes no

[Help!](#)

When you are done, enter your highscore below and continue.

Fill in:

✓ 17

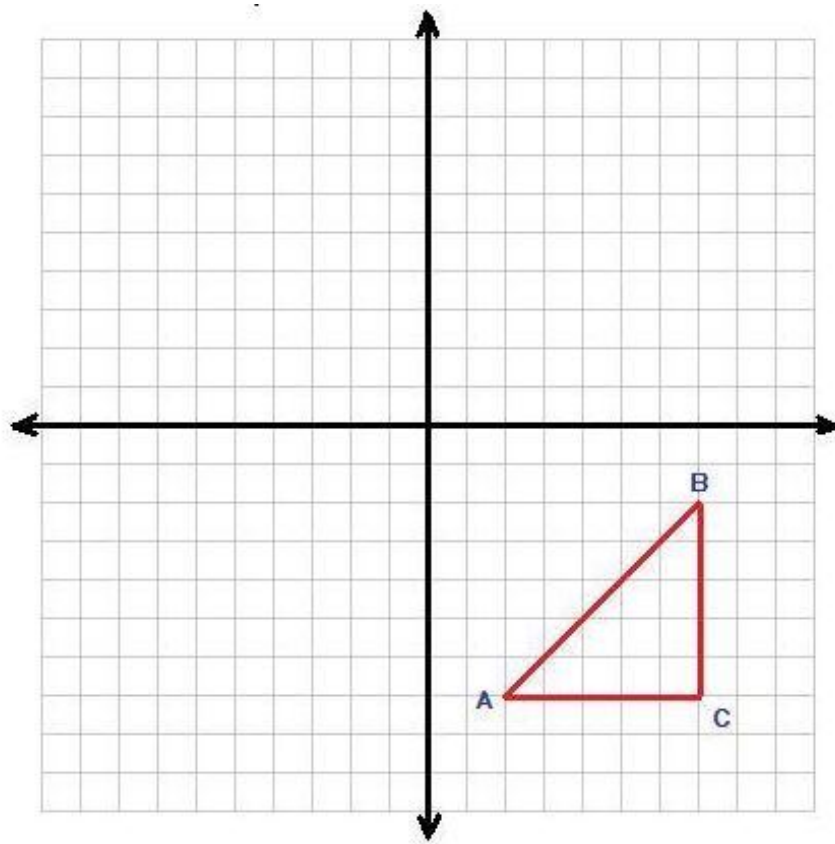
Hints:

- The answer is

9) Duplicate assistment: Assistment #377506 "377506 - Game Survey" was not displayed.

10) Assistment #369005 "369005 - Triangle Reflection"

Reflect the triangle across the **x axis**. What are the coordinates of point **A** after the reflection?

**Fill in:**

✓ (2,7)

✓ (2,7)

✓ (2,7)

✓ (2,7)

✓ 2,7

✓ 2,7

✓ 2,7

✓ 2,7

Hints:

- To reflect, you need to flip the shape over the x axis.
- The current coordinates of point A are (2,-7)
- The x-value... stays the same when reflect across the x-axis is multiplied it by -1 when reflecting across the y-axis.

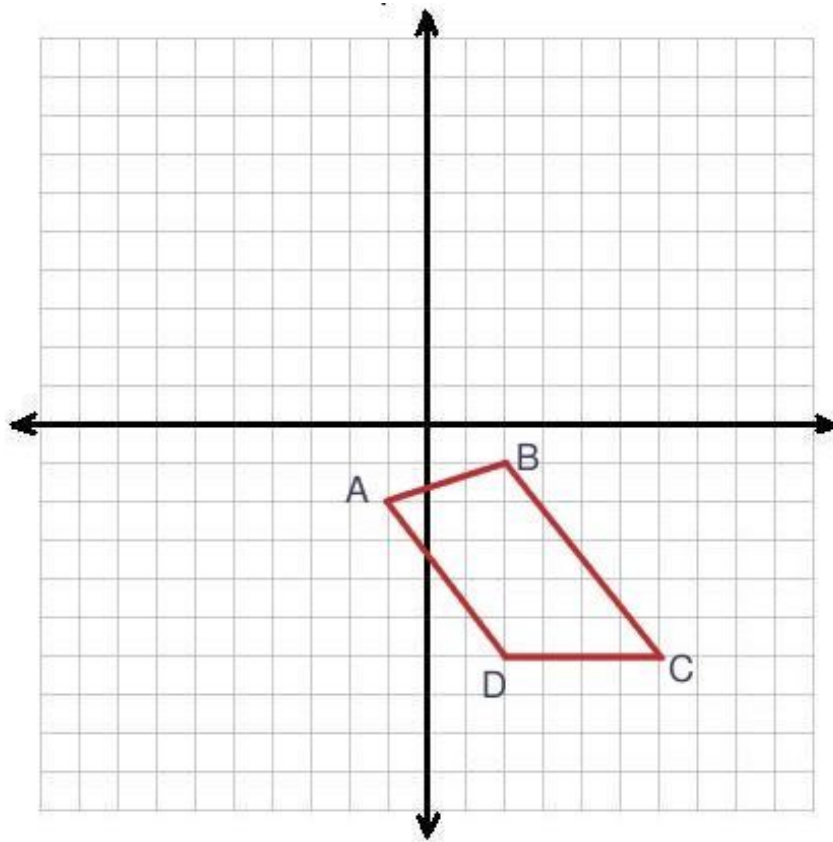
The y-value...

stays the same when reflect across the y-axis
is multiplied it by -1 when reflecting across the x-axis.

Type in (2,7)

11) Assistent #368988 "368988 - Quadrilateral Translation"

Translate the quadrilateral **left 2** units and **up 2** units. What are the coordinates of point **D** after the translation?



Fill in:

- ✓ (0,-4)
- ✓ (0,-4)
- ✓ (0,-4)
- ✓ (0,-4)
- ✓ 0,-4
- ✓ 0,-4
- ✓ 0,-4
- ✓ 0,-4

Hints:

- To translate, you need to **start at each point and count 2 to the left and then 2 up.**
- The current coordinates of point **D** are **(2,-6)**
- From (2,-6) you will move to **(0,-4).**

Type in (0,-4)

12) Assistent #378513 "378513 - Triangle Rotation"

Rotate the triangle clockwise about the origin **90 degrees**. What are the coordinates of point **C** after the rotation?

Fill in:

- ✓ (-8,-4)
- ✓ (-8 , -4)
- ✓ (-8, -4)
- ✓ (-8 , -4)
- ✓ -8,-4
- ✓ -8, -4
- ✓ -8 , -4
- ✓ -8 , -4

Hints:

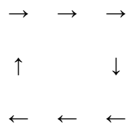
- Redraw the triangle on a seperate sheet of paper.

Rotating about the origin means that (0,0) on the graph will be the center of the rotation.

- 90 degree rotation is a quarter turn.

180 degree rotation is a half turn.

Clockwise means the direction that a clock moves.



Rotate your drawing 90 degrees.

- The current coordinates of the point C are (4,-8)

When you rotate 90 degrees the x and y values reverse. Also the sign will change on one of the two numbers.

When you rotate 180 degrees the sign will change on x and y values.

- The x-value of point C will change from 4 to -8 when you rotate 90 degrees.

The y-value will change from -8 to -4.

Type in (-8,-4)

Problem Set "Multiplying Binomials Experiment" id:[78281]

1) Assistment #112664 "112664 - Multiplying Binomials"

If the [directions](#) are [to apply](#) the distributive property to multiply these binomials:

$$(8x-7)(5x-2)$$

Which option correctly multiplies the binomials?

$$\begin{aligned} \text{a. } (8x-7)(5x-2) &= (8x)(5x)-(8x)(2)-(7)(5x)+(7)(2) \\ &= 13x^2-10x-12x+9 \\ &= 13x^2-22x+9 \end{aligned}$$

$$\begin{aligned} \text{b. } (8x-7)(5x-2) &= (8x)(5x)-(8x)(2)+(7)(5x)-(7)(2) \\ &= 40x^2-16x+35x-14 \\ &= 40x^2+19x-14 \end{aligned}$$

$$\begin{aligned} \text{c. } (8x-7)(5x-2) &= (8x)(5x)-(8x)(2)-(7)(5x)+(7)(2) \\ &= 85x^2-82x-75x+72 \\ &= 85x^2-157x+72 \end{aligned}$$

$$\begin{aligned} \text{d. } (8x-7)(5x-2) &= (8x)(5x)-(8x)(2)-(7)(5x)+(7)(2) \\ &= 40x^2-16x-35x+14 \\ &= 40x^2-51x+14 \end{aligned}$$

Multiple choice:

a

b

c

d

2) Assistment #112697 "112697 - 106491 - FOIL"

Simplify the equation:

$$(4x+5)(2x+9)$$

You need to enter your answer in the right format for the computer to grade it.

1. Use standard form, which means you put the highest power first.
2. Use the ^ to show exponents just like you do with a graphing calculator.
3. Do not put in any spaces.

For example: $6 + x^2 - 4x^3 - 2x$ is $-4x^3 + x^2 - 2x + 6$ in standard form and

You would type in: $-4x^3+x^2-2x+6$

Fill in:

✓ $8x^2+46x+45$

Hints:

- Be sure to read the rules in orange carefully.

To solve the problem:

Think of each polynomial as one side of a rectangle.

$$2x \quad + \quad 9$$

$$4x$$

+

$$5$$

- Then calculate the area for each section of the rectangle.

$$2x \quad + \quad 9$$

$$4x \quad (2x)(4x) \quad (9)(4x)$$

+

$$5 \quad (2x)(5) \quad (9)(5)$$

- Then add each area together:

$$(2x)(4x)+(9)(4x)+(2x)(5)+(9)(5)$$

and then simplify:

$$8x^2+46x+45$$

Type in: $8x^2+46x+45$

3) Assistment #112782 "112782 - FOIL"

Simplify the equation:

$$(8x+7)(3x-9)$$

You need to enter your answer in the right format for the computer to grade it.

1. Use standard form, which means you put the highest power first.
2. Use the ^ to show exponents just like you do with a graphing calculator.
3. Do not put in any spaces.

For example: $6 + x^2 - 4x^3 - 2x$ is $-4x^3 + x^2 - 2x + 6$ in standard form and
 You would type in: $-4x^3+x^2-2x+6$

Fill in:

✓ $24x^2+-51x-63$

✓ $24x^2-51x-63$

Hints:

- Be sure to read the rules in orange carefully.

To solve the problem:

Think of each polynomial as one side of a rectangle.

$$3x \qquad \qquad \qquad + \qquad \qquad -9$$

$$8x$$

+

$$7$$

- Then calculate the area for each section of the rectangle.

$$3x \qquad \qquad \qquad + \qquad \qquad -9$$

$$8x \qquad (3x)(8x) \qquad \qquad (-9)(8x)$$

+

$$7 \qquad (3x)(7) \qquad \qquad (-9)(7)$$

- Then add each area together:

$$(3x)(8x)+(-9)(8x)+(3x)(7)+(-9)(7)$$

and then simplify:

$$24x^2+-51x-63$$

Type in: $24x^2+-51x-63$

4) Assistment #369098 "369098 - Game Instructions"

In the next step you are going to play **Rags to Riches- Multiplying Binomials**, a game where you will try to earn a million dollars by successfully multiplying binomials, for at least five minutes. Be sure to remember your **high score** when you are done playing!

The game is multiple choice and you have limited number of hints if you get stuck on a question. Try to earn as much money as you can and good luck!

When you are done, return to this window and continue.

What are you going to do?

Multiple choice:

- Brew some coffee
 - No, you are going to continue and play Rags to Riches- Multiplying Binomials and return to this window
- Continue and play Rags to Riches- Multiply Polynomials and return to this window
- Clean your room
 - No, you are going to continue and play Rags to Riches- Multiplying Binomials and return to this window

5) Assistment #377495 "377495 - Rags to Riches Game"

Please click the picture below and play the game for at least five minutes (you can play more if you want to!). Make sure to keep track of your score!





When you are done, enter your highscore below and continue.

Algebra:

✓ 17

Hints:

- The answer is

6) Assistment #377506 "377506 - Game Survey"

Did you think the game was:

Multiple choice:

- ✓ Educational and fun?
- ✓ Fun but not educational?
- ✓ Boring but educational?
- ✓ Boring and not educational?
- ✓ I had technical difficulties.

Hints:

- The answer is

7) Assistment #378227 "378227 - ASSISTments Instruction"

In the next step you are going to answer a series of questions on **ASSISTments**.

When you click the ASSISTments image, a new window will open and you will answer questions for at least five minutes, but you may continue as long as you want.

When you are done, you will enter your score and then continue.

What are you going to do on the next page?

Multiple choice:

MULTIPLE CHOICE.

- ✓ Click the ASSISTments link, use it for at least five minutes, then enter your score
- ✗ Go shopping
 - No, you are going to continue and play Wrecks Factor
- ✗ Write a poem
 - No, you are going to continue and play Wrecks Factor

Hints:

- The answer is

8) Assistment #377510 "377510 - ASSISTments Test Drive"

Please click on the picture below and answer questions for at least five minutes.



When you're done enter how many questions you answered below.

Ungraded open response:

✓ 52

9) Assistment #112668 "112668 - Multiplying Binomials"

If the directions are to apply the distributive property to multiply these binomials:

$$(7x-4)(2x-9)$$

Which option correctly multiplies the binomials?

$$\begin{aligned} \text{a. } (7x-4)(2x-9) &= (7x)(2x)-(7x)(9)-(4)(2x)+(4)(9) \\ &= 9x^2-16x-6x+13 \\ &= 9x^2-22x+13 \end{aligned}$$

$$\begin{aligned} \text{b. } (7x-4)(2x-9) &= (7x)(2x)-(7x)(9)+(4)(2x)-(4)(9) \\ &= 14x^2-63x+8x-36 \\ &= 14x^2+-55x-36 \end{aligned}$$

$$\begin{aligned} \text{c. } (7x-4)(2x-9) &= (7x)(2x)-(7x)(9)-(4)(2x)+(4)(9) \\ &= 72x^2-79x-42x+49 \\ &= 72x^2-121x+49 \end{aligned}$$

$$\text{d. } (7x-4)(2x-9) = (7x)(2x)-(7x)(9)-(4)(2x)+(4)(9)$$

$$= 14x^2 - 63x - 8x + 36$$

$$= 14x^2 - 71x + 36$$

Multiple choice:

a

b

c

d

10) Assistment #112780 "112780 - FOIL"

Simplify the equation:

$$(10x+1)(6x-6)$$

You need to enter your answer in the right format for the computer to grade it.

1. Use standard form, which means you put the highest power first.
2. Use the ^ to show exponents just like you do with a graphing calculator.
3. Do not put in any spaces.

For example: $6 + x^2 - 4x^3 - 2x$ is $-4x^3 + x^2 - 2x + 6$ in standard form and
 You would type in: $-4x^3+x^2-2x+6$

Fill in:

$60x^2+-54x-6$

$60x^2-54x-6$

Hints:

- Be sure to read the rules in orange carefully.

To solve the problem:

Think of each polynomial as one side of a rectangle.

$$6x \qquad \qquad \qquad + \qquad \qquad -6$$

10x

+

1

- Then calculate the area for each section of the rectangle.

$$6x \qquad + \qquad -6$$

$$10x \qquad (6x)(10x) \qquad (-6)(10x)$$

+

$$1 \qquad (6x)(1) \qquad (-6)(1)$$

- Then add each area together:
 $(6x)(10x)+(-6)(10x)+(6x)(1)+(-6)(1)$
 and then simplify:

$$60x^2+-54x-6$$

Type in: $60x^2+-54x-6$

11) Assistment #112799 "112799 - Multiplying Binomials"

If the directions are to apply the distributive property to multiply these binomials:

$$(4x+5)(6x-1)$$

Which option correctly multiplies the binomials?

$$\begin{aligned} \text{a. } (4x+5)(6x-1) &= (4x)(6x)-(4x)(1)+(5)(6x)-(5)(1) \\ &= 10x^2-5x+11x-6 \\ &= 10x^2+6x-6 \end{aligned}$$

$$\begin{aligned} \text{b. } (4x+5)(6x-1) &= (4x)(6x)-(4x)(1)+(5)(6x)+(5)(1) \\ &= 24x^2-4x+30x+5 \\ &= 24x^2+26x+5 \end{aligned}$$

$$\begin{aligned} \text{c. } (4x+5)(6x-1) &= (4x)(6x)-(4x)(1)+(5)(6x)-(5)(1) \\ &= 46x^2-41x+56x-51 \\ &= 46x^2+15x-51 \end{aligned}$$

$$\text{d. } (4x+5)(6x-1) = (4x)(6x)-(4x)(1)+(5)(6x)-(5)(1)$$

$$= 24x^2 - 4x + 30x - 5$$

$$= 24x^2 + 26x - 5$$

Multiple choice:

 a

 b

 c

 d

Problem Set "PhET Experiment" id:[95541]**1) Assistment #384094 "384094 - Finding h of Quadratics in Standard Form (Type 1)"**

Find the x coordinate, h , of the vertex of the graph of the following function:

$$f(x) = -5x^2 + 4x + 5$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 0.4

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

- To find the x coordinate of the vertex, h , use the formula:

$$h = \frac{-b}{2a}$$

•

$$\begin{aligned} h &= -(4)/(2(-5)) \\ &= -4/(2(-5)) \\ &= -4/-10 \\ &= 2/5 \end{aligned}$$

The answer is $2/5$.

2) Assistment #384153 "384153 - Finding k of Quadratics in Standard Form (Type 3a)"

Find the y coordinate of the vertex, k , of the following equation, given that the x part, h , is $5/6$.

$$f(x) = 3x^2 - 5x$$

If not a whole number, enter the answer as a fraction

If not a whole number, enter the answer as a fraction.

Algebra:

✓ -2.08333333333333

Hints:

- To find the y part of the vertex, **k**, calculate **f(h)**.

-

$$\begin{aligned}
 f(h) &= f(5/6) \\
 &= 3(5/6)^2 - 5(5/6) \\
 &= 3(25/36) - 5(5/6) \\
 &= 75/36 - 5(5/6) \\
 &= 75/36 - 25/6 \\
 &= 75/36 - 150/36 \\
 &= 75/36 - 150/36 \\
 &= -75/36 \\
 &= -25/12
 \end{aligned}$$

The answer is **-25/12**.

3) Assistment #384175 "384175 - Finding k of Quadratics in Standard Form (Type 1b)"

Find the y coordinate of the vertex, **k**, of the following equation.

$$f(x) = -4x^2 + 2x + 5$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 5.25

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

To find the y coordinate of the vertex, **k**, you need to evaluate **f(h)**.

To find the x coordinate of the vertex, **h**, use the formula:

$$h = \frac{-b}{2a}$$

-

$$\begin{aligned} h &= -(2)/(2(-4)) \\ &= -2/(2(-4)) \\ &= -2/-8 \\ &= 1/4 \end{aligned}$$

-

$$\begin{aligned} f(h) &= f(1/4) \\ &= -4(1/4)^2 + 2(1/4) + 5 \\ &= -4(1/16) + 2(1/4) + 5 \\ &= -4/16 + 2(1/4) + 5 \\ &= -4/16 + 2/4 + 5 \\ &= -4/16 + 8/16 + 5 \\ &= -4/16 + 8/16 + 80/16 \\ &= 84/16 \\ &= 21/4 \end{aligned}$$

The answer is $21/4$.

4) Assistment #415871 "415871 - In this next acti..."

In this next activity you will learn about the properties of parabolas and how to find the coordinates of a parabola's vertex.

You will then practice and answer questions related to these skills.

Finally, you will be given a brief quiz.

Note: You will see in the corner of your that there are 43 items you need to do. Due to the creation of this problem set that number is to large. You will do fewer than 30 items.

Multiple choice:

✓ Ok

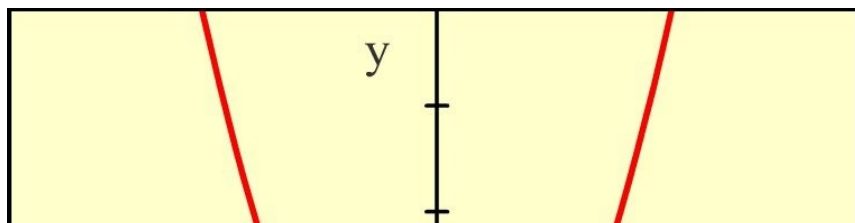
Hints:

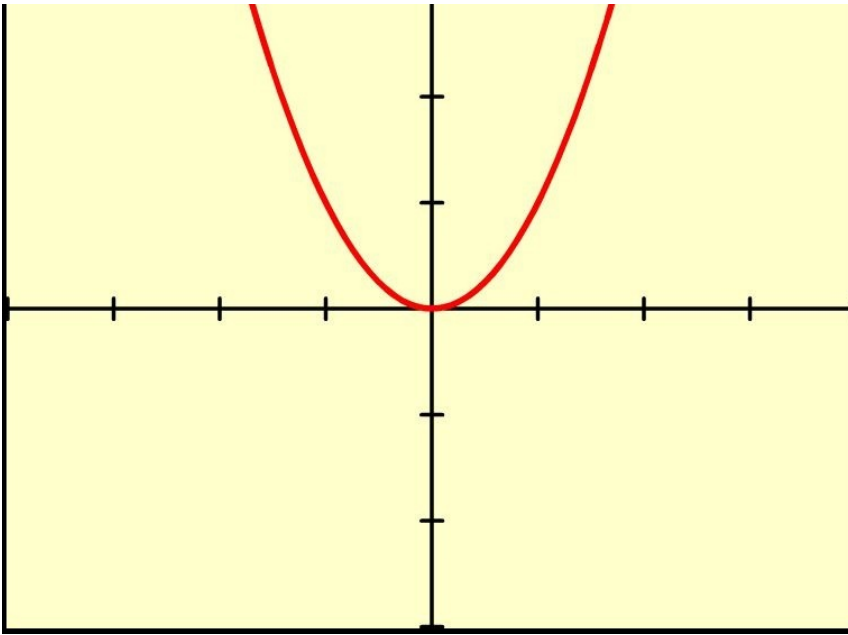
- The answer is Ok.

5) Assistment #372359 "372359 - Quadratic equatio..."

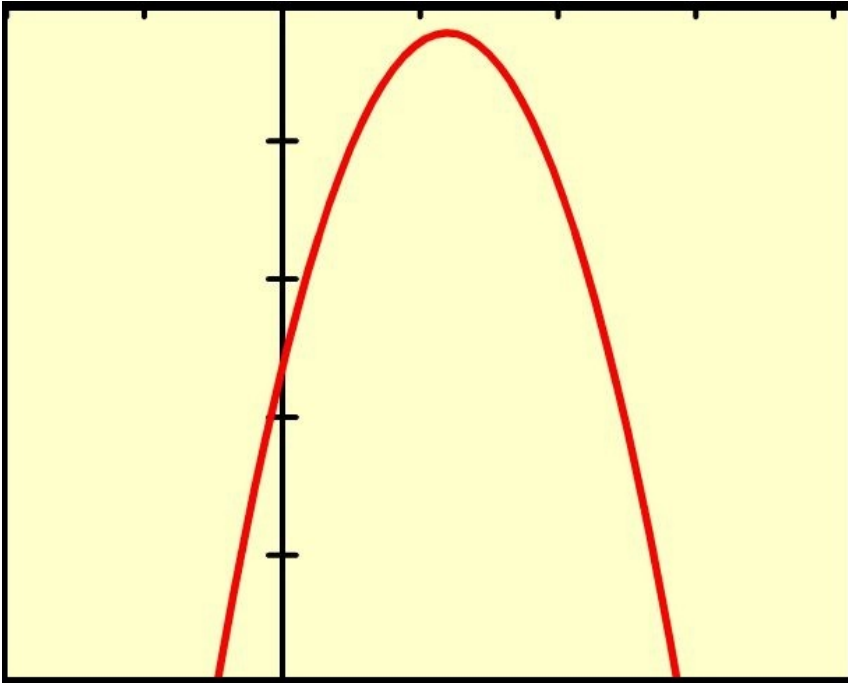
Quadratic equations are written in the form $f(x) = ax^2 + bx + c$

When a quadratic equation is graphed it is referred to as a **parabola**. A parabola looks like this:





Or like this:



Parabolas can also be wider or thinner than this and be located anywhere on a coordinate system.

For a function to be quadratic and to be graphed as a parabola, a must be a number other than zero. A parabola can be graphed from $f(x) = 4x^2 + 8x - 6$ just as easily as it can be graphed from $f(x) = x^2$.

Which of these is a parabola?

Remember, a parabola is written in the form $f(x) = ax^2 + bx + c$

Multiple choice:

$f(x) = x^3 + 5$

- A quadratic equation must be in the form $f(x) = ax^2 + bx + c$.

✓ $f(x) = x^2 + 3x - 5$

✗ $f(x) = 7$

- A quadratic equation must be in the form $f(x) = ax^2 + bx + c$.

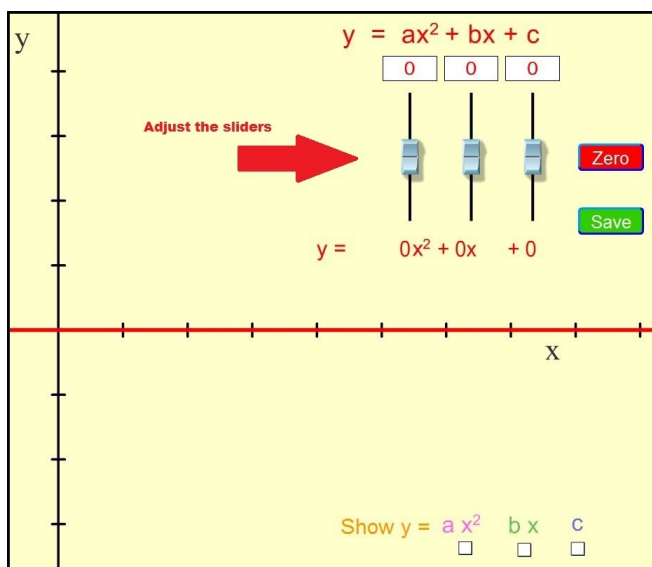
✗ $f(x) = 6x$

- A quadratic equation must be in the form $f(x) = ax^2 + bx + c$.

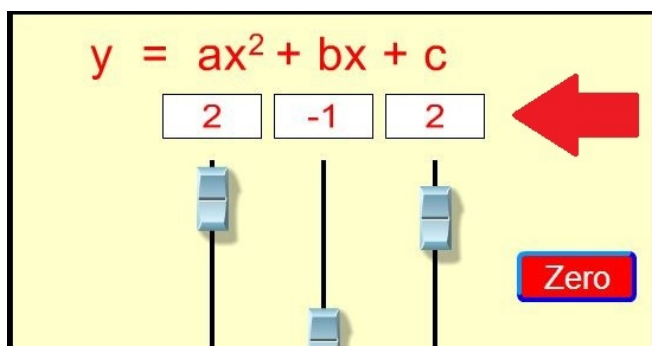
Hints:

6) Assistment #375724 "375724 - Use the equation ..."

In the following steps you will be using the "equation grapher" to graph different parabolas. To graph a parabola you move the sliders up and down. Each slider affects a different value (from right to left: a, b, and c).



If you want to be more precise you can click on the numbers above the sliders and replace them with exact values. Remember-- if you see "x" with no number in front of it the coefficient is 1 and that's what you should enter into the equation grapher.



$$y = 2x^2 - 1x + 2$$

Save

Lets now graph the parabolla $f(x) = 2x^2 - x + 2$

Enter the numbers above into the equation grapher below:

About...

y

$$y = ax^2 + bx + c$$

0 0 0

Zero

Save

$$y = 0x^2 + 0x + 0$$

X

Show $y = a x^2 + b x + c$

PhET

Does your parabola (with the values from above) open up or down?

Multiple choice:

✓ Up

✗ Down

- Check the equation grapher again. Make you entered a positive value for a.

Hints:

- The answer is

7) Assistent #375735 "375735 - This time, enter ..."

$y = ax^2 + bx + c$
 $y = 0x^2 + 0x + 0$

About...
 Zero
 Save
 Show $y = a x^2 + b x + c$
 PhET

This time, enter a negative value for **a**. Does the parabola open up or down?

Multiple choice:

Up

- Make sure you entered a negative value for **a**.

Down

Hints:

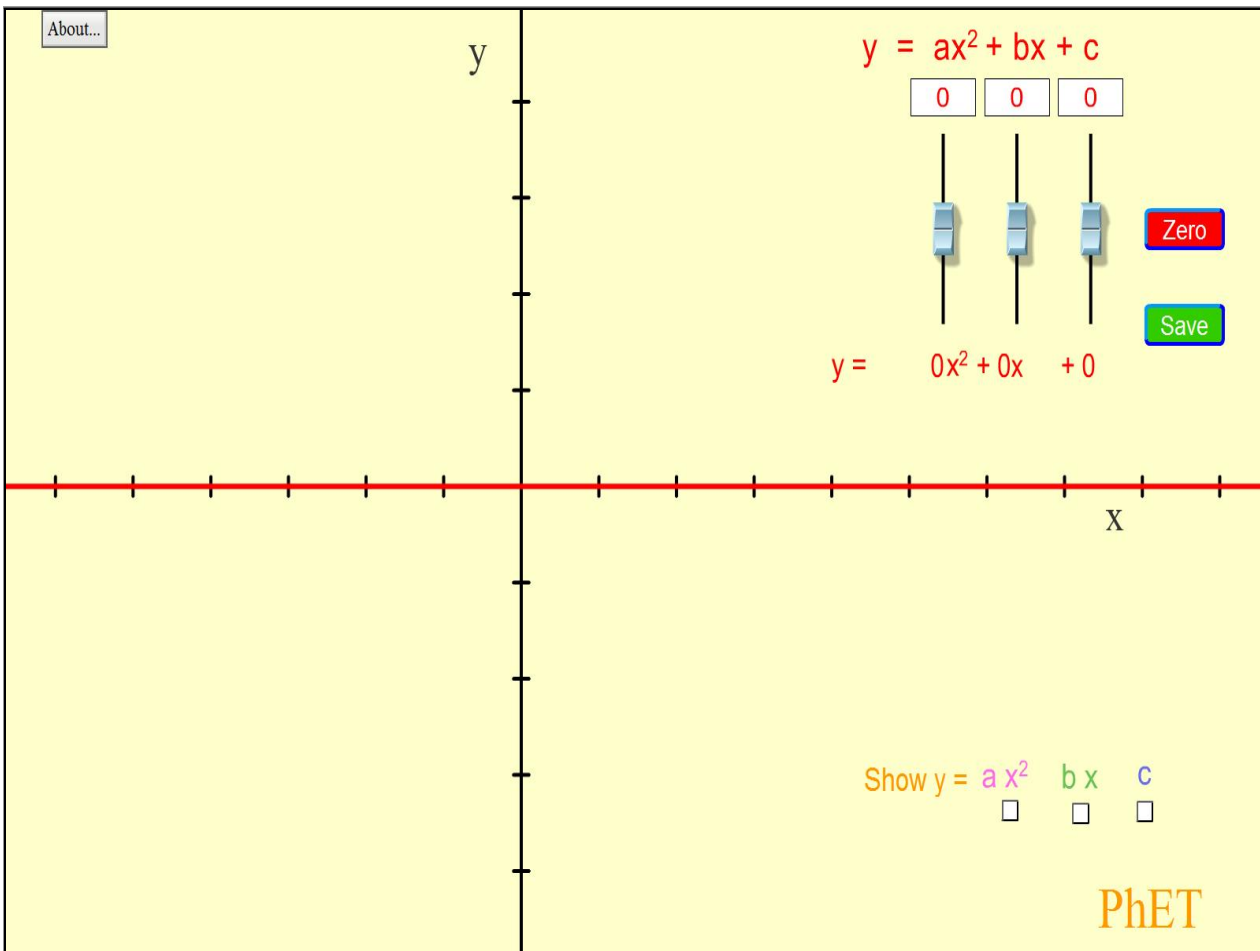
- The answer is

8) Assistment #375736 "375736 - Enter the value 1..."

Scroll down to the equation grapher and enter the value **1** for **a**. Click the **Save** button. Your parabola should turn blue.

The image shows a digital interface for graphing a parabola. At the top, the equation $y = ax^2 + bx + c$ is displayed. Below this, three input boxes contain the values 1, 0, and 0. Underneath these boxes are three vertical sliders. The first slider is set to 1, the second to 0, and the third to 0. To the right of the sliders are two buttons: a red 'Zero' button and a green 'Save' button. Below the sliders, the equation $y = 1x^2 + 0x + 0$ is displayed. At the bottom, there is a coordinate plane with an x-axis labeled 'X'. A large red arrow points upwards from the x-axis towards the 'Save' button.

Enter the value **.1** for **a**. You should see two parabolas. Which one is wider, the **red** one ($a = .1$) or the **blue** one ($a = 1$)?

**Multiple choice:**

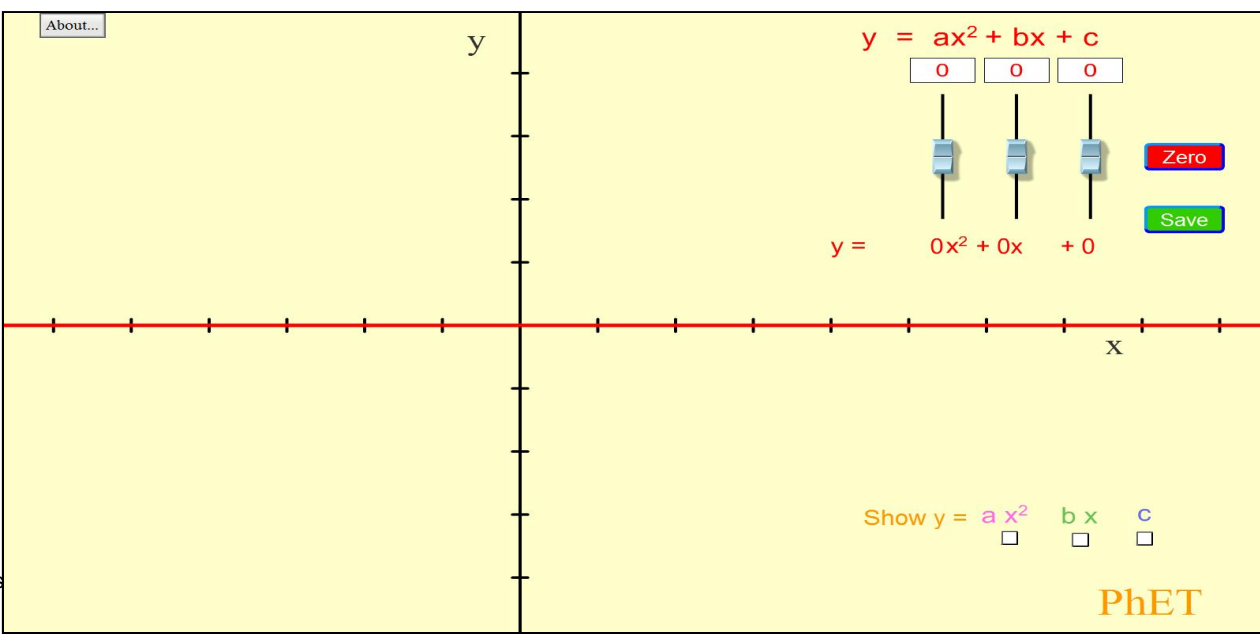
✓ Red (a = .1)

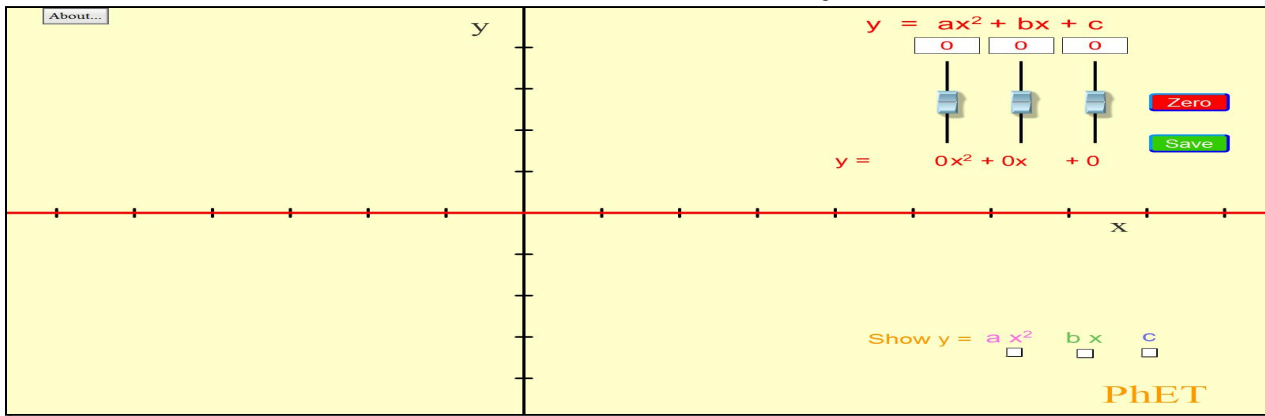
✗ Blue (a = 1)

Hints:

- The answer is

9) Assistent #375740 "375740 - Enter the value -..."





Enter the value **-1** for **a**. Click the **Save** button. Enter the value **-1** for **a**. Which parabola is wider, the **red one** ($a = -1$) or the **blue one** ($a = -1$)?

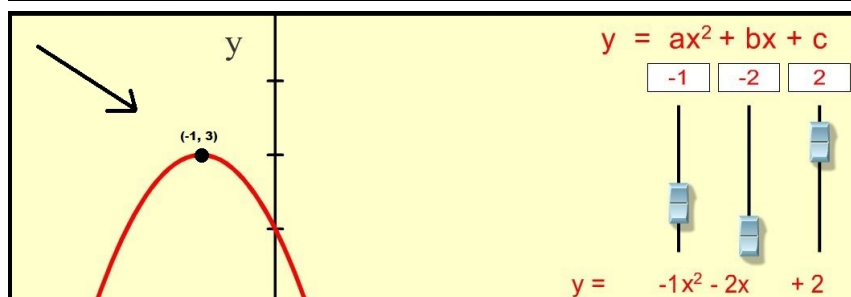
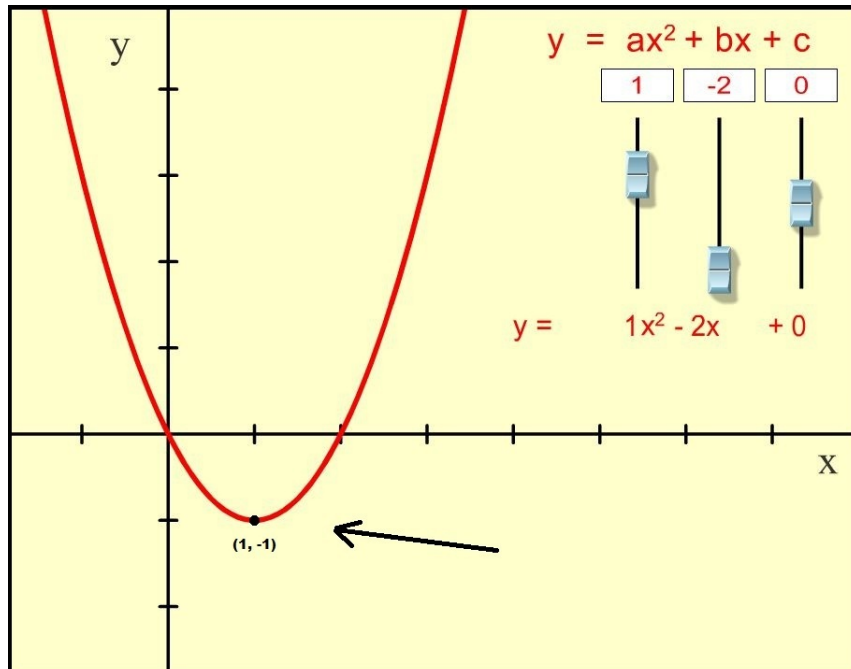
Multiple choice:

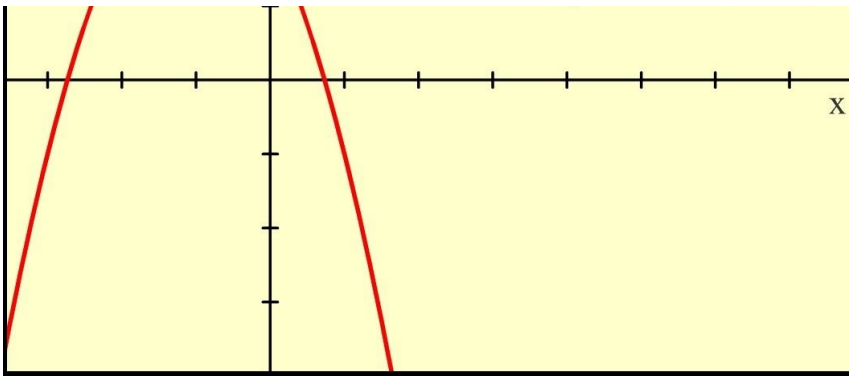
- ✓ Red one ($a = -1$)
- ✗ Blue one ($a = -1$)

Hints:

10) Assistent #372360 "372360 - Every parabola be..."

Every parabola begins at its **vertex**. The vertex of a parabola is its lowest or highest point.





Enter a positive value for a in the equation grapher. Is the vertex the parabola's highest or lowest point?

About...
y

$$y = ax^2 + bx + c$$

Zero

Save

$$y = 0x^2 + 0x + 0$$

$$\text{Show } y = a x^2 \quad b x \quad c$$

PhET

x

Multiple choice:

- Lowest point

✓ Lowest point

✗ Highest point

- Did you enter a positive value for a?

Hints:

- The answer is

11) Assistent #375741 "375741 - Enter a negative ..."

This time enter a negative value for a. Is the vertex the parabola's highest or lowest point?

About...

$y = ax^2 + bx + c$

0 0 0

Zero

Save

$y = 0x^2 + 0x + 0$

X

Show $y = a x^2$ $b x$ c

PhET

Multiple choice:

✓ Highest point

✗ Lowest point

- Did you enter a negative value for a?

a:

Hints:

- The answer is

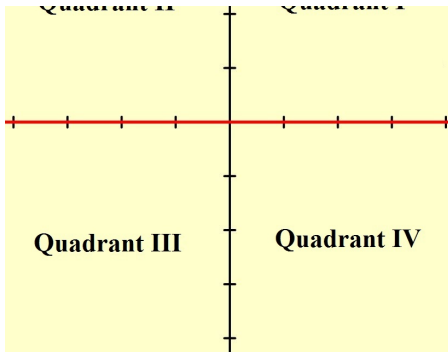
12) Assistent #382248 "382248 - Quadrant1"

Graph the equation $f(x) = x^2 + 2x$ in the equation grapher below:

Which quadrant does the vertex lie in?

Remember:



**Multiple choice:**

- Quadrant I
 - Click on the hint
- Quadrant II
 - Click on the hint
- Quadrant III
- Quadrant IV
 - Click on the hint

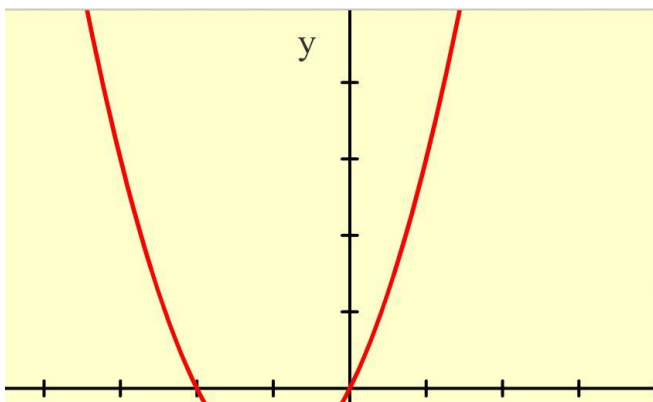
Hints:

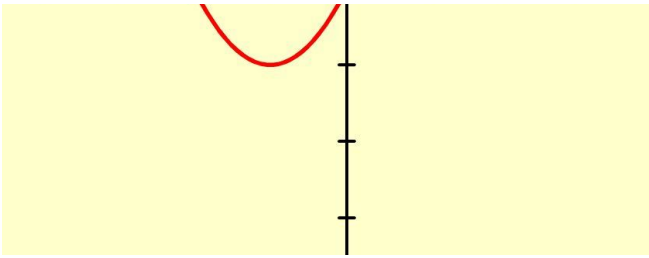
$y = ax^2 + bx + c$

1 2 0

$y = 1x^2 + 2x + 0$

Enter the numbers above into the equation grapher ($a = 1$, $b = 2$, $c = 0$)





Your parabola should look like this.

13) Assistent #382249 "382249 - Quadrant2"

Graph the equation $f(x) = .5x^2 - x + 2$ in the equation grapher below:

About...
y

$y = ax^2 + bx + c$

Zero

Save

$y = 0x^2 + 0x + 0$

X

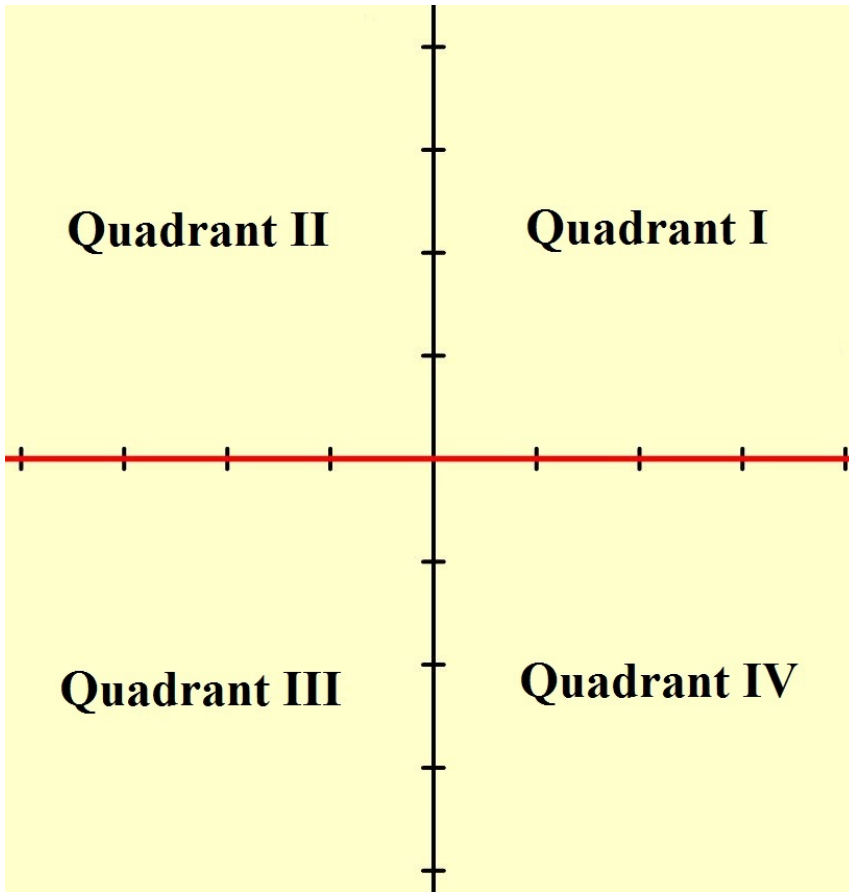
Show $y = a x^2 + b x + c$

a x^2
 b x
 c

PhET

Which quadrant does the vertex lie in?

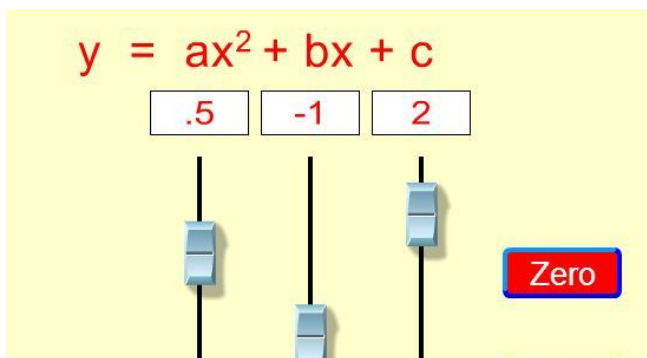
Remember:



Multiple choice:

- Quadrant I
- Quadrant II
- Quadrant III
- Quadrant IV

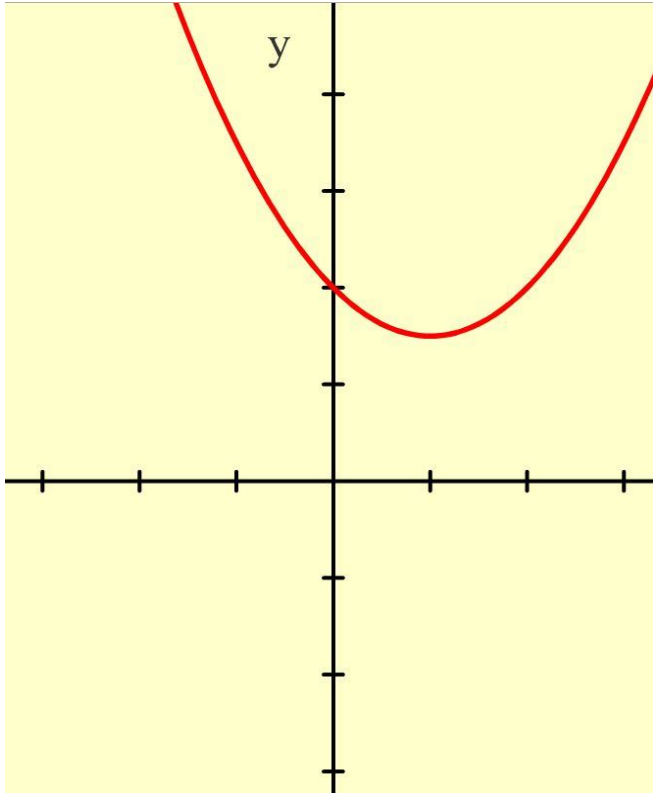
Hints:



Save

$$y = 0.5x^2 - 1x + 2$$

Enter the numbers above into the equation grapher (a = .5, b = -1, c = 2)



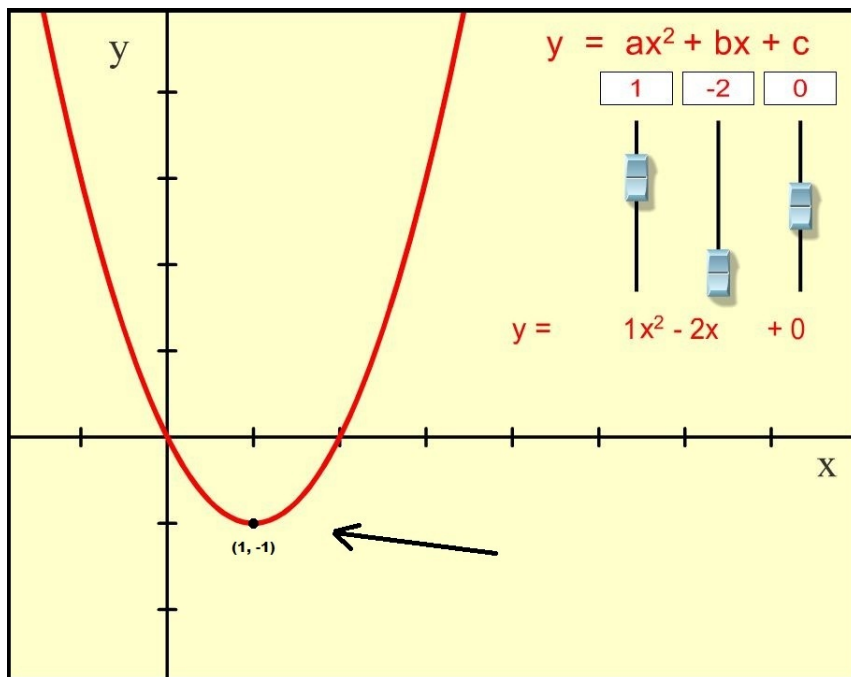
Your parabola should look like this.

14) Assistment #372361 "372361 - x value phet"

A) Now let's practice calculating the vertex.

The x value of a parabola's vertex is given by the equation $h = -b/2a$ where the vertex is written (h, k) .

In the image below h is 1 and k is -1, with the vertex lying at (1, -1).



The solution method for finding h is shown below:

Find h in the quadratic equation $f(x) = x^2 - 2x$.

$$a = 1$$

$$b = -2$$

$$-b/2a = -(-2)/2(1)$$

$$= 2/2$$

$$= 1$$

$$h = 1$$

Multiple choice:

✓ OK

Hints:

- The answer is

B) The y value of a parabola's vertex is given by $f(h)$ where the vertex is given by (h, k) . In other words, the y value (k) of a parabola's vertex is equal to $a(h)^2 + b(h) + c$.

The solution method for finding k is shown below.

In the previous example (above), we found that h was equal to 1. The equation is $f(x) = x^2 - 2x$.

$$f(h) = a(h)^2 + b(h) + c$$

$$f(1) = (1)^2 - 2(1) + 0$$

$$= 1 - 2$$

$$= -1$$

$$k = -1$$

Multiple choice:

✓ OK

15) Assistent #375818 "375818 - Find the vertex o..."

A) Find the vertex of the graph of $f(x) = -2x^2 + 4x$.

Use the equation grapher to estimate your answer.

Equation Grapher interface showing the equation $y = ax^2 + bx + c$ and its current values: $y = 0x^2 + 0x + 0$. The interface includes a coordinate plane, sliders for coefficients, and buttons for 'Zero' and 'Save'.

Take the time to learn the formulas. Later, there will be no equation grapher.

Multiple choice:

✓ I have a good idea of where the vertex will be.

Hints:

•

$y = ax^2 + bx + c$

-2 4 0

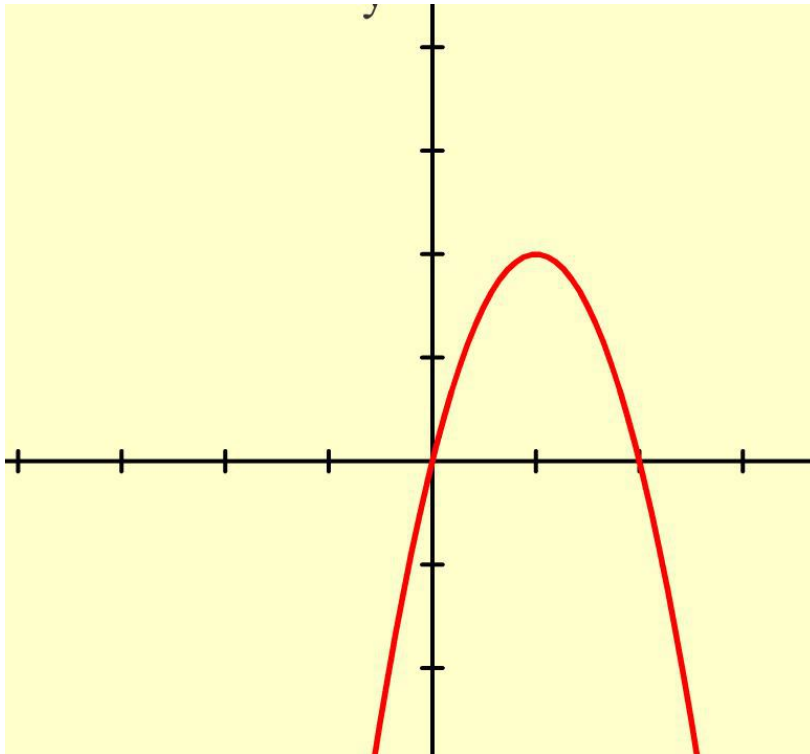
Zero

Save

$y = -2x^2 + 4x + 0$

Enter these values for a and b.

•



Your parabola should look like this.

B) Now solve the equation and find h and k.

Remember, the equation is $f(x) = -2x^2 + 4x$.

$$h = -b/2a$$

$$k = f(h)$$

Answer in the form (h,k) with no spaces.

Fill in:

✓ (1,2)

Hints:

- $a = -2$
 $b = 4$

$$h = -4/2(-2)$$
$$h = 1$$

$$k = -2(1)^2 + 4(1)$$
$$k = 2$$

The answer is (1,2)

16) Assistment #375819 "375819 - Find the vertex o..."

A) Find the vertex of the graph of $f(x) = x^2 - 2x - 3$.

Use the equation grapher to estimate your answer.

$y = ax^2 + bx + c$
 $y = 0x^2 + 0x + 0$
 Show $y = a x^2 + b x + c$
 PhET

Multiple choice:

✓ OK

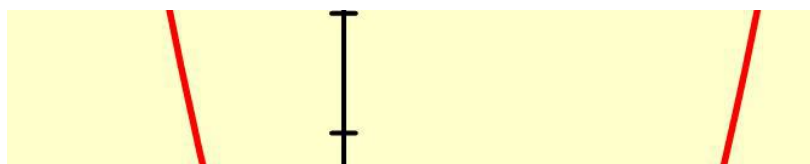
Hints:

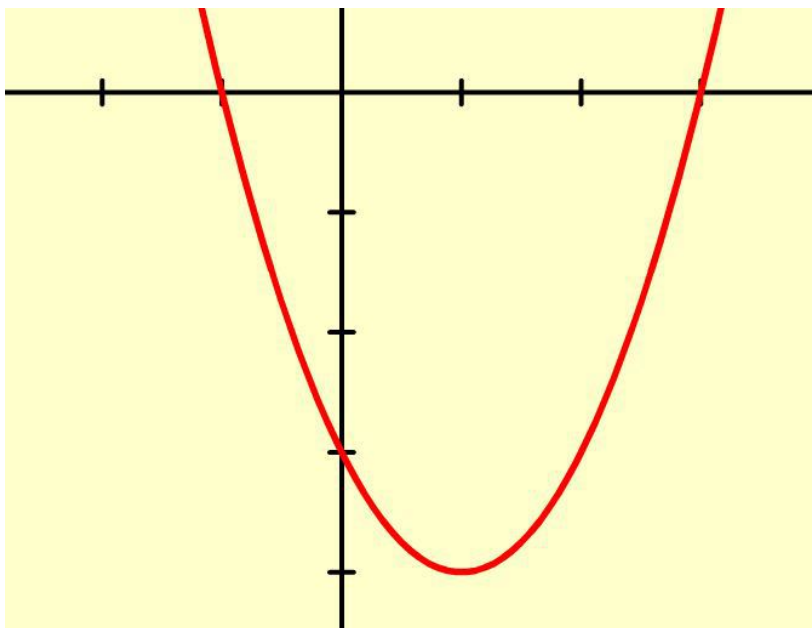
•

$y = ax^2 + bx + c$
 $y = 1x^2 - 2x - 3$

Enter these value for a, b, and c.

•





Your parabola should look like this.

B) Now solve the equation and find h and k .

Remember, the equation is $f(x) = x^2 - 2x - 3$.

$$h = -b/2a$$

$$k = f(h)$$

Answer in the form (h,k) with no spaces.

Fill in:

✓ (1,-4)

Hints:

- $a = 1$
- $b = -2$

$$h = 2/2(1)$$

$$h = 1$$

$$k = (1)^2 - 2(1) - 3$$

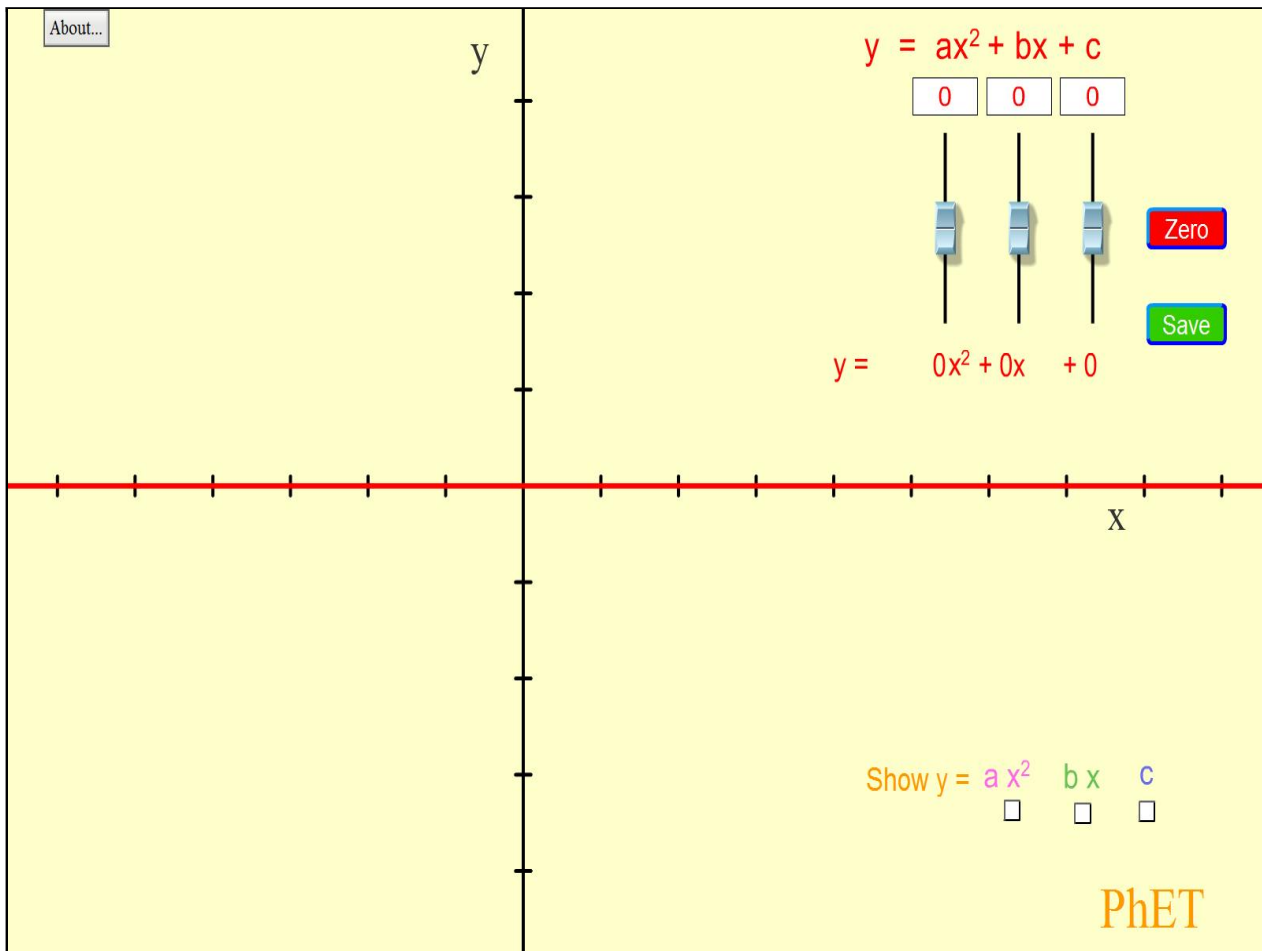
$$k = -4$$

The answer is (1,-4)

17) Assistment #375820 "375820 - Find the vertex o..."

A) Find the vertex of the graph of $f(x) = -5x^2 + 10x + 2$.

Use the equation grapher to estimate your answer.

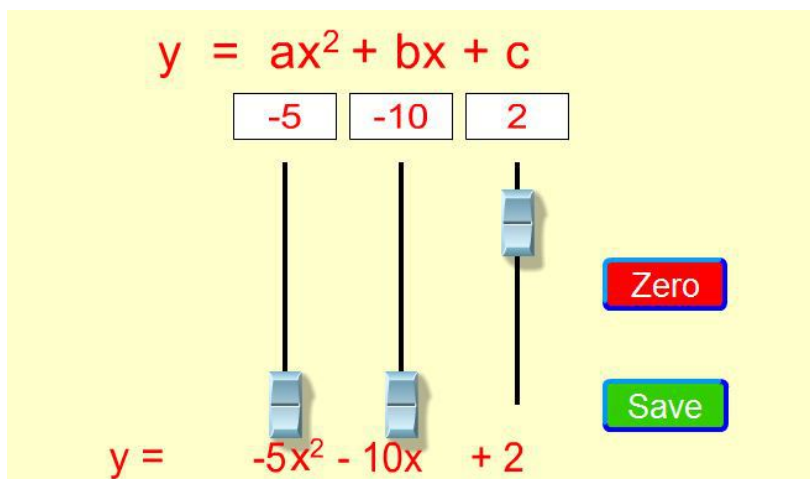


Multiple choice:

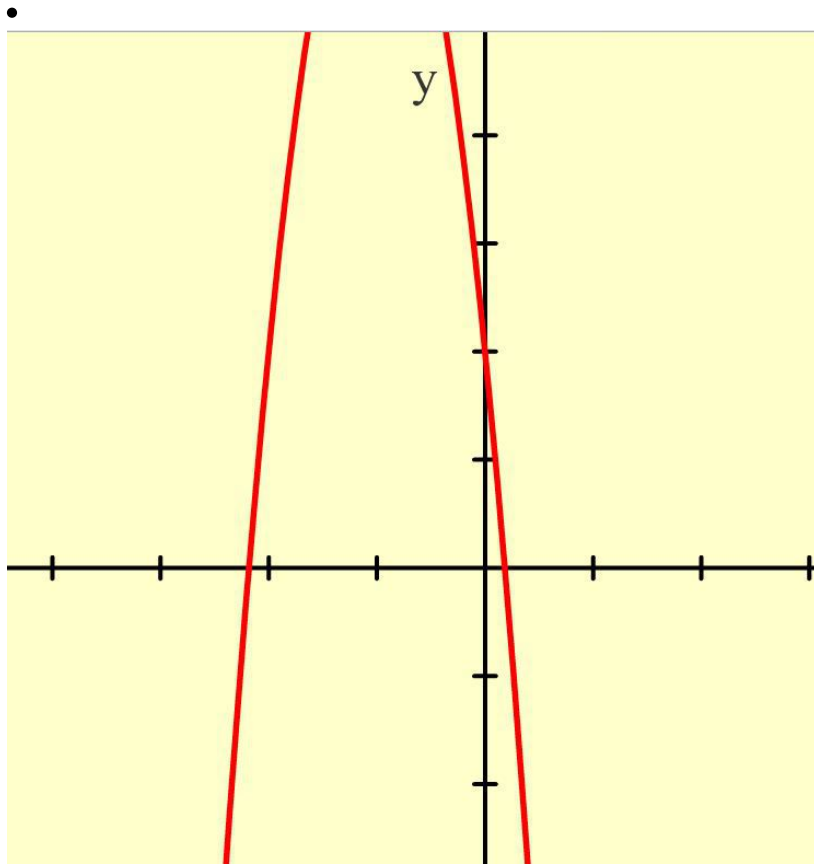
✓ OK

Hints:

•



Enter these values for a, b, and c.



Your parabola should look like this.

B) Now solve the equation and find h and k.

Remember, the equation is $f(x) = -5x^2 + 10x + 2$.

$$h = -b/2a$$

$$k = f(h)$$

Answer in the form (h,k) with no spaces.

Fill in:

✓ (1,7)

Hints:

- $a = -5$

$$b = 10$$

$$h = -10/2(-5)$$

$$h = 1$$

$$k = -5(1)^2 + 10(1) + 2$$

$$k = 7$$

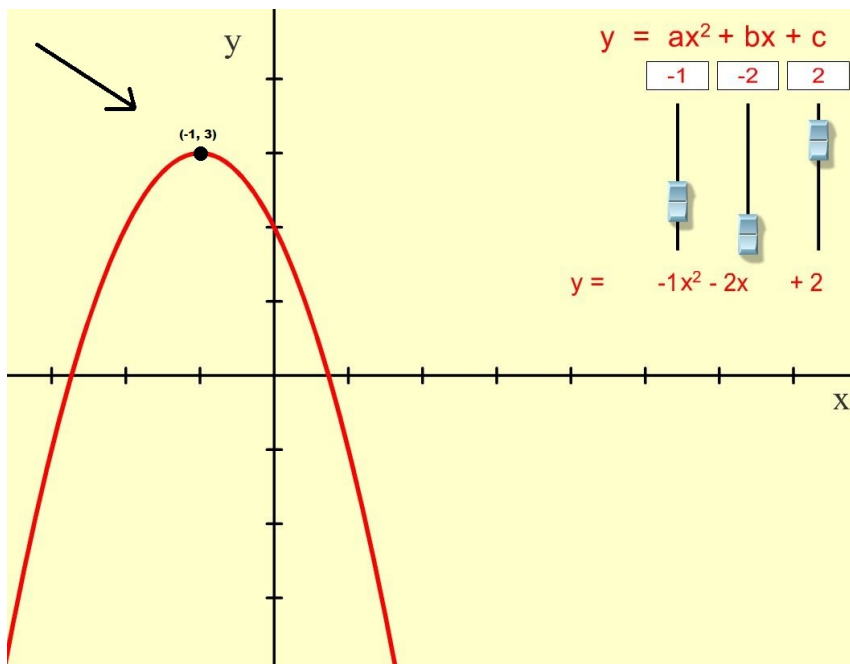
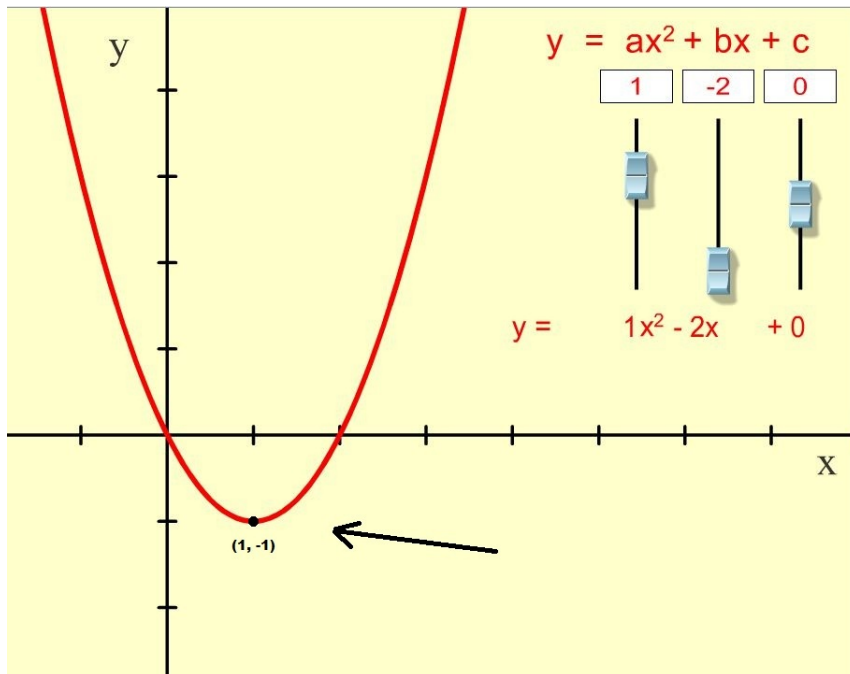
The answer is (1,7)

18) Duplicate assistment: Assistment #415871 "415871 - In this next acti..." was not displayed.

19) Duplicate assistment: Assistment #372359 "372359 - Quadratic equatio..." was not displayed.

20) Assistment #377892 "377892 - 2"

Every parabola begins at its **vertex**. The vertex of a parabola is its lowest or highest point.



When a parabola opens **up (a is positive)** the **vertex is its lowest** point.

When a parabola opens **down (a is negative)** the **vertex is its highest** point.

Is the vertex the highest or lowest point in $f(x) = 16x^2 - 5x + 8$?

Multiple choice:

Highest

- Note: $a=16$ and it is positive. Read about what happens when a is positive

Lowest

Hints:

- Remember, $a = 16$ (positive).

21) Assistment #377893 "377893 - 3"

Is the vertex the highest or lowest point in $f(x) = -x^2 - 3$?

Multiple choice:

Highest

Lowest

- Remember, a parabola with a negative a value opens downwards.

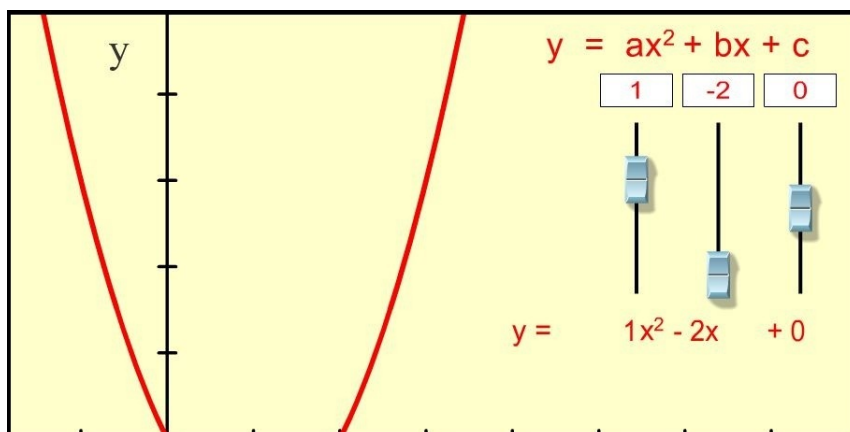
Hints:

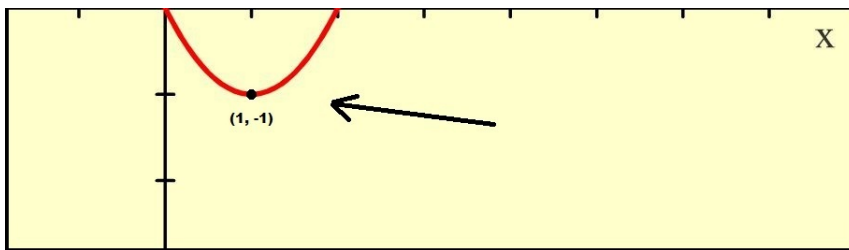
- Remember $a = -1$ (negative).

22) Assistment #377994 "377994 - 4"

A) The x value of a parabola's vertex is given by the equation $h = -b/2a$ where the vertex is written (h, k) .

In the image below h is 1 and k is -1, with the vertex lying at $(1, -1)$.





The solution method for finding h is shown below:

Find h in the quadratic equation $f(x) = x^2 - 2x$.

$$a = 1$$

$$b = -2$$

$$\begin{aligned} -b/2a &= -(-2)/2(1) \\ &= 2/2 \\ &= 1 \end{aligned}$$

$$h = 1$$

Multiple choice:

✓ OK

Hints:

- The answer is

B) The y value of a parabola's vertex is given by $f(h)$ where the vertex is given by (h, k) . In other words, the y value (k) of a parabola's vertex is equal to $a(h)^2 + b(h) + c$.

The solution method for finding k is shown below.

In the previous example (above), we found that h was equal to 1. The equation is $f(x) = x^2 - 2x$.

$$f(h) = a(h)^2 + b(h) + c$$

$$f(1) = (1)^2 - 2(1) + 0$$

$$= 1 - 2$$

$$= -1$$

$$k = -1$$

Multiple choice:

✓ OK

23) Assistment #377996 "377996 - 6"

Find the vertex of the graph of $f(x) = -2x^2 + 4x$.

Answer in the form (h,k) with no spaces.

Fill in:

✓ (1,2)

Hints:

- $h = -$

$$b/2a$$

$$k = f(h)$$

- $a = -2$

$$b = 4$$

$$h = -4/2(-2)$$

$$h = 1$$

$$k = -2(1)^2 + 4(1)$$

$$k = 2$$

The answer is (1,2)

24) Assistment #377997 "377997 - 7"

Find the vertex of the graph of $f(x) = x^2 - 2x - 3$.

Answer in the form (h,k) with no spaces.

Fill in:

✓ (1,-4)

Hints:

- $h = -$

$$b/2a$$

$$k = f(h)$$

- $a = 1$

$$b = -2$$

$$h = 2/2(1)$$

$$h = 1$$

$$k = (1)^2 - 2(1) - 3$$

$$k = -4$$

The answer is (1,-4)

25) Assistment #377998 "377998 - 8"

Find the vertex of the graph of $f(x) = -5x^2 + 10x + 2$.

Answer in the form (h,k) with no spaces.

Fill in:

✓ (1,7)

Hints:

- $h = -$

$$b/2a$$

$$k = f(h)$$

- $a = -5$

$$b = 10$$

$$h = -10/2(-5)$$

$$h = 1$$

$$k = -5(1)^2 + 10(1) + 2$$

$$k = 7$$

The answer is (1,7)

26) Assistment #384102 "384102 - Finding h of Quadratics in Standard Form (Type 1)"

Find the x coordinate, **h**, of the vertex of the graph of the following function:

$$f(x) = -3x^2 + x - 2$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 0.166666666666667

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

- To find the x coordinate of the vertex, **h**, use the formula:

$$-b$$

$$h = \frac{-b}{2a}$$

$$2a$$

-

$$\begin{aligned} \mathbf{h} &= -(1)/(2(-3)) \\ &= -1/(2(-3)) \\ &= -1/-6 \end{aligned}$$

The answer is $1/6$.

27) Assistment #384161 "384161 - Finding k of Quadratics in Standard Form (Type 3a)"

Find the y coordinate of the vertex, k , of the following equation, given that the x part, h , is $1/4$.

$$f(x) = 4x^2 - 2x$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ -0.25

Hints:

- To find the y part of the vertex, k , calculate $f(h)$.

-

$$\begin{aligned} f(h) &= f(1/4) \\ &= 4(1/4)^2 - 2(1/4) \\ &= 4(1/16) - 2(1/4) \\ &= 4/16 - 2(1/4) \\ &= 4/16 - 2/4 \\ &= 4/16 - 8/16 \\ &= 4/16 - 8/16 \\ &= -4/16 \\ &= -1/4 \end{aligned}$$

The answer is $-1/4$.

28) Assistment #384141 "384141 - Finding k of Quadratics in Standard Form (Type 1a)"

Find the y coordinate of the vertex of the following equation.

Given that the x coordinate or h , is $-1/5$.

$$f(x) = 5x^2 + 2x + 2$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 1.8

Hints:

- Calculate $f(h)$.

$$f(h) = f(-1/5)$$

•

$$f(h) = f(-1/5)$$

$$= 5(-1/5)^2 + 2(-1/5) + 2$$

$$= 5(1/25) + 2(-1/5) + 2$$

$$= 5/25 + 2(-1/5) + 2$$

$$= 5/25 - 2/5 + 2$$

$$= 5/25 - 10/25 + 2$$

$$= 5/25 - 10/25 + 50/25$$

$$= 45/25$$

$$= 9/5$$

The answer is $9/5$.

29) Assistment #384179 "384179 - Finding k of Quadratics in Standard Form (Type 1b)"

Find the y coordinate of the vertex, k , of the following equation.

$$f(x) = 3x^2 - 4x + 5$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 3.66666666666667

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

To find the y coordinate of the vertex, k, you need to evaluate $f(h)$.

To find the x coordinate of the vertex, h, use the formula:

$$h = \frac{-b}{2a}$$

•

$$\begin{aligned} h &= -(-4)/(2(3)) \\ &= 4/(2(3)) \\ &= 4/6 \\ &= 2/3 \end{aligned}$$

•

$$\begin{aligned} f(h) &= f(2/3) \\ &= 3(2/3)^2 - 4(2/3) + 5 \\ &= 3(4/9) - 4(2/3) + 5 \\ &= 12/9 - 4(2/3) + 5 \\ &= 12/9 - 8/3 + 5 \\ &= 12/9 - 24/9 + 5 \\ &= 12/9 - 24/9 + 45/9 \\ &= 33/9 \\ &= 11/3 \end{aligned}$$

The answer is $11/3$.

30) Assistment #384152 "384152 - Finding k of Quadratics in Standard Form (Type 2a)"

Find the y coordinate of the vertex, k, of the following equation, given that the x part, h, is 0.

$$f(x) = -4x^2 + 5$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 5

Hints:

- To find the y part of the vertex, k, calculate $f(h)$.
-

$$\begin{aligned}
 f(h) &= f(0) \\
 &= -4(0)^2 + 5 \\
 &= 5
 \end{aligned}$$

The answer is 5.

31) Assistment #384178 "384178 - Finding k of Quadratics in Standard Form (Type 1b)"

Find the y coordinate of the vertex, k, of the following equation.

$$f(x) = x^2 + 3x + 2$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ -0.25

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

To find the y coordinate of the vertex, k, you need to evaluate **f(h)**.

To find the x coordinate of the vertex, **h**, use the formula:

$$h = \frac{-b}{2a}$$

•

$$\begin{aligned}
 h &= -(3)/(2(1)) \\
 &= -3/(2(1)) \\
 &= -3/2
 \end{aligned}$$

•

$$\begin{aligned}
 f(h) &= f(-3/2) \\
 &= 1(-3/2)^2 + 3(-3/2) + 2 \\
 &= 1(9/4) + 3(-3/2) + 2 \\
 &= 9/4 + 3(-3/2) + 2 \\
 &= 9/4 - 9/2 + 2 \\
 &= 9/4 - 18/4 + 2
 \end{aligned}$$

$$= 9/4 - 18/4 + 8/4$$

$$= -1/4$$

$$= -1/4$$

The answer is $-1/4$.

32) Assistment #384112 "384112 - Finding h of Quadratics in Standard Form (Type 2)"

Find the **x** coordinate, **h**, of the vertex of the graph of the following function:

$$f(x) = -2x^2 - 4$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 0

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

- To find the **x** coordinate of the vertex, **h**, use the formula:

$$h = \frac{-b}{2a}$$

-

$$\begin{aligned} h &= -(0)/(2(-2)) \\ &= 0/(2(-2)) \\ &= 0/-4 \\ &= 0 \end{aligned}$$

The answer is **0**.

33) Assistment #384132 "384132 - Finding h of Quadratics in Standard Form (Type 4)"

Find the **x** coordinate, **h**, of the vertex of the graph of the following function:

$$f(x) = 5x^2$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 0

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

- To find the x coordinate of the vertex, **h**, use the formula:

$$h = \frac{-b}{2a}$$

-

$$\begin{aligned} h &= -(0)/(2(5)) \\ &= 0/(2(5)) \\ &= 0/10 \\ &= 0 \end{aligned}$$

The answer is **0**.

34) Assistment #384189 "384189 - Finding k of Quadratics in Standard Form (Type 2b)"

Find the y coordinate of the vertex, **k**, of the following equation.

$$f(x) = x^2 + 5$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 5

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

To find the y coordinate of the vertex, k , you need to evaluate $f(h)$.

To find the x coordinate of the vertex, h , use the formula:

$$h = \frac{-b}{2a}$$

•

$$\begin{aligned} h &= -(0)/(2(1)) \\ &= 0/(2(1)) \\ &= 0/2 \\ &= 0 \end{aligned}$$

•

$$\begin{aligned} f(h) &= f(0) \\ &= 1(0)^2 + 5 \\ &= 5 \end{aligned}$$

The answer is 5.

35) Assistment #384101 "384101 - Finding h of Quadratics in Standard Form (Type 1)"

Find the x coordinate, h , of the vertex of the graph of the following function:

$$f(x) = -3x^2 - 5x + 3$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ -0.8333333333333333

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

- To find the x coordinate of the vertex, h , use the formula:

$$h = \frac{-b}{2a}$$

2a

•

$$\begin{aligned} h &= -(-5)/(2(-3)) \\ &= 5/(2(-3)) \\ &= 5/-6 \end{aligned}$$

The answer is $-5/6$.

36) Assistment #384162 "384162 - Finding k of Quadratics in Standard Form (Type 3a)"

Find the y coordinate of the vertex, **k**, of the following equation, given that the x part, **h**, is $3/4$.

$$f(x) = -2x^2 + 3x$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 1.125

Hints:

- To find the y part of the vertex, **k**, calculate **f(h)**.

•

$$\begin{aligned} f(h) &= f(3/4) \\ &= -2(3/4)^2 + 3(3/4) \\ &= -2(9/16) + 3(3/4) \\ &= -18/16 + 3(3/4) \\ &= -18/16 + 9/4 \\ &= -18/16 + 36/16 \\ &= -18/16 + 36/16 \\ &= 18/16 \\ &= 9/8 \end{aligned}$$

The answer is $9/8$.

37) Assistment #384198 "384198 - Finding k of Quadratics in Standard Form (Type 3b)"

Find the y coordinate of the vertex, **k**, of the following equation.

$$f(x) = 3x^2 - 3x$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ -0.75

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

To find the **y** coordinate of the vertex, **k**, you need to evaluate **f(h)**.

To find the **x** coordinate of the vertex, **h**, use the formula:

$$h = \frac{-b}{2a}$$

•

$$\begin{aligned} h &= -(-3)/(2(3)) \\ &= 3/(2(3)) \\ &= 3/6 \\ &= 1/2 \end{aligned}$$

•

$$\begin{aligned} f(h) &= f(1/2) \\ &= 3(1/2)^2 - 3(1/2) \\ &= 3(1/4) - 3(1/2) \\ &= 3/4 - 3(1/2) \\ &= 3/4 - 3/2 \\ &= 3/4 - 6/4 \\ &= 3/4 - 6/4 \\ &= -3/4 \\ &= -3/4 \end{aligned}$$

The answer is **-3/4**.

38) Assistment #384142 "384142 - Finding k of Quadratics in Standard Form (Type 1a)"

Find the **y** coordinate of the vertex of the following equation.

Given that the **x** coordinate or **h**, is **2**.

$$f(x) = -x^2 + 4x - 4$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 0

Hints:

- Calculate $f(h)$.

$$f(h) = f(2)$$

•

$$f(h) = f(2)$$

$$= -1(2)^2 + 4(2) - 4$$

$$= -1(4) + 4(2) - 4$$

$$= -4 + 4(2) - 4$$

$$= -4 + 8 - 4$$

$$= -4 + 8 - 4$$

$$= -4 + 8 - 4$$

$$= 0$$

$$= 0$$

The answer is 0.

39) Assistment #384210 "384210 - Finding k of Quadratics in Standard Form (Type 4b)"

Find the y coordinate of the vertex, k, of the following equation.

$$f(x) = 4x^2$$

If not a whole number, enter the answer as a fraction.

Algebra:

✓ 0

Hints:

- This equation is in **standard form**.

$$f(x) = ax^2 + bx + c$$

To find the **y** coordinate of the vertex, **k**, you need to evaluate **f(h)**.

To find the **x** coordinate of the vertex, **h**, use the formula:

$$h = \frac{-b}{2a}$$

•

$$\begin{aligned} h &= -(0)/(2(4)) \\ &= 0/(2(4)) \\ &= 0/8 \\ &= 0 \end{aligned}$$

•

$$\begin{aligned} f(h) &= f(0) \\ &= 4(0)^2 \\ &= 0 \end{aligned}$$

The answer is **0**.
