# Hamstring Assistance Device 

A Major Qualifying Project Report<br>Submitted to the Faculty of<br>WORCESTER POLYTECHNIC INSTITUTE<br>In partial fulfillment of the requirements for the<br>Degree of Bachelor of Science in Mechanical Engineering<br>By

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Date: 4/28/16
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## Acknowledgements

Throughout this project, the team utilized the experience and expertise of several individuals in the WPI community. The team would like to thank the following individuals for their contributions to the project: Jared Grier Class of 2018, Ben Freed Class of 2018, Trey Kling Class of 2015 and finally our advisor Professor Eben Cobb.


#### Abstract

Reduced functionality of the hamstring muscle creates a need for a device to assist in riding a bicycle. The project is to design a device to enable a person who has reduced usage of the hamstring muscle to ride a bicycle by aiding leg motion between the pedal angles of $180^{\circ}$ to $225^{\circ}$. The device is for recreational cycling, and adaptable to a range of bicycles. Design concepts were made to store energy provided during the portion of the pedal stroke in which the user can provide power $\left(0^{\circ}-180^{\circ}\right)$, so it could be utilized during the portion of the pedal stroke where the user cannot provide power due to their disability $\left(180^{\circ}-225^{\circ}\right)$. The final design uses a pair of extension springs with a four stage pulley system to store energy and provide the range of motion for the pedal stroke.


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## Introduction

Bicycling is not only a great form of alternative transportation, but also a wonderful recreational activity. Unfortunately many people experience injury which may render them unable to ride a bicycle, one of the more common injuries among Americans is that of a stroke. After stroke there can be lasting effects on its victim such as hemiparesis which is a partial paralysis of one side of the body. It has been shown that bicycle riding can be used as an effective form of physical therapy for such victims. Hemiparesis victims while, may be capable of riding a stationary bicycle, may not have the necessary muscular control to complete a full bicycle crank cycle on a recreational bicycle, in particular these victims whose hemiparesis has affected their hamstring muscles will have increased difficulty in completing a portion of the crank cycle in which the hamstring muscle is the only active muscle. The goal of this project is to design and build a device to enable a user who has reduced usage of the hamstring to ride a bicycle by aiding leg motion between the crank angles of $180^{\circ}$ to $225^{\circ}$ (the angles of a crank cycle in which the hamstring is the only active muscle). This device must be useable for recreational purposes, and must be adaptable to a range of bicycles. This report will explain the methods used to create the device as well as provide information on the end product, conclusions and suggestions for future work on this problem.

## Background

"Stroke is the leading cause of serious, long-term disability in the United States" (Weiss, T. C). One of these long term disabilities is known as hemiparesis, which is a partial paralysis of one side of the body. Approximately 8 out of 10 stroke survivors suffer from some form of hemiparesis (Hemiparesis, 2014). In addition to stroke, many diseases of the nervous system or brain, such as multiple sclerosis or brain tumors, can cause hemiparesis (Weiss, T. C.). With hemiparesis, the disabled person still has the ability to operate the affected side of their body; however, this operation suffers from reduced muscular strength (Hemiparesis). There are many accepted treatment options for those who suffer from hemiparesis, some involve electrical stimulation, while others focus more on physical rehabilitation of the affected muscle groups (Hemiparesis).

Whichever treatment method, or combination thereof, is chosen for rehabilitation after a stroke, it is important to understand the concepts of both neuroplasticity and neurogenesis.

Neuroplasticity is the brain's ability to "rewire" itself after being damaged. Neurogenesis refers to the brain's ability to create new neurons. These neurons will require support from neighboring cells, blood supply, and connection with other neurons for survival. (Neuroplasticity and Stroke Recovery). "Rehabilitation involving neuroplasticity principles requires repetition of task and task specific practice to be effective" (Neuroplasticity and Stroke Recovery). What this means for stroke patients is that the more the patient is able to use, or practice stimulating, the affected areas of the body and mind, the more effective rehabilitation will be. (Neuroplasticity and Stroke Recovery).

For patients suffering from lower extremity weakness, the pedaling motion required to ride a bicycle could be an effective repetitive motion to strengthen all muscles in the leg. Utilizing the concept of neuroplasticity and its application to stroke patients, it would be desirable for a patient to have the ability to incorporate bicycling into everyday life, perhaps even as a primary mode of transportation. Due to excessive weakness of any or all muscles in the leg, it may be impossible to use a bicycle without some form of pedal assistance.

Studies have shown that muscles work in a systematic and coordinated way during cycling to direct power from the human body to the pedal and crank of the bicycle. This is known as muscle recruitment and there have been exhaustive studies researching the patterns of how humans use their muscles while cycling. We have studied this literature and identified critical areas where force production by a rider with hemiparesis, specifically affecting their hamstring muscles, would be weakened or impossible.

The crank cycle can be broken down into three phases, the propulsive or downstroke phase, the recovery or upstroke phase and the pushing phase, in which the foot is pushed forward at the top dead center (TDC).


Figure 1: Crank Cycle Phases
The propulsive phase, beginning at the top of the stoke $\left(0^{\circ}\right)$, is characterized by the extension of the hip and extension of the knee. These motions primarily recruit the quadriceps and glutes. During the recovery phase, from $180^{\circ}$ to $360^{\circ}$, the hamstrings and hip flexors work together to flex both the hip and knee. Force generated by these muscles serve two functions. The first is to reduce the resistance on the crank for the propulsive phase on the opposite leg. The second, the recovery phase provides flexion allowing the crank to rotate and assist the opposite leg in propulsion.


Figure 2: Hamstring Leg Motion


Figure 3: Hamstring Calf Motion
The primary focus of our project, the hamstring muscle group, is comprised of three different muscles, The Bicep femoris, the semimembranosus and the semitendinosus. This group is active from $10^{\circ}-350^{\circ}$ at varying intensities. The Bicep femoris is active from $350^{\circ}-230^{\circ}$, with peak output at $110^{\circ}$. The semimembranosus and semitendinosus are active from $10^{\circ}-230^{\circ}$, with a peak output at $100^{\circ}$. During the last $45^{\circ}$ of hip extension range of motion, ending just past the $180^{\circ}$ point of the crank cycle, at the beginning of the recovery phase, the hamstrings work alone in hip extension. This is where riders with weak hamstrings are unable to continue applying
torque to the pedal in the recovery phase and must attempt to complete the crank cycle using torque generated by the other leg, which is in the propulsion stage.

With a weak hamstring, it may still be possible for a rider to cause a full revolution of the crank by using down-stroke force from the opposite leg. However there is an importance to a pedal stroke for where there is even distribution of power to the pedals during the course of the entire pedal revolution. The use of racing pedals that restrain the foot to the pedal are an example of this concept. These restraints help the rider to exert force throughout the full revolution by allowing them to fully engage their active muscles, including the hamstrings, on the upstroke of the pedal cycle. Muscles activated in a defined pattern are not just for optimizing the energy transfer from the human body to the machine but also provide protection to the major joints. For this reason we look to design a device to aid the hamstring in generating force on the pedal during the recovery phase of the pedal stroke, to help riders with hemiparesis have an improved cycling experience and even reduce the risk of injury.

So far, many devices have been designed to aid rehabilitation of weakened muscles due to hemiparesis, but none simply for recreational purposes. Many are based on the premise of actuating the weaker muscles against incrementally increasing resistance. One such device is US patent 6220991B1, depicted in Figure 4.


Figure 4: Depiction of Device From US patent 6220991B1
The user grips the handles and places his or her feet in the pedal straps. They would then rotate the pedals. The pedals are connected to the handles, causing some motion. They are also connected to a fan blade in the front of the device, which provides slight resistance. This device allows for safe exercise for a person with reduced muscle strength, such as in the case with hemiparesis. Conventional exercises such as jogging or weight lifting can be too strenuous for a person with reduced muscle strength. This device has the advantage of allowing for varying loads as well as providing a controlled experience.

With respect to the proposed goal, devices exist that could be used to enhance the use of a bicycle for recreational or competitive activity. One such device is US patent 5515746A, depicted in Figure 5.


Figure 5: Depiction of Device From US patent 5515746A

This device was designed to increase torque to the drive shaft without increasing the length of the crank arm. It consists of a "bearing disposed on a frame of the bicycle and has an eccentric plate put on a rotating shaft having cranks with pedal" (U.S. Patent No. 5515746A, 1994). The plate is fixed relative to the frame of the bicycle. There are linking members connecting the chain wheel to a working plate. The result is that the chain wheel can be rotated in a smaller radius, resulting in greater torque. This device could be useful for a person with hemiparesis because the person would produce reduced torque for sections of the cycle.

Another type device to allow the use of a bicycle for a person with hemiparesis would be one that attached to the user. This is seen is U.S. Patent No. 6368256, depicted in Figure 6.


Figure 6: Depiction of Device From U.S. Patent No. 6368256
As can be seen, there are elastic bands that reach from the waist to the feet. During the downward motion of the pedaling action, the bands are stretched, storing energy. This energy is released during the upward motion, assisting the user. For our particular case of hemiparesis, the subject has a weakened hamstring. This results in difficulty raising up the leg in the backward motion of the stroke. This device would take energy from the stronger sections of the legs and use it for the problematic section.

Before beginning discussion on the design of a device for a bicycle, let us first define some basic bicycle terminology, for this please refer to Figure 7 below:


Figure 7: Bike Frame Terminology

In the following discussions we refer to a section of the bike as "the rear triangle" this is comprised of the seat tube, the chain stay, and the seat stay.

## Functional Requirements

This section lists the functional requirements developed by the project team. These requirements act as the design specifications for the final device. Each requirement is followed by a short explanation of its significance to the problem we have outlined in previous sections. They are used in the design matrix to rank each device on how well it meets each functional requirement.

- Must be adaptable to a range of commuter/road bikes bicycles.
- The team wants the device to be useful to people who already have a bicycle so they don't have to pay for an expensive new one.
- Must interface with bike and/or rider(allow for free motion of the bike)
- The goal is to design an assistive device for recreational purposes. This specification is to ensure that our design will allow a bicycle go anywhere a non assisted bicycle would normally go, rather than be stationary or relient on a source of power.
- Must aid leg motion between the angles of $180^{\circ}$ (bottom of pedal cycle) to $225^{\circ}$.
- The users that are the focus of the project cannot generate enough force with their hamstring to pull their leg through the phase denoted by the angles. These numbers were found through research that stated $180^{\circ}$ to $225^{\circ}$ is the range at which the hamstring is the primary muscle engaged
- Powered solely by the rider of the bike
- Team team does not want did not want to use any electrical components to make the device. These require expensive components, increase weight and would cause the device to rely on a power source.
- Must cost under $\$ 100$ to produce.
- Each student is allotted $\$ 150$ though the MQP program at Worcester Polytechnic Institute. This device budget was decided to allow for the creation of multiple prototypes
should one design fail to work in practice, or should a prototype break during testing. This will also potentially allow for a series of design iterations on a successful design as well.
- Must weigh under 5lb
- The device cannot increase the weight of the bike and rider system by a large margin or it will increase the force required on the pedal to continue forward motion, negatively affecting our goal. However the device must have some weight so it was found through research that the average weight of a commuter bike is 301 b and it was decided that $15 \%$ increase in weight would be acceptable, which left us with 5 lb .
- Must retain the weight balance that is characteristic of the bicycle.
- The use of a bicycle relies on it being a balanced devices that does not tip. The device must not cause major change in the bicycles balance as we don't want a user that has difficulty riding a bicycle to have to operate an imbalance bicycle.
- Must be smaller than 50 cm by 38 cm by 12 cm
- Based on the geometry of an average commuter bicycle the team decided that this would be the most appropriate design envelope without inhibiting the normal operation of the bicycle as a device of this size would fit within the frame of the bike.
- Must not interfere with pedaling motion
- One of the challenges of this problem is working around the mechanisms that make up a bicycle. Our device must avoid that path of any preexisting components that are in motion while riding including the wheels, crank and chain. The device must also allow the leg to be engaged with the pedal at all times as well as avoid the leg entirely for as it has potential to cause injury.
- Easily removable with basic tools
- This allows a user to attach the device to a bicycle without having to pay for unconventional tools. Some tools that would be considered basic are a screwdriver, wrench, pliers, hammer or allen wrench.
- Must comply with (ASME) ASTM standard G50-10 for weather resistant material
- The device to be designed is for a recreational bicycle rather than a stationary bicycle so it should be able to withstand the weathering conditions bicycles are typically subjected to.
- Must generate positive tangential force sufficient to supply motion through the range of $180^{\circ}$ to $225^{\circ}$
- Tangential force, relative to the path of the crank, on the pedal is needed to accelerate and maintain speed of the bicycle. The force on the pedal was found through experimentation using a spring scale on the bicycle pedal as well as mathematical evaluation of the bikerider system with a desired acceleration of the rider.
- Producible in WPI laboratories
- The team only has access to the equipment in WPI laboratories so we would be limited to the manufacturing tools available to us. This must be considered when developing a design to ensure that it will be producible.
- Means of controlling and inducing proper ankle position while keeping the foot attached to the pedal
- One of the issues hemiparesis patients suffer from, is an inability to maintain ankle alignment. The alignment of the ankle relative to the pedal affects the amount of power one is able to transmit to the pedal.


## Preliminary Design

## Two Chains Design Concept

One design that was conceptualized was assigned the name of "Two Chains" design, this concept was based off of a regenerative braking system for bicycles in which the bicycle momentum would be stored in a flywheel, when braking, and released back to the wheel when needed for acceleration. The two chains design, was essentially this regenerative braking system without a flywheel for energy storage, rather the design would transmit the rotational energy through a gearing system directly to the bicycle cranks. Depicted below in Figure 8 is a representation of this design.


Figure 8: Drawing of "Two Chains" Design Concept

Seen above in Figure 8 is the design concept for the two chains design. In this design rotational energy from the wheel is transmitted from gear 1 (G1 in figure) through the first chain (labeled C 1 above), to gear 2 ( G 2 above). The gearing here was designed to take the high angular velocity of the wheel as an input, and gear it down to a low angular velocity, high torque output. Gear 2
was then directly attached to gear 3 (G3 above), thus allowing gear three to rotate at the same angular velocity as gear 2 . Gear 3 would than transmit its rotational energy through chain 2 (C2 above) to gear 4 (G4 above). The gearing in this section of the design was meant to lower the angular velocity of gears 2 and 3, and generate a higher torque output at gear 4, thus ensuring the device would be able to lift the user's leg through the desired crank angle, without causing the crank to rotate too quickly. During the conceptualization of this design, it was discussed that a coasting mode would be desirable, should the user wish to stop pedaling, while remaining in motion. It was also discussed that we should consider implementing a gear cassette allowing for variable gear ratios, and subsequently variable output angular velocities and output torques to the crank.

Ultimately it was decided that it would cost the most to produce, would be less adaptable to a range of bikes, and would be difficult for a laymen to install on their personal bikes, for these reasons the design was rejected. These reasons were tabulated in a decision matrix to compare this concept to others. The decision matrix can be found in Appendix H: Decision Matrix.

## Four Bar Design Concept

Another design that was considered was a quick return linkage mechanism. In this design, a bar would be mounted directly to the pedal shaft and connect to a spring through the means of a four bar mechanism. Energy would be stored in the spring during the downward phase of the pedal stroke where the rider is able to apply force, this energy would then be released during the upward phase of the pedal stroke which the rider has difficulty completing due to their disability. The four bar would be designed so that the section of the stroke that stores energy would be a greater angle than the section of the stroke that the energy is released in. This
way, the returned force would be concentrated in the portion of the stroke needed. This would be designed with the same method as a quick return mechanism, a simple representation of this device can be seen below in Figure 9


Figure 9: Depiction of "Four Bar" Design Concept
In the figure above, the mechanism has pin joints at points $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D . Link 1 represents the crank of the bicycle, while links 2 and 3, make up the remainder of the quick return mechanism. The addition of the spring in this mechanism, allows for an appropriate amount of energy to be stored during the pushing phase of the pedal stroke, which would be released during the portion of pedal stroke the rider needed assistance with.

This design scored poorly relative to the other designs in our decision matrix because it poorly met many of the design requirements. For example, it had a low score in "adaptable to a
range of bikes". This is because the angles were dependent on the size of the bike and attaching the mechanism is dependent on the shape of the bicycle. In addition, the bulky nature of the device caused it to score poorly in "Doesn't interfere with motion of bike" and "Maintain weight balance of bike." The design would require long beams that would need to reciprocate rapidly. Such movement would be isolated to one side of the bicycle, causing imbalance. This also caused concerns for the weight of the device, lowering its score in the weight requirement.

The device did score well in some other areas, particularly ones related to the functionality of the device. It did increase the power to the pedal and it was powered solely by the rider. It could be made with materials that would meet weather resistance standards. Like the other devices, it scored well in force applied, attach foot to pedal, and force application. This suggests that certain aspects of this design could be integrated into future designs.

## Retractor Design Concept



Figure 10: Depiction of "Retractor" Design Concept

The retractor design concept was based on the motion of a tape measure as it pulls in the tape. A design concept was created that would use a spring placed behind the seat of the bike used to pull on the pedal of the bike to cause normal motion of the pedal through the phase of the stroke where the leg is weak. A steel cable would be connected to the spring and the pedal. During the downstroke the wire would be pulled causing deflection in the spring. The stored energy would then be released as the pedal continues in the cycle and the spring returns to a neutral position. This design out scored the other designs significantly in the decision matrix with a score of 979 (see Appendix H: Decision Matrix) due to many attractive features. Its mounting placement makes it highly adaptable to different bikes and gave the designer plenty of room to design the features of the device without interfering with the normal motion of the bike and rider. Also due to the small number of parts it seemed like the most inexpensive and simple way to achieve the desired force outputs on the bicycle crank.

A variety of spring options were explored including a radial torsion spring, an extension spring and finally a torsion bar.


Figure 11: Radial Torsion Spring Example


Figure 13: Torsion Bar Example

## Design Analysis \& Refinement

After measuring that the distance between the pedals at two opposite points along the cycle was 16 inches, we concluded that the spring must allow for 16 inches of displacement. This design requirement immediately eliminated the spiral spring from the list of options as there are no available spiral springs with that amount of displacement that were strong enough for our
application. Manufacturing a custom spring was briefly considered but given that there were other spring options concerns about the costs and challenges of designing such a part deterred us from exploring the option further.

Our team concluded that the torsion bar would likely be the best option for our design as it took up very little space and would be very inexpensive. Also with the simple addition of a lever arm at the non-fixed end of the torsion bar we would be able to easily adjust the linear motion of the wire based on the angle of deflection that was attainable from the torsion bar. However designing the torsion bar proved to be far more challenging than expected.

The first task in designing the torsion bar, was to determine the forces the torsion bar would need to exert on the system to assist the rider through the full motion of the pedal stroke. We began by determining an appropriate acceleration for the bicycle to undergo due to the assisting force of the torsion bar, this value was obtained from table 7-1 of Robert L. Norton's Design of Machinery text, the team used a value of 0.1 g , a common acceleration encountered during gentle acceleration in an automobile. Combining this acceleration with the mass of the system (rider mass + bike mass + device mass) we could calculate the necessary force to be applied to the bike, using Newton's second law, this force was found to be 18.5lbs. After taking into account the rolling friction of the wheels, and assuming the rider was in a top gear, we determined the necessary force to be acting on the crank would be approximately 27lbs, this amount of force would cause the bike to accelerate at our desired 0.1 g 's (detailed calculations can be found in Appendix B: Force Required to Accelerate Bike).

After determining the force required to pull on the crank to achieve our desired acceleration, we conducted a four-bar analysis to determine the amount of torque the torsion bar would need to generate in-order to pull the crank with the desired force through the crank phase
in question, 180-225 degrees. We determined the max torque the torsion bar needed to be capable of generating, using an 18 inch lever arm, would be 610 inch-pounds (a detailed four-bar mechanism analysis and torsion bar calculations can be found in Appendix C: Four-Bar Analysis and Torsion Bar Calculations).

The three most important factors we had to consider for the design of the torsion bar where, the angle of twist produced by the torque on the torsion bar, the stresses at the mounting ends of the torsion bar, and the safety factor of the torsion bar. To calculate the angle of twist we used Equation 1 below:

$$
\theta=\frac{T l}{J G}
$$

Equation 1: Torsion Bar Angle of Twist
In Equation 1, theta represents the angle of twist, or angular deflection experienced by the torsion bar, T the torque applied to the torsion bar, $l$ the length of the torsion bar, J the polar area moment of inertia, and G the modulus of rigidity (shear modulus). The modulus of rigidity is a material property and was changed according to which material we were considering. To calculate the stress of the torsion bar, we used Equation 2, below:

$$
S_{t}=K_{f s}\left(\frac{16 T}{\pi D^{3}}\right)
$$

Equation 2: Stress in a Torsion Bar
Where $K_{f s}$ is the fatigue stress concentration factor, $T$ is the torque the torsion bar is subjected to, and $D$ is the equivalent diameter of the square mounting end on the torsion bar. The equivalent diameter is calculated through equations 6.7 c , and 6.7 d, from Norton's Machine Design Text reproduced below as Equation 3 and Equation 4.

$$
A_{95}=\pi\left[\frac{d^{2}-(0.95 d)^{2}}{4}\right]
$$

$$
D_{\text {equiv }}=\sqrt{\frac{A_{95}}{0.0766}}
$$

Equation 4: Equivalent Diameter for Non-Round Cross Section
Where $A_{95}$ represents the portion of the cross-sectional area of the non-round part that is stressed between $95 \%$ and $100 \%$ of its maximum stress. And $D_{\text {equiv }}$ is the equivalent diameter of a noncircular rotating cross section, the square mounting ends of the torsion bar for us. The torsion bar we were designing had a square mounting end, which was smaller than the diameter of the torsion bar itself; this change in geometry causes a disruption in the flow of force through the part, and as such will concentrate forces at the interface of the two geometries. $K_{f s}$, the fatigue stress concentration factor, accounts for the increased stress due to the change in geometry when the part is subjected to dynamic loading, and can be calculated with equation 6.11 b from Norton's Machine Design text reproduced below, as Equation 5:

$$
K_{f s}=1+q\left(K_{t}-1\right)
$$

Equation 5: Fatigue Stress Concentration Factor
Where $q$ is the notch sensitivity and $K_{t}$ is the geometric stress concentration factor. The notch sensitivity is defined in equation 6.13 of Norton's Machine Design text, reproduced below as Equation 6:

$$
q=\frac{1}{1+\frac{\sqrt{a}}{\sqrt{r}}}
$$

Equation 6: Notch Sensitivity
Where $a$ represents Neuber's constant, and $r$ the notch radius. The notch radius, refers to the radius of curvature of the edge between two sections of differing geometries. Neuber's constant can be determined from tables 6-6, 6-7, and 6-8 of Robert L. Norton's Machine Design text
book, for the materials we were using we needed to interpolate these tables, so we could get Neuber's constants for tensile strengths not listed in the tables (interpolation of these tables can be found in Appendix F: Interpolations for Determining Stress Concentration Factors). The geometric stress concentration factor used in Equation 5 can be calculated using:

$$
K_{t}=A\left(\frac{r}{d}\right)^{b}
$$

Equation 7: Geometric Stress Concentration Factor
Where $d$ is the diameter of the smaller geometry, and $r$ is the radius of curvature between the two geometries; $A$ and $b$ represent constants which can be determined from tables in appendix C of Robert L. Nortons Machine Design text book, once again to get the values for our specific geometry we had to interpolate these tables, this interpolation can be found in Appendix F: Interpolations for Determining Stress Concentration Factors.

Lastly the safety factor of the torsion bar can be determined by the ratio between the yield strength of the material and the stresses in the material, for our purposes we used Equation 8 below:

$$
n=\frac{\pi D^{3}}{32 K_{f s}\left(\frac{T_{a}}{S_{n}}+\frac{T_{m}}{S_{y}}\right)}
$$

Equation 8: Safety Factor for a Torsion Bar
Where $D$ is the diameter of the torsion bar, $K_{f}$ is the fatigue stress concentration factor, $T_{a}$ the alternating torque, $T_{m}$ the mean torque, $S_{n}$ the fatigue limit of the material, and $S_{y}$ the yield strength of the material. Since our torsion bar operates between zero torque and max torque, only being rotated in one direction, it is subjected to repeated loading, for which the alternating and mean torques are equivalent. The fatigue limit of the torsion bar is determined by taking into account the number of cycles the torsion bar will be subjected to as well as various operating conditions such as the loading conditions, the size, the finishing on the part, the operating
temperature, and the desired reliability; the fatigue limit can be determined using the following equations:

$$
\begin{gathered}
S(N)=a N^{b} \\
\text { Equation 9: Stress of Torsion Bar as a Function of Cycles } \\
b=\frac{1}{Z} \log \left(\frac{S_{m}}{S_{e}}\right) \\
\text { Equation 10: B value for Equation } 9 \\
z=\log \left(N_{1}\right)-\log \left(N_{2}\right) \\
\text { Equation 11: } z \text {-value for Equation } 10 \\
\log (a)=\log \left(S_{m}\right)-3 b \\
\text { Equation 12: a-value for Equation } 9
\end{gathered}
$$

Where $N$ is the number of cycles to which the torsion bar is subjected, $N_{l}$ is always 1000 cycles, and $N_{2}$ represents the number of cycles at which the fatigue limit occurs. $S_{m}$ is the mean strength at $10^{3}$ cycles and $S_{e}$ is the endurance limit of the material (for some materials this is called the fatigue limit and denoted as $\mathrm{S}_{\mathrm{f}}$ ); both the mean strength and the endurance limit can be calculated using equations 6.7 and 6.9 from Norton's Machine Design text, reproduced below:

$$
S_{m}=0.9 S_{u t}
$$

Equation 13: Mean Strength for Bending Loading

$$
S_{m}=.75 S_{u t}
$$

Equation 14: Mean Strength for Axial Loading

$$
S_{e}=C_{\text {load }} C_{\text {size }} C_{\text {surf }} C_{\text {temp }} C_{\text {reliab }} S_{e}
$$

Equation 15: Corrected Endurance Limit
Where $S_{u t}$ is the ultimate tensile strength of the material; $C_{\text {load }}, C_{\text {size }}, C_{\text {surf }}, C_{\text {temp }}$, and $C_{\text {reliab }}$ refer to constants determined by various conditions the torsion bar is subjected to, and are further
defined in equation 6.7 of Norton's Machine Design text book. $S_{e}$ ' refers to the estimated endurance limit and is determined for various materials using equation 6.5 of Norton's machine design text.

Using these equations we were able to develop spreadsheets allowing us to analyze the angle of twist, the torsion bar stress, and the safety factor for various diameters and lengths of the torsion bar. Using these spreadsheets we could easily alter the material properties to analyze different material options for the torsion bar. The materials we considered were low carbon stainless Steel, Aluminum 6065 and a series of plastics. The materials were chosen based on their yield strength, elastic modulus, cost and availability. The spreadsheets could then be compared to find the best diameter and length of the torsion bar, such that it would provide an appropriate angle of twist without being at risk of failure (examples of these spreadsheets can be found in Appendix L: Spreadsheet Analysis). The data points from the stress spreadsheet could then be used to generate a Goodman diagram to visualize the performance of each option, a Goodman diagram for aluminum 6061 can be seen below in Figure 14(for the complete set of Goodman diagrams produced please refer to Appendix A: Goodman Diagrams). After weeks of analysis it was concluded that the best option would be aluminum 6061 however this was not without serious compromise. By mounting the bar perpendicular to the direction of the bike, the bar was limited to be no longer than the length of the handle bars. This limitation restricted us to a maximum deflection angle of 9 degrees from a bar 10 inches in length and 1.25 inches in diameter. The team concluded that while potentially viable this option was poor due to the large length of the lever arm (approximately 8.5 feet for the torsion bar described above) required to achieve the necessary 16 inches of linear displacement to allow the pedals to complete a full
cycle. With this decision the team came to the conclusion that the torsion bar would be a poor method of obtaining an assistive pedal force, and thus explored alternative options.


Figure 14: Goodman Diagram for Al-6061

With a far greater understanding of the problem at hand the team generated a new design of this retractor device, utilizing extension springs rather than a torsion bar or spiral springs to obtain the necessary pedal assistance force. In order to get proper linear deflection from the spring, the mounting placement was moved from behind the seat to under the top bar. Also a pulley is used to double the linear displacement of the extension spring to further our pursuit of 16in of displacement by the end of the steel wire that is attached to the pedal. Finally in order to
pull the pedal up in the direction desired, a guidance pulley was added to the rear triangle of the bike directly above the axle of the back wheel, a depiction of this concept is seen below in Figure 15.


Figure 15: Representation of Spring Mechanism Design

After some brief research and analysis is was concluded that this embodiment of the retractor design would be the best way to meet our design specifications. More information of the final design of this concept will be included in the next section.

## Final Design

The final design consisted of a force producing mechanism, consisting of the two extension springs and pulley system 1, from Figure 16 below, these components were contained between two U-channels, which were fastened to the top tube of the bicycle via aircraft clamps. A cable was routed through the pulley system, around a guidance pulley and attached to the pedal, to supply the necessary assistive force.


Figure 16: Depiction of Final Retractor Design

## Linear Displacement

The bicycle crank is 8 inches from the center of its rotation axis to the center of the pedal. This means that during a full pedal cycle, the pedal experiences 16 inches of linear displacement. For the purposes of our device, this means the cable exiting the U-Channel will need to be capable of experiencing the required 16 inches of extension to account for the 16 inches of displacement at the pedal. The size limitations of the bike only provide 20 inches to place the spring mechanism in, since the springs have a free length of 8 inches, this leaves 12 inches of
space for displacement. Since we needed to obtain 16 inches of displacement, we chose to utilize the mechanical advantage of a compound pulley system to increase the length of cable that exits the U-channel while decreasing the amount of displacement the springs will experience.

## Pulley System

A compound pulley system provides mechanical advantage by dividing the amount of force, required to displace an object of weight (w), a distance $x$, by the number of rope passes $(\mathrm{N})$ made through the pulley system, such that the user must pull the rope a distance of N times x to achieve an object displacement of distance x. For our design we need to increase the distance pulled to achieve the appropriate linear displacement of 16 inches. In order to maintain the required force output of the spring mechanism we will need to increase the spring rate by N times. Since we are now adding pulleys to our design the amount of room for linear displacement of the springs will decrease even further, the pulleys chosen have an outer sheave diameter of 2 inches, to make a compound pulley system we will need two of these pulley blocks, such that the amount of space allotted for linear displacement within the U-channel mechanism will be decreased by 4 inches from 12 inches to 8 inches. With the addition of pulleys to the mechanism we will need to include a method of mounting them, which will take up space as well. The mounting design for the pulleys takes away an additional 3 inches from our linear displacement available within the U-channel, this limits us to 5 inches of linear displacement. With 5 inches of available room for the springs to experience linear displacement, we will need a pulley setup that has at least 4 passes, which will require the springs to be displaced 4 inches to achieve the desired cable displacement of 16 inches.

## Spring Selection

Discovered during analysis, the cable will need to be capable of exerting 30 lbs of pulling force on the pedal, this will provide the necessary torque about the crank axis to lift the dead weight of an average human leg (detailed analysis is provided in Appendix D: Torque Required to Lift Dead Weight of Leg and Appendix E: Pulley Design Analysis). Since we will be making 4 passes over the pulley system the force produced by the spring setup must be at least 120 lbs after the spring is displaced 4 inches (16/4 inches) which will require a spring rate of $32 \mathrm{lb} / \mathrm{in}$. Due to size limitations for spring diameter created by the internal width of the U -channel being 1.25 inches, we chose to implement two springs in parallel, each with a spring rate approximately half of what is mentioned above. The spring rate of the springs we chose is 16 $\mathrm{lb} / \mathrm{in}$, with an initial tension of 8 lbs . Thus the combined spring rate is $32 \mathrm{lb} / \mathrm{in}$ with a total initial tension in the system of 16 lbs . At an extension of 4 inches, neglecting the initial tension these springs will produce a pulling force of 128 lbf , when we include the initial tension of 16 lbf , we have a total pulling force from the springs of 144 lbf which is only slightly more than the desired pulling force, but subsequently will be enough to lift the dead weight of a heavier than average leg.

## Mounting Structure

For our design, we needed a way to enclose the device so that the mechanisms were at least partially covered and well supported. We also needed it to be light and easy to modify. We also have to consider ease of manufacturing and repairs. Our original design was to have one Uchannel with a groove cut into the side. There would be a pin that slides in the groove to support the pulleys. We decided that this did not cover the mechanisms enough and that cutting a groove could be problematic. We decided to instead use two U-channels; one on top and one
underneath. They would be spaced apart from each other to form a slot without the need for cutting one. The pulleys would also be supported more securely. In addition, the springs would be mostly covered up, making the device safer for the user. We wanted to minimize the weight of the channels, so we used $1 / 8$ th in thick aluminum channels that were 1 in wide with $1 / 2$ in legs. The total length of each channel is 20 in .

In order to hold the channels together, we designed a set of brackets that hold the parts together. One would be used to mount the springs and be mounted to the back of the channels. The spring hooks would be attached to this bracket, via spring anchors. The bracket has legs on the sides so that bolts could be used to attach it to the channels, this bracket is depicted below in Figure 17. On the opposite end of the U-channel, there would be a similar bracket, used to mount the pulley, depicted in Figure 18.


Figure 17: Spring Mounting Bracket


Figure 18: Pulley Mounting Bracket

In order to mount the device onto the bicycle, a series of airplane clamps were used. These are adjustable and easy to attach using just a screwdriver. To attach the clamps, a series of slots were cut into the top U-channel. The airplane clamps could then be fully opened and threaded through the slots. These aircraft clamps would also be used to hold the acrylic plate that supports the rear pulley in the proper position.

## Guidance Pulley

In order for the device to complete the task of lifting the rider's leg, the energy from the springs and the displacement of the wire must be directed effectively. The force from the springs must be supplied to the pedal at the correct position and from an ideal angle. The wire must also
not interfere with the normal motion of the rider's leg. To do this a method of guiding the wire along its path was designed.

The solution that was chosen to guide the wire was a side mounted pulley that would change the direction of the wire from its position where it exits the device. The hardware chosen was a side mounted single pulley pictured below in Figure 19. This part is very thin so the wire is kept close to the bike. This is advantageous as compared block pulley which would pull the wire away from the frame which brings up issues with safety and would result in a loss of force exerted on the pedal due to the transmission angle of the wire.


Figure 19: Side Mount Guidance Pulley
The challenge of designing this aspect of the final device was choosing a mounting mechanism. Our key requirements were that the position of the pulley would be such that when the pedal reached the bottom part of the pedal stroke the potential energy in the springs would be released and that there would not be a significant loss in the transfer of energy due to a large transmission angle. After conducting a force analysis (Appendix E: Pulley Design Analysis), a position inside the rear triangle of the bike was determined. This position is both (a) above the pedal so it will begin pulling on the pedal after it reaches the bottom of the stroke and (b) results in the best possible angle of transmission, which is tangential to pedal direction, during most of the weak portion of the rider's pedal stroke. In order to mount the pulley in this rear section of
the rear triangle a mounting plate was designed, displayed below in Figure 20. This plate was meant to use aircraft clamps to hold it to the frame of the bike and the guidance pulley would be bolted to the plate. The plate was designed out of acrylic because of its light weight, low cost, and manufacturing ease. A tear out analysis was completed to ensure the material would be strong enough to hold up to the forces applied both at the pulley and the clamps (detailed calculations of this can be found in Appendix G: Guidance Pulley Mounting Plate Tear-Out Analysis). The final design utilizes the least material possible while still allowing for some aesthetic additions to the plate.


Figure 20: Mounting Plate for Guidance Pulley

## Pedal Connection

The final step in our design was to connect the wire to the pedal. The simple solution we chose was to loop the wire around the connector between the pedal and the crank shaft. To do this a steel wire rope thimble clip was purchased along with some U bolts made for the wire diameter chosen. The thimble clip is used to keep the loop of wire around the pedal large enough to not do damage to the wire and to prevent the wire from sliding up the shaft. The U bolts ensure that the wire stays looped around the pedal and does not come undone during usage of the device.


The final spring mechanism is depicted below in Figure 22.


Figure 22: Final CAD Model of Spring Mechanism

## Results

During assembly of the spring mechanism, the team was experimenting with sliding the acrylic block back and forth within the U-channel, in doing this we discovered that there was a considerable amount of friction present between the sliding blocks and the aluminum U channels. We became concerned that this large amount of friction would cause issues when the device was completed. The input force required by the user felt excessive during the trials.

When initially attaching the device to the bike, we were short one aircraft clamp that was needed to attach the acrylic plate to the bike. We decided to attach the guidance pulley mounting plate to the bike with only three aircraft clamps, rather than the four we had designed it to use. Unfortunately, due to a decreased shearing area, caused by the missing aircraft clamp, the stress induced by the operation of the spring mechanism caused the aircraft clamp, to tear out of the plate; luckily we had manufactured a spare.

After breaking our first guidance pulley mounting plate, we acquired the missing aircraft clamp, and attached the alternate mounting plate to the bike using all four aircraft clamps as we originally intended. As our analysis had predicted, the part would not fail when correctly attached to the bike. With the guidance pulley properly attached and the device working we began judging how well the device worked. The first thing we noticed during our tests was that the guidance pulley had been mounted too low; making it so the device would provide an assisting force between about 90 and 270 degrees of the crank cycle. We had wanted an assisting force between the crank angles of about 170 and 350 degrees, with the crank angle range needing the most assistance being 180 to 245 degrees. By choosing to mount the guidance pulley higher
we could have achieved a resulting crank angle of assistance closer to that which we desired. This issue with location was a result of using a different bicycle than we had originally designed our system for.

The second largest issue we discovered about our device was how much force it required to extend the spring system during the downward pedal stroke. With both springs in place it felt as though the springs pulled the pedal through its pedal stroke with an acceleration that may be uncomfortable or unsafe for a person suffering from diminished muscular strength. As an experiment we disconnected one of the springs, cutting the output force in half, while this required a much more reasonable force to extend the springs the team didn't feel like the device was providing quite enough of an assisting force when the spring retracted; however, through discussion our team determined that the lower acceleration of the return pedal stroke from the use of one spring was more ideal for the devices intended use.

The final and least worrisome issue discovered in the device, was that the mechanism could not fit completely in the frame of the bike, as we had hoped. This was due to the size of the pulley blocks, with pulley blocks that were just slightly too wide to fit the pulley vertically aligned in the slot of the U-channel, we were forced to mount the pulleys in a horizontal alignment. The horizontal mounting orientation of the pulley required the two U-channels to be separated with a larger gap than a vertical pulley orientation would have required, resulting in a final mechanism height of 3.40 inches. With a head tube length of 3 inches, we could not make use of the full length of the top bar, as we had intended to. This forced us to mount the device with a diagonal offset from the center of the frame. With the spring mechanism mounted at an angle, the cable exiting the spring mechanism was forced to rub against the edge of the aluminum spring mounting bracket, as it made its path to the guidance pulley; this rubbing
caused, the cable to abrade its protective plastic coating, and the team postulated that eventually the cable would fray and subsequently snap after repeated uses.

## Conclusions

The goal statement of this project was to design and build a device to enable a user who has reduced usage of the hamstring to ride a bicycle by aiding leg motion between the pedal angles of $180^{\circ}$ to $225^{\circ}$. Considering this, the device produced comes very close to meeting this goal, but still requires improvements and further prototyping in order to fully reach the goal.

The final design does unquestionably aid leg motion through the angles specified, but it does so with some very significant drawbacks. The greatest of these is the large input force required from the rider during the down-stroke in order to extend the springs. By demanding so much energy from the rider during this phase there will be greater fatigue while riding and reduced energy for propulsion. Furthermore, given that this device is meant for a stroke victim the input force required might be more than they can exert. If a rider was unable to extend the spring then this device would only be successful in moving the issue of not being able to complete a pedal stroke to a different phase of the pedal stroke. This concern makes it very questionable whether this device would be helpful to a stroke victim. However, as stated in the results section it is possible that only using one spring would be more effective and could possibly alleviate this concern.

Solving the issues with this device may not be as simple as just removing a spring. Our calculations and tests show that it takes more force than that spring can supply to lift and average man's leg. This device may require future engineers to look into more advanced solutions to supply forces as the current device would not be comfortable to ride even for an able bodied person. The device may need to employ clever mechanisms that utilize mechanical advantage or electromechanical devices to generate a truly useful device. In the current prototype the high input force required and the loss of energy when it is finally released both indicate the device
may need more elaborate methods of mechanical advantage in order to make it usable for a stroke victim. A potential stronger solution to the issue would be the use of an electric motor. This would significantly drop the devices reliance on the rider and could remove the need to for complex mechanisms which could pose safety risks to the rider. Much more prototyping would need to be done to explore these concepts.

The greatest challenges that the team faced when designing this device was likely the design requirements we had placed on ourselves. Demanding that the device be purely mechanical and easily attachable to many bike was a demanding pair of requirements that significantly limited our imagination. While such a device would be both novel and ideal, it is doubtful that such a device would be the most effective way to aid a stroke victim in riding a bicycle. This team concluded after our attempt at creating such a device that a broader approach to solving the problem with more succinct design specifications should be used by engineers exploring this concept in the future. Some of these possible approaches will be discussed in the next and final section of this paper.

## Recommendations and Future Work

After testing our prototype, we concluded that certain aspects of the design could be improved. Our original prototype had issues fitting onto the bicycle, and with the amount of force required by the user. We found out that our original assumptions used to calculate the necessary force were wrong, and that the required force was actually less than we had expected.

To address these concerns, certain mechanical changes to the device are possible. First, the friction of the device could be reduced in the slider block through the use of a layer of lowfriction material, or changing the block material to a low friction material. The force could also be reduced by using a single custom spring that provides a more suitable force. In addition to being reduced, the force needs to be applied at the ideal portion of the pedal stroke. This problem arose when we tested the bicycle on a different bicycle than we had originally designed the device for. This could be accomplished by adjusting the location of the guidance pulley.

To make the device fit properly in the bicycle, it must be reduced in size. By using smaller pulleys in addition to the single custom spring the distance between the two U-channels could be reduced. This would reduce the total height of the device, making it fit better in the available space. It also has the added benefit of covering the mechanisms, making the device safer for the user.

Other improvements to the device go beyond just re-arranging the components. Future work could include an analysis of potential materials to find ones more suited to the desired goal. This would be an improvement over just using materials that were chosen based on cost and availability. Different designs could also be considered. For example, the use of a motor to apply force would not increase the force required from the user at the non-powered portion of the pedal stroke. Another design would be to use a flywheel to store the energy. The wheel could be pre-
charged with a motor in a charging stand. This design would have the advantage of using an external power source without requiring the user to carry the weight of the motor on the bicycle. A more complicated system could be redesigning a regenerative braking system, to harness the energy of the spinning wheel and transmit it to the pedals.

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## Appendix A: Goodman Diagrams







## Appendix B: Force Required to Accelerate Bike



Figure 1: Free Body Diagram of Bicycle
The following calculation will determine the necisary force $F_{c}$ required to be applied at 90 degrees to the crank arm, to achieve a desired acceleration as outlined bellow. The desired acceleration was determined through the use of table 7-1 found in Norton Design of machinery, the value for a normal vehicle acceleration was used.

Where: $L_{c}$ is the length of the crank
$r_{w}$ is the radius of the wheel
f is the friction coefficient between the wheel and the ground
$\mathrm{w}_{\text {bike }}$ is the weight of the bike
$\mathrm{w}_{\text {person }}$ is the weight of the person riding the bike
$w_{\text {device }}$ is the weight of the assisting device
$w_{\text {sys }}$ is the combined weight of the system
$m_{\text {sys }}$ is the mass of the system

## GIVENS::

$\mathrm{L}_{\mathrm{c}}:=\sin \quad \mathrm{r}_{\mathrm{w}}:=13 \mathrm{in} \quad \mathrm{w}_{\text {bike }}:=301 \mathrm{bf} \quad \mathrm{w}_{\text {person }}:=1501 \mathrm{lbf} \quad \mathrm{w}_{\text {device }}:=51 \mathrm{lbf}$
$\mathrm{f}:=.75 \quad \mathrm{w}_{\text {sys }}:=\mathrm{w}_{\text {bike }}+\mathrm{w}_{\text {person }}+\mathrm{w}_{\text {device }}=185 \cdot \mathrm{lbf}$
$m_{\text {sys }}:=\frac{w_{\text {sys }}}{g}=185 \mathrm{lb}$

## KNOWN//ASSUMED VARIABLES::

$$
\begin{aligned}
& \mathrm{G}_{1}:=4 \quad \mathrm{G}_{2}:=6 \\
& \mathrm{a}:=.1 \cdot \mathrm{~g}=3.217 \frac{\mathrm{ft}}{\mathrm{~s}^{2}}
\end{aligned}
$$

Where: $\mathrm{G}_{1}$ is the diameter of the driving gear, attached to the crank $\mathrm{G}_{2}$ is the diameter of the driven gear, attached to the wheel
$\omega_{\text {crank }}$ is the assumed average rotational velocity of the crank
$a$ is the desired acceleration of the system

## CALCULATIONS::

$$
\mathrm{F}_{\mathrm{s}}:=\mathrm{m}_{\mathrm{sys}} \cdot \mathrm{a}=18.5 \cdot \mathrm{lbf} \quad \begin{aligned}
& \mathrm{F}_{\mathrm{s}} \text { is the force required to propell the } \\
& \text { system mass at the desired acceleration }
\end{aligned}
$$

The required reaction force at the wheel $\left(\mathrm{R}_{\mathrm{FW}}\right)$ is equal to the force required to propell the system $\left(F_{s}\right)$. Since the wheel has a friction coefficient less than 1 some of the force produced by the wheel will be lost, thus the wheel must produce a slightly higher force to account for this. Calculating for the output force of the wheel to achieve the desired $\mathrm{R}_{\mathrm{FW}}$ we have:
$\mathrm{F}_{\mathrm{w}}:=\frac{\mathrm{F}_{\mathrm{s}}}{\mathrm{f}}=24.667 \cdot \mathrm{lbf} \quad \mathrm{f}=0.75$

The required force applied 90 degrees to the crank will be dependent on the gear ratio the rider has selected, for our purposes we have assumed the highest gear ratio (biggest gear at the cranks, and smallest gear at the wheel). Calculating for this force we have:

$F_{c}$ is the force required to be applied at 90 degrees to crank, to achieve desired acceleration, dependent on the gear ratio.

We can use this force to determine the appropriate spring constants, and deflections to be used within our design such that we ensure our design will provide the desired acceleration.

## Appendix C: Four-Bar Analysis and Torsion Bar Calculations

KNOWN: Provided with the required force to obtain a desired acceleration (as calculated previously in another document), the length of the bycicle crank and the length of the lever arm used to apply torque to a torsion bar.
FIND:
1.) The required length for the connecting rod, the link connecting the crank are to the lever arm.
2.) Determine the angles $\theta_{2}, \theta_{3}, \theta_{4}$ as functions of the crank angle $\theta_{c}$ 2A.) Determine the transmission angle $\mu$
3.) Determine the force acting along link 3 as a function of the required tangential force $F_{t}$ (previously calculated)

3A.) Determine the maximum and minum force acting along link 3 , and the corresponding crank angle at which these extremes occur
4.) Determine the required angular deflection of the torsion bar to achieve 16 in of linear displacement at the end of the desired lever arm length
5.) Use information found in parts 1-4 combined with an assumed torsion bar length to determine the required diameters of a torsion bar, for a solid circular cross section, and a hollow closed circular cross section.
6.) Use information calculated in part 5 to determine the weight of each torsion bar design

SCHEMATIC: for geometrical analysis:


Figure 1: system Device Modeled as a 4-bar crank-rocker mechanism in an open configuration Where:
$r_{c}$ is the length of the crank on the bike and represents link 2 in a fourbar mechanism $L_{c}$ is the length of the connecting rod and represents link 3 in a fourbar mechanism $L_{A}$ is the length of the leverarm attatched to the torsion bar and represents link 4 in a fourbar mechanism
d is the shortest distance between the the origins $\mathrm{O}_{2}$ and $\mathrm{O}_{4}$ and represents link 1 of a fourbar mechanism
$\theta_{c}$ is the angle of the crank arm, in relation to the $y$-axis, as depectited in figure 1
$\theta_{2}$ is the angle between the positive $\mathrm{x}_{2}{ }^{\text {' axis }}$ and the crank arm (link 2)
$\theta_{3}$ is the angle between the positive $x_{3}$ axis and the connecting rod (link 3 )
$\theta_{4}$ is the angle between the positive $X$-axis and the lever arm (link 4)
$\mathrm{X}_{1}$ represents the distance in the horizontal direction between $\mathrm{O}_{2}$ and $\mathrm{O}_{4}$ $\mathrm{Y}_{1}$ represents the distance in the vertical direction between $\mathrm{O}_{2}$ and $\mathrm{O}_{4}$


Figure 2: Free Body Diagram of Linkage in an open configuration

Where:
$F_{t}$ is the tangential force required to act @90 degrees to the crank to achieve the desired acceleration
$\theta_{x}$ is the angle between the $x_{3}{ }^{\prime}$ axis and $F_{t}$
$\mathrm{F}_{\mathrm{A}}$ is the force that can be applied through the connecting rod (link 3 ) and delivered to the
lever arm (link 4) attached to the torsion bar $\left(\mathrm{O}_{4}\right)$
$\mu$ is the angle between the connecting rod and the leverarm (link 3 and link 4 respectivly), and is refered to as the transmission angle
$\beta$ is the angle between $F_{t}$ and $F_{A}$

GIVEN DATA: for geometrical analysis:
DRIVING VARIABLES::

$$
\mathrm{r}_{\mathrm{c}}:=\sin \quad \mathrm{L}_{\mathrm{A}}:=1 \sin \quad \mathrm{X}_{1}:=30 \mathrm{in} \quad \mathrm{Y}_{1}:=2 \sin \quad \mathrm{~F}_{\mathrm{t}}:=\frac{70}{2} \mathrm{lbf}
$$

$$
\begin{aligned}
\theta c & :=0 . .360 \\
{ }^{\theta} \theta_{\mathrm{c}} & =\frac{2 \pi}{360} \theta \mathrm{c}
\end{aligned}
$$

DRIVEN VARIABLES::

$$
\theta_{2}\left(\theta_{\mathrm{c}}\right):=270 \operatorname{deg}-\theta_{\mathrm{c}} \mathrm{~d}:=\sqrt{\mathrm{X}_{1}^{2}+\mathrm{Y}_{1}^{2}}=41.037 \cdot \mathrm{in} \quad \mathrm{~L}_{\mathrm{c}}:=\sqrt{\left(\mathrm{Y}_{1}-\mathrm{L}_{\mathrm{A}}+\mathrm{r}_{\mathrm{c}}\right)^{2}+\mathrm{X}_{1}^{2}}=34.986 \cdot \mathrm{in}
$$

## EQUATIONS REQUIRED FOR FOUR BAR ANALISYS:

$\mathrm{A}_{\mathrm{x}}\left(\theta_{\mathrm{c}}\right)=\mathrm{r}_{\mathrm{c}} \cdot \cos \left(\theta_{2}\left(\theta_{\mathrm{c}}\right)\right)$

$$
\mathrm{A}_{\mathrm{y}}\left(\theta_{\mathrm{c}}\right):=\mathrm{r}_{\mathrm{c}} \cdot \sin \left(\theta_{2}\left(\theta_{\mathrm{c}}\right)\right)
$$

$S\left(\theta_{c}\right):=\frac{{ }_{\mathrm{r}_{\mathrm{c}}}{ }^{2}-\mathrm{L}_{\mathrm{c}}{ }^{2}+\mathrm{L}_{A}{ }^{2}-\mathrm{d}^{2}}{2 \cdot\left(\mathrm{~A}_{\mathrm{X}}\left(\theta_{\mathrm{c}}\right)-\mathrm{d}\right)}$

$$
P\left(\theta_{c}\right):=\frac{A_{y}\left(\theta_{c}\right)^{2}}{\left(A_{X}\left(\theta_{c}\right)-d\right)^{2}}+1
$$

$$
\mathrm{Q}\left(\theta_{\mathrm{c}}\right):=\frac{2 \cdot \mathrm{~A}_{\mathrm{y}}\left(\theta_{\mathrm{c}}\right) \cdot\left(\mathrm{d}-\mathrm{S}\left(\theta_{\mathrm{c}}\right)\right)}{\mathrm{A}_{\mathrm{x}}\left(\theta_{\mathrm{c}}\right)-\mathrm{d}}
$$

$$
R\left(\theta_{c}\right):=\left(d-S\left(\theta_{c}\right)\right)^{2}-L_{A}{ }^{2}
$$

## ANALISYS OF A FOUR BAR MECHANISM IN AN OPEN CONFIGURATION:

$$
B_{y}\left(\theta_{c}\right):=\frac{-Q\left(\theta_{c}\right)-\sqrt{Q\left(\theta_{c}\right)^{2}-4 \cdot P\left(\theta_{c}\right) \cdot R\left(\theta_{c}\right)}}{2 \cdot P\left(\theta_{c}\right)}
$$

$$
B_{x}\left(\theta_{c}\right):=S\left(\theta_{c}\right)-\frac{2 \cdot A_{y}\left(\theta_{c}\right) \cdot B_{y}\left(\theta_{c}\right)}{2 \cdot\left(A_{x}\left(\theta_{c}\right)-d\right)}
$$

$$
\theta_{3}\left(\theta_{c}\right):=\operatorname{atan}\left(\frac{B_{y}\left(\theta_{c}\right)-A_{y}\left(\theta_{c}\right)}{B_{x}\left(\theta_{c}\right)-A_{x}\left(\theta_{c}\right)}\right)
$$



$$
\theta_{x}\left(\theta_{c}\right):=\left(180 \operatorname{deg}-\theta_{2}\left(\theta_{c}\right)\right)-90 \operatorname{deg}
$$

$$
\mu\left(\theta_{c}\right):=\left|\theta_{3}\left(\theta_{c}\right)-\theta_{4}\left(\theta_{c}\right)\right|
$$

$$
+
$$

$\beta_{2}\left(\theta_{c}\right):=\left|\theta_{x}\left(\theta_{c}\right)-\left|\theta_{3}\left(\theta_{c}\right)\right|\right|$
$F A_{\theta c}:=F_{t} \cdot \cos \left(\beta_{2}\left(\theta_{\theta c}\right)\right)$
these calculations for $\mathrm{F}_{\mathrm{A}}$ show the amount of Force that will need to be transmitted along the conncecting rod ( $\mathrm{L}_{\mathrm{c}}$ from Figure 1.) inorder to generate the $\mathrm{F}_{\mathrm{t}}$, such that the system is capable of achieving the desired acceleration.


Plot 1: The applied force $F_{A}$ acting through link 3, plotted against the crank angle $\theta_{c}$

the max and min functions highlighted in light blue return the maximum and minum forces required through 1 complete rotation of the crank. The coresponding match functions, highlighted in orange, return the index at which these values are found, in this case the index value coresponds to the crank angle $\theta_{\mathrm{c}}$

Calculating the required angular deflection of the torsion bar to achieve the necisary linear displacement of 16 in

$L_{d}$ is the required linear displacement at the end of the lever arm, this is driven by the length of the crank.

$$
\mathrm{L}_{\mathrm{d}}:=16 \mathrm{in}
$$

Linear displacement = 16 in

Figure 3: Schematic for determining torsion bar angular deflection $\theta$, based on linear displacement
using the law of cosines to calculate for $\theta$ given a pre-determined lever arm length we have:
$\theta:=\operatorname{acos}\left(\frac{\mathrm{L}_{\mathrm{A}^{2}}+\mathrm{L}_{\mathrm{A}}{ }^{2}-\mathrm{L}_{\mathrm{d}}{ }^{2}}{2 \cdot \mathrm{~L}_{\mathrm{A}} \cdot \mathrm{L}_{\mathrm{A}}}\right)=52.776 \cdot \operatorname{deg}$
using the law of cosines to calculate the length of the lever arm $\left(L_{1}\right)$ given an angular deflection for the torsion bar
$\mathrm{L}_{\mathrm{arm}}:=22 \mathrm{in}$
$\theta_{\text {torsionBar }}=4.33 \mathrm{deg}$
Given
$\cos \left(\theta_{\text {torsionBar }}\right)=\frac{\mathrm{L}_{\text {arm }}{ }^{2}+\mathrm{L}_{\text {arm }}{ }^{2}-\mathrm{L}_{\mathrm{d}}{ }^{2}}{2 \cdot \mathrm{~L}_{\text {arm }} \cdot \mathrm{L}_{\text {arm }}}$
Find $\left(\mathrm{L}_{\text {arm }}\right)=17.647 \mathrm{ft}$

## TORSION BAR CALCULATIONS:

KNOWN: The transmission angle $\mu$ as calculted above, the force applied through the connecting link (link 3) $F_{A}$ as calculated above. The modulous of rigidity for the proposed material to be used for the torsion bar. The cross sectional geometry of the torsion bar (circular, as outlined above). The desired angular deflection of the torsion bar $\theta$. The equation for angular deflection of a torsion bar.

ASSUME: a length for the torsion bar
FIND: The required diameters of torsion bar, D for a closed circular cross section; $\mathrm{D}_{\mathrm{o}}, \mathrm{d}_{\mathrm{i}}$ for a tubular cross section.

## SCHEMATICS:



Figure 4: Cross Section of Closed Circular Torsion Bar


Figure 5: Cross Section of Tubular Torsion Bar

EQUATION FOR ANGULAR DEFLECTION OF A TORSION BAR::
$\theta=\frac{\mathrm{T} \cdot \mathrm{1}}{\mathrm{J} \cdot \mathrm{G}}$
Where::
$\theta=$ the angular deflection of the torsion bar, for the given lever arm this has been calculated to need to be 54 degrees
$\mathrm{T}=$ the torque applied to the torsion bar
I = the length of the torsion bar from its grounding point to location of applied torque
$J=$ the polar moment of area
$\mathrm{G}=$ modulous of rigidity (a material property)

## VARIABLES:

DEFINED:
The shear modulous of rigidity as obtained from Aerospace Specification Metals Inc. for AISI type 304 Stainless Steel is:

$$
\mathrm{G}_{\text {st } 304}:=86 \mathrm{GPa}
$$

KNOWN:
D : $=\frac{3}{16}$ in
UNDEFINED--VARIABLE GUESSES:
$1_{\mathrm{c}}:=6 \mathrm{in}$
EQUATIONS:

$$
\mathrm{J}_{0}:=\frac{\pi \cdot \mathrm{D}^{4}}{32}
$$

The torque applied to the torsion bar will be the product of the force acting perpendicular to the leverarm (link 4), and the length of the lever arm. Thus we have:
$\mathrm{F}_{\text {TLA }}:=\mathrm{F}_{\max } \cdot \sin \left(\mu\left(\theta_{\mathrm{cMaxF}}\right)\right)=33.859 \mathrm{lbf}$

$$
\mathrm{L}_{\mathrm{A}}=18 \cdot \mathrm{in}
$$

$\mathrm{T}_{1}:=\mathrm{L}_{\mathrm{A}} \cdot \mathrm{F}_{\mathrm{TLA}}=609.459 \cdot \mathrm{lbf} \cdot \mathrm{in}$

Given

$$
\begin{aligned}
& \theta=\frac{\mathrm{T}_{1} \cdot \mathrm{I}_{\mathrm{c}}}{\frac{\pi \cdot \mathrm{D}^{4}}{32} \cdot \mathrm{G}_{\text {st } 304}} \\
& \mathrm{~L}_{0}:=\operatorname{Find}\left(\mathrm{I}_{\mathrm{c}}\right)=2.287 \cdot \mathrm{in}
\end{aligned}
$$

$$
\mathrm{L}_{1}:=\left|\left(\mathrm{L}_{0}\right)\right|=2.287 \cdot \mathrm{in}
$$

Where $L_{1}$ is the recomended length of the torsion bar, for the required torque $T_{1}$ at the given transmission angle $\mu$.

## Tubular Cross Section Torsion Bar Calculations:

The only difference in the calculation of angular deflection for a tubular torsion bar is the equation used for the polar moment of area $(\mathrm{J})$; for a tubular cross section this is, $\mathrm{J}_{\mathrm{t}}:=\frac{\pi \cdot\left(\mathrm{D}_{\mathrm{o}}^{4}-\mathrm{d}_{\mathrm{i}}^{4}\right)^{\text {n }}}{32}$ Solving for $\mathrm{d}_{\mathrm{i}}$ of a tubular cross section we have:

## ASSUMED VARIABLE VALUES:

$D_{0}:=\frac{1}{4}$ in $\quad d_{i}:=0.1940 \mathrm{in}$
$D_{0}$ is the desired outer diameter of the tubular torsion bar, $I_{t}$ represents the length of the tubular cross section torsion bar.
undefined guess value for the inner diameter of the tubular torsion bar:

$$
1_{\mathrm{t}}:=3 \mathrm{in}
$$

Given

$$
\begin{aligned}
& \theta=\frac{\mathrm{T}_{1} \cdot \mathrm{~L}_{\mathrm{t}}}{\frac{\pi \cdot\left(\mathrm{D}_{0}^{4}-\mathrm{d}_{\mathrm{i}}^{4}\right)}{32} \cdot \mathrm{G}_{\mathrm{st} 304}} \\
& \mathrm{~L}_{2}:=\operatorname{Find}\left(\mathrm{L}_{\mathrm{t}}\right)=4.608 \cdot \mathrm{in} \\
& \mathrm{~L}_{3}:=\left|\left(\mathrm{L}_{2}\right)\right|=4.608 \cdot \mathrm{in}
\end{aligned}
$$

$\mathrm{t}_{\text {tube }}:=\left(\mathrm{D}_{\mathrm{o}}-\mathrm{d}_{\mathrm{i}}\right)=0.056 \cdot$ in
where $t_{\text {tube }}$ represents the wall thickness of the tube, and $L_{3}$ represents the required length of the torsion bar to achieve the desired angular deflection.

## Weight Calculations:

Using the information calculated above combined with material property data we can now find the difference in weight between the two torsion bar cross sections.

The weight density as obtained from Aerospace Specification Metals Inc. for AlSI type 304
Stainless Steel is:
$\gamma_{\text {st } 304}:=0.289 \frac{\mathrm{lbf}}{\mathrm{in}^{3}}$

## Closed Circular Cross Section:



$$
\mathrm{V}_{\mathrm{c}}:=\mathrm{A}_{\mathrm{c}} \cdot \mathrm{~L}_{1}=0.063 \cdot \mathrm{in}^{3}
$$

$\mathrm{w}_{\mathrm{c}}:=\mathrm{V}_{\mathrm{c}} \cdot \gamma_{\mathrm{st} 304}=0.018 \cdot \mathrm{lbf}$

Tubular Cross Section

$$
A_{t}:=\frac{\pi \cdot\left(D_{0}^{2}-\mathrm{d}_{\mathrm{i}}^{2}\right)}{4}=0.02 \cdot \mathrm{in}^{2}
$$

$$
\mathrm{V}_{\mathrm{t}}:=\mathrm{A}_{\mathrm{t}} \cdot \mathrm{~L}_{3}=0.09 \cdot \mathrm{in}^{3}
$$

$$
\mathrm{w}_{\mathrm{t}}:=\mathrm{V}_{\mathrm{t}} \cdot \gamma_{\mathrm{st} 304}=0.026 \cdot \mathrm{lbf}
$$

Where A is the cross sectional area of the torsion bar, V represents the vollume of material, and $w$ represents the total weight of the torsion bar. Subscripts ' $c$ ' and ' $t$ ' have been assigned to represent the values calculated for a closed circular cross section and a tubular cross section respectively.

## Appendix D: Torque Required to Lift Dead Weight of Leg

GIVEN: A stroke victom suffering from hemiperises, has trouble completing a bycicle crank cycle, specificily between the angle of 180 degrees and 245 degrees, where 0 degrees is when the crank is in line with the positive Y -Axis (refer to figure 1 for this cordinate system).

FIND: The required assistive torque to aid the victom in completing the crank cycle between the angles of 180 degrees and 245 degrees.

ASSUMPTIONS: 1.) $10 \%$ of the assistive torque will be lost due to friction.
2.) The dead weight of the leg is $17 \%$ of the users weight
3.) The assumed weight of the user is 160 lbf
4.) The $F_{\text {leg }}$ will be considerd as the dead weight of the leg


Figure 1: Free Body Diagram of the Crank
Where:
$\theta_{\mathrm{C}}=$ The angle of the crank
$\beta=$ The angle between the crank and the downward acting force of the leg
$\mathrm{R}_{\mathrm{C}}=$ The Length of the crank
$F_{\text {leg }}=$ The Downward force of the leg
$\mathrm{T}_{\mathrm{in}}=$ The input torque, required to move the bike, generated during the first 180 degrees of the crank cycle.
$T_{r}=$ The reaction torque, equal and opposite to the input torque, is generated during the last
180 degrees of the crank cycle.
$T_{f}=$ The resistance torque caused by friction within the system

## KNOWN:

$w_{\text {person }}:=1601 \mathrm{bf}$
$\mathrm{w}_{\text {leg }}:=.17 \cdot \mathrm{w}_{\text {person }}=27.2 \cdot \mathrm{lbf}$
$\mathrm{R}_{\mathrm{C}}:=\sin$
$F_{\text {leg }}:=w_{\text {leg }}=27.2 \mathrm{lbf} \quad \theta_{\mathrm{c}}:=0 \mathrm{deg}, 1 \mathrm{deg} . .360 \mathrm{deg}$

## CALCULATIONS:

$\beta\left(\theta_{c}\right):=180 \operatorname{deg}-\theta_{c}$
The input and reaction torque can be calculated by multiplying the the perpendicular component of the leg force by the length of the crank. The perpendicular component of the leg force will be represented as $F_{p}$ and can be calculated as:
$F_{p}\left(\theta_{c}\right):=F_{1 \mathrm{eg}} \cdot \cos \left(90 \operatorname{deg}-\beta\left(\theta_{c}\right)\right)$
The torque caused by the weight of the leg can then be calculated for any crank angle $\theta_{\mathrm{c}}$ as:
$\mathrm{T}_{\mathrm{in}}\left(\theta_{\mathrm{c}}\right):=\mathrm{F}_{\mathrm{p}}\left(\theta_{\mathrm{c}}\right) \cdot \mathrm{R}_{\mathrm{C}}$


## Crank Angle (Radians)

Plot 1: The Torque caused by the weight of the leg through one rotation of the crank
The maximum torques will be caused when the force of the leg acts perpendicularly to the crank, thus the maximum torques will be:

$$
\begin{array}{ll}
\mathrm{T}_{\max }:=\mathrm{T}_{\mathrm{in}}(90 \mathrm{deg}) & \mathrm{T}_{\min }:=\mathrm{T}_{\mathrm{in}}(270 \mathrm{deg}) \\
\mathrm{T}_{\max }=217.6 \cdot \mathrm{lbf} \cdot \mathrm{in} & \mathrm{~T}_{\min }=-217.6 \cdot \mathrm{lbf} \cdot \mathrm{in}
\end{array}
$$

The above torques were calculated without considering the friction assumption, takeing assumption 1 into account we have:
$\mathrm{T}_{\mathrm{f}}:=.1 \cdot \mathrm{~T}_{\max }=21.76 \cdot \mathrm{lbf} \cdot \mathrm{in}$
where $T_{f}$ in this case is the maximum frictional torque experienced through the crankcycle, to design a device that will assist the user in lifting the dead weight of their leg the device will need to supply a torque capable of overcoming this frictional torque, thus we have:
$\mathrm{T}_{\text {actual }}:=\mathrm{T}_{\text {max }}+\mathrm{T}_{\mathrm{f}}=239.36 \cdot \mathrm{lbf} \cdot$ in

Since the constraints of the problem state that the range in which aid needs to be supplied is between 180 and 245 degrees, these maximum torque values lie outside of the desired crank angle range. We will now consider the crank angle range we are attempting to aid the user with, the maximum torque requried in our range will occure at 245 degrees, thus we have:
$T_{\text {rangeMAX }}:=T_{\text {in }}(245 \mathrm{deg})$
$\mathrm{T}_{\text {rangeMAX }}=-197.213 \cdot \mathrm{lbf} \cdot \mathrm{in}$
$\mathrm{T}_{\text {fRANGE }}:=.1 \cdot \mathrm{~T}_{\text {rangeMAX }}=-19.721 \cdot \mathrm{lbf} \cdot \mathrm{in}$
$\mathrm{T}_{\text {actualRANGE }}:=\mathrm{T}_{\text {rangeMAX }}+\mathrm{T}_{\text {fRANGE }}=-216.934 \cdot \mathrm{lbf} \cdot \mathrm{in}$
That is that the maximum torque our device will need to supply to the crank will be approximatly $217 \mathrm{lbft}^{*}$ in. Through supplying this torque to the crank, the bike will be able to maintain constant velocity, during the section of pedal stroke that the user is unable to supply a force.

## Appendix E: Pulley Design Analysis

GIVEN: The mechanism depicted in figure 1, a pully diameter of 2.5 inches, and a desired torque at the crank of 217 lbft in

FIND: The force required from the spring to provide the desired torque about the crank
ASSUMPTIONS: 1.) $10 \%$ of the spring force will be lost due to friction


Figure 1: Depiction of Mechanism on Bike
Where:
-The Purple Lines represent a continuous cable grounded at $\mathrm{O}_{1}$, and connected to the bike pedal at point A.
-The green tension springs provide the force in the system, and is grounded at $\mathrm{O}_{2}$
-Pulley System 1 serves to decrease the linear displacement needed by the tension spring to obtain the necisary 16 inches cable displacement
-Pulley 2 represents a guidance pulley with a diameter of 2.5 inches used to redirect the cable to the pedal
-Point A represents the point at which the cable attaches to the pedal
$-\mathrm{O}_{3}$ represents the axis of rotation for the bycicle crank, and origin of the global position axis


Figure 2: Length variables of mechanism

Where:
$r_{\mathrm{c}}=$ The length of the pedal crank
$\mathrm{Lc}_{3}=$ The length of cable measured from the center of roller 1 to the center of the guidance pulley (pulley 2)
$\mathrm{Lc}_{4}=$ The length of cable from the center of the guidance pulley (pulley 2) to the attachment point on the pedal (point A)
$L_{h}=$ The length of the housing for the spring pulley mechanism, from where the spring is grounded at $\mathrm{O}_{2}$ to the center of roller 1 .
$D_{\text {pully }}=$ The diameter of the guidence pully (pulley 2)


Figure 3: Isolated Mechanism, with Relevent Angles
Where:
$\theta_{c}=$ The angle of the pedal crank
$\theta_{2}=$ The angle of link $2\left(r_{d}\right)$ from the $x$-axis
$\theta_{4}=$ The angle of link 5 from the $x^{\prime}$-axis
$\mu=$ The transmission angle between link 2 and link 3
$Y_{1}=$ The vertical offset from $\mathrm{O}_{2}$ to the center of the guidence pully
$\mathrm{X}_{1}=$ The horizontal offset of the guidence pully
$\mathrm{Y}_{2}=$ The vertical offset of $\mathrm{O}_{4}$ from $\mathrm{O}_{2}$
$\mathrm{X}_{2}=$ The horizontal offset of $\mathrm{O}_{4}$ from $\mathrm{O}_{2}$
$\mathrm{O}_{3}=$ The center of rotation of the pedal crank
$\mathrm{O}_{2}=$ The point at which the spring is grounded
$\mathrm{O}_{1}=$ The point at which the cable is grounded

## POSITION ANALYSIS

## KNOWN VARIABLES:

$\mathrm{r}_{\mathrm{c}}:=\sin \quad \mathrm{X}_{1}:=4 \mathrm{in} \quad \mathrm{Y}_{1}:=20 \mathrm{in} \quad \mathrm{X}_{2}:=24 \mathrm{in} \quad \mathrm{Y}_{2}:=22$ in

$$
\begin{array}{lll}
x_{h}:=\sin & D_{\text {pully }}:=2.5 \text { in } & \\
& { }^{r_{p}}:=\frac{D_{\text {pully }}}{2} & \theta c:=0 . .360 \\
& \theta_{\theta c}:=\frac{2 \pi}{360} \theta c
\end{array}
$$

## CALCULATIONS:

To begin we will create a function to find $\theta_{2}$ for a given $\theta_{\mathrm{c}}$ :
$\theta_{2}\left(\theta_{c}\right):=\theta_{c}-90 \mathrm{deg}$
Now we will calculate $\theta_{4}$, since ${L c_{3}}$ will remain the same length this can be calculated using the pythagorean therom, in conjuntion with a sine or cosine function.
$L_{5}:=\sqrt{\left(\mathrm{X}_{1}+\mathrm{X}_{2}-\mathrm{x}_{\mathrm{h}}\right)^{2}+\left[\mathrm{Y}_{2}-\left(\mathrm{Y}_{1}+\mathrm{r}_{\mathrm{p}}\right)\right]^{2}}$
$\theta_{4}:=\operatorname{asin}\left[\frac{\left[Y_{2}-\left(Y_{1}+r_{p}\right)\right]}{L_{5}}\right]=2.148 \cdot \operatorname{deg}$
and now solving for the $x$ and $y$ cordinates of joint $A$ we have:
$A_{X}\left(\theta_{c}\right):=r_{c} \cdot \cos \left(\theta_{2}\left(\theta_{c}\right)\right)$
$A_{y}\left(\theta_{c}\right):=r_{c} \cdot \sin \left(\theta_{2}\left(\theta_{c}\right)\right)$

In order to calulate the required force of the spring we will need to know the transmission angle $\mu$, to find this we can use the law of cosines, refer to figure 4 below for a depiction of the triangle we will use for this calculation, it is importnat to note that side C of this triangle is not part of the mechanism itself, but rather a distance between $\mathrm{O}_{2}$ and and the guidance pulley.


Figure: 4: The triangle for use with the law of cosines

Side C can be approximated as:
$\mathrm{C}=\sqrt{\left(\mathrm{X}_{1}+\mathrm{r}_{\mathrm{p}}\right)^{2}+\mathrm{Y}_{1}{ }^{2}}$
for any angle $\theta_{c}$ the side length $B$ can be approximated as:
$B\left(\theta_{c}\right):=\sqrt{\left(X_{1}+r_{p}+A_{x}\left(\theta_{c}\right)\right)^{2}+\left(Y_{1}+A_{y}\left(\theta_{c}\right)\right)^{2}}$
Side $A$ is the crank and thus has a length of $r_{c}=8$ in
$A:=r_{c}=8$ in
and now using the law of cosines we can calculate the angle $\mu$ for any given crank angle $\theta_{c}$ $\mu\left(\theta_{c}\right)=\operatorname{acos}\left(\frac{A^{2}+B\left(\theta_{c}\right)^{2}-C^{2}}{2 \cdot A \cdot B\left(\theta_{c}\right)}\right)$


Figure 4: Representation of relevent varibles for force calculations
Where:
$\mathrm{F}_{\mathrm{s}}=$ The total force of the spring system
$F_{1}=$ The Force acting through the cable due to the spring force
$F_{p}=$ The perpendicular force component of $F_{1}$, acting perpendicular to the crank at point $A$
$T_{1}=$ The required torque to rotate the crank with the dead weight of the users leg through the desired aid angle
$\beta=$ the angle between the applied force $F_{1}$ and its perpendicular component $F_{p}$
$\mu=$ the transmission angle between the crank and the attached cable
$\mathrm{O}_{1}=$ The axis of rotation for the crank

KNOWN:
$\mathrm{T}_{1}:=217 \mathrm{lbf} \cdot \mathrm{in} \quad \mathrm{r}_{\mathrm{c}}=8 \cdot \mathrm{in}$
To calculate the required force $F_{1}$ we must first devolope a function for the angle $\beta$ for any crank angle $\theta_{c}$, thus we have:
$\beta\left(\theta_{c}\right):=90 \operatorname{deg}-\mu\left(\theta_{c}\right)$
Now using the required torque that was calculated in previous analysis, we can determine the force $F_{1}$ required to act through the cable.
$\mathrm{F}_{\theta_{\mathrm{c}}}:=\frac{\mathrm{T}_{1}}{\mathrm{r}_{\mathrm{c}}} \cdot \cos \left(\beta\left(\theta_{\theta c}\right)\right)$


## Crank Angle (Radians)

Plot 1: Force Acting on Pedal Through Crank Cycle
$\mathrm{F}_{1 \mathrm{MAX}}:=\max (\mathrm{F} 1)=27.125 \cdot \mathrm{lbf}$
${ }_{\mathrm{C}} \mathrm{MaxF}:=\operatorname{match}(\max (\mathrm{F} 1), \mathrm{F} 1)=(278)$
if we aproximate a $10 \%$ force loss due to friction, and consider that pulley 1 depicted in figure 1 will divide the supplied spring force equally into the four cable sections we can determine the necisary spring force as:
$\mathrm{F}_{\text {friction }}:=.1 \cdot \mathrm{~F}_{1 \mathrm{MAX}}=2.712 \cdot \mathrm{lbf}$
$F_{\text {spring }}:=4 \cdot\left(\mathrm{~F}_{\text {friction }}+\mathrm{F}_{1 \mathrm{MAX}}\right)=119.35 \cdot \mathrm{lbf}$

## Appendix F: Interpolations for Determining Stress Concentration Factors

DETERMINING THE A VALUE FOR THE TORSIONAL GEOMETRIC STRESS CONCENTRATION FACTOR:

$$
\mathrm{AT}:=\left(\begin{array}{l}
.86331 \\
.84897 \\
.83425 \\
.90337
\end{array}\right) \quad \mathrm{D}:=\left(\begin{array}{cccc}
2^{3} & 2^{2} & 2 & 1 \\
1.33^{3} & 1.33^{2} & 1.33 & 1 \\
1.20^{3} & 1.20^{2} & 1.20 & 1 \\
1.09^{3} & 1.09^{2} & 1.09 & 1
\end{array}\right)
$$

$\mathrm{D} 11:=\mathrm{D}^{\mathrm{T}} \cdot \mathrm{D}=\left(\begin{array}{cccc}74.198 & 40.189 & 22.614 & 13.376 \\ 40.189 & 22.614 & 13.376 & 8.397 \\ 22.614 & 13.376 & 8.397 & 5.62 \\ 13.376 & 8.397 & 5.62 & 4\end{array}\right)$
$\mathrm{A} 11:=\mathrm{D}^{\mathrm{T}} \cdot \mathrm{AT}$
$\mathrm{Ut}:=\mathrm{D} 11^{-1} \cdot \mathrm{~A} 11 \quad \mathrm{Ut}=\left(\begin{array}{c}-3.522 \\ 15.839 \\ -23.037 \\ 11.756\end{array}\right)$
this is the polynomial we will use to calculate the 'A' value needed:

$$
\operatorname{At}(\mathrm{x}):=U \mathrm{t}_{0} \cdot \mathrm{x}^{3}+U \mathrm{t}_{1} \cdot \mathrm{x}^{2}+U t_{2} \cdot \mathrm{x}+U \mathrm{t}_{3}
$$

$$
A_{t}:=\operatorname{At}(6.18869)=-358.934
$$

where:
$\mathrm{Ut}_{0}=-3.522$
$\mathrm{Ut}_{1}=15.839$
$\mathrm{Ut}_{2}=-23.037$
$\mathrm{Ut}_{3}=11.756$

DETERMINING THE 'b' VALUE FOR THE TORSIONAL GEOMETRIC STRESS CONCENTRATION FACTOR:

$$
\begin{array}{rl}
\mathrm{B}:=\left(\begin{array}{l}
-.23865 \\
-.23161 \\
-.21649 \\
-.12692
\end{array}\right) & \mathrm{D}:=\left(\begin{array}{cccc}
2^{3} & 2^{2} & 2 & 1 \\
1.33^{3} & 1.33^{2} & 1.33 & 1 \\
1.20^{3} & 1.20^{2} & 1.20 & 1 \\
1.09^{3} & 1.09^{2} & 1.09 & 1
\end{array}\right) \\
\mathrm{D} 1:=\mathrm{D}^{\mathrm{T}} \cdot \mathrm{D} \\
\mathrm{~B} 1:=\mathrm{D}^{\mathrm{T}} \cdot \mathrm{~B} & \\
\mathrm{Utb}:=\mathrm{D}^{-1} \cdot \mathrm{~B} 1 & \mathrm{Utb}=\left(\begin{array}{c}
-3.05 \\
13.951 \\
-20.755 \\
9.871
\end{array}\right)
\end{array}
$$

this is the polynomial we will use to calculate the b value for any $\mathrm{D} / \mathrm{d}$ ratio:

$$
\mathrm{bt}(\mathrm{x}):=\mathrm{Utb} \cdot \mathrm{X}^{3}+\mathrm{Utb}_{1} \cdot \mathrm{x}^{2}+\mathrm{Utb}_{2} \cdot \mathrm{x}+\mathrm{Utb}_{3}
$$

where:
$\mathrm{Utb}_{0}=-3.05$
$\mathrm{Utb}_{1}=13.951$
$\mathrm{Utb}_{2}=-20.755$
$\mathrm{Utb}_{3}=9.871$
now calculating the neuber constant to find the notch sensitivity $q$ : (for steels, Data from PG. 378 of Machine Design Text)
Sut $:=\left(\begin{array}{c}50 \\ 55 \\ 60 \\ 70 \\ 80 \\ 90 \\ 100 \\ 110 \\ 120 \\ 130 \\ 140 \\ 160 \\ 180 \\ 200 \\ 220 \\ 240\end{array}\right) \quad$ Neub $:=\left(\begin{array}{c}0.130 \\ 0.118 \\ 0.108 \\ 0.093 \\ 0.055 \\ 0.049 \\ 0.080 \\ 0.070 \\ 0.062 \\ 0.039 \\ 0.0 .031 \\ 0.024 \\ 0.018 \\ 0.013 \\ 0.009\end{array}\right)$

$$
\text { guess }:=\left(\begin{array}{c}
0.01 \\
1 \\
1 \\
1
\end{array}\right)
$$

Neub $=\mathbf{f}(\mathrm{Sut}, \mathrm{C} 3, \mathrm{C} 2, \mathrm{C} 1, \mathrm{C} 0)$
$\mathrm{f}(\mathrm{x}, \mathrm{C} 3, \mathrm{C} 2, \mathrm{C} 1, \mathrm{C} 0): \mathrm{C} 3 \cdot \mathrm{x}^{3}+\mathrm{C} 2 \cdot \mathrm{x}^{2}+\mathrm{C} 1 \cdot \mathrm{x}+\mathrm{C} 0$
$\mathrm{C} 3:=$ guess $_{0}$
$C 2:=$ guess $_{1}$
$\mathrm{C} 1:=$ guess $_{2}$
$\mathrm{C} 0:=$ guess $_{3}$
sol $:=$ genfit(Sut,Neub, guess,f) $=\left(\begin{array}{c}-2.67 \times 10^{-8} \\ 1.509 \times 10^{-5} \\ -3.078 \times 10^{-3} \\ 0.246\end{array}\right)$

$$
\begin{aligned}
\mathrm{C} 33 & =\mathrm{sol}_{0} \\
\mathrm{C} 22 & =\mathrm{sol}_{1} \\
\mathrm{C} 11 & =\mathrm{sol}_{2} \\
\mathrm{C} 00 & =\mathrm{sol}_{3}
\end{aligned}
$$



Ultimate Tensile Strength (ksi)
this evaluates the function for a ultimate tensile strength of 185 ksi

```
neub1 := f(185,C33,C22,C11,C00)=0.024
```

now calculating the neuber constant to find the notch sensitivity $q$ : (for Hardened Aluminum Data from PG. 378 of Machine Design
Text)


Neub $=\mathrm{f}(\mathrm{Sut}, \mathrm{C} 3, \mathrm{C} 2, \mathrm{C} 1, \mathrm{C} 0)$
$\mathrm{f}(\mathrm{x}, \mathrm{C} 3, \mathrm{C} 2, \mathrm{C} 1, \mathrm{C} 0):=\mathrm{C} 3 \cdot \mathrm{x}^{3}+\mathrm{C} 2 \cdot \mathrm{x}^{2}+\mathrm{C} 1 \cdot \mathrm{x}+\mathrm{C} 0$

C3 $=$ guess ${ }_{0}$
$C_{2}:=$ guess $_{1}$
$\mathrm{C} 1:=$ guess $_{2}$
$\mathrm{CO}=$ guess $_{3}$
sol $:=\operatorname{genfit}\left(\right.$ Sut, Neub, guess,f) $=\left(\begin{array}{c}-1.69 \times 10^{-6} \\ 3.508 \times 10^{-4} \\ -0.025 \\ 0.768\end{array}\right)$

$$
\begin{aligned}
& \mathrm{C} 33:=\mathrm{sol}_{0} \\
& \mathrm{C} 22:=\mathrm{sol}_{1} \\
& \mathrm{C} 11:=\mathrm{sol}_{2} \\
& \mathrm{COO}:=\mathrm{sol}_{3}
\end{aligned}
$$



Ultimate Tensile Strength (ksi)
this evaluates the function for a ultimate tensile strength of 185 ksi

$$
\text { neub2 }:=\mathrm{f}(83, \mathrm{C} 33, \mathrm{C} 22, \mathrm{C} 11, \mathrm{C} 00)=0.134
$$

now calculating the neuber constant to find the notch sensitivity $q$ : (for Annealed Aluminum Data from PG. 378 of Machine Design Text)

$$
\text { Sut }:\left(\begin{array}{l}
10 \\
15 \\
20 \\
25 \\
30 \\
35 \\
40 \\
45
\end{array}\right)
$$

$$
\text { Neub }:=\left(\begin{array}{l}
0.500 \\
0.341 \\
0.264 \\
0.217 \\
0.180 \\
0.152 \\
0.126 \\
0.111
\end{array}\right)
$$

$$
\text { guess }:=\left(\begin{array}{c}
0.01 \\
1 \\
1 \\
1
\end{array}\right)
$$

$$
\text { Neub }=\mathrm{f}(\mathrm{Sut}, \mathrm{C} 3, \mathrm{C} 2, \mathrm{C} 1, \mathrm{C} 0)
$$

$$
\mathrm{f}(\mathrm{x}, \mathrm{C} 3, \mathrm{C} 2, \mathrm{C} 1, \mathrm{C} 0):=\mathrm{C} 3 \cdot \mathrm{x}^{3}+\mathrm{C} 2 \cdot \mathrm{x}^{2}+\mathrm{C} 1 \cdot \mathrm{x}+\mathrm{C} 0
$$

$$
\text { C3 }=\text { guess }_{0}
$$

$$
\mathrm{C}_{2}:=\text { guess }_{1}
$$

$$
\mathrm{Cl}_{1}=\text { guess }_{2}
$$

$$
\mathrm{Co}=\text { guess }_{3}
$$

$$
\text { sol : }:=\text { genfit(Sut,Neub, guess,f })=\left(\begin{array}{c}
-1.521 \times 10^{-5} \\
1.615 \times 10^{-3} \\
-0.061 \\
0.954
\end{array}\right)
$$

$$
\begin{aligned}
& \mathrm{C} 33^{\mathrm{N}:=\mathrm{sol}_{0}} \\
& \mathrm{C} 22:=\mathrm{sol}_{1} \\
& \mathrm{C} 11:=\mathrm{sol}_{2} \\
& \mathrm{C} 1
\end{aligned}
$$



Ultimate Tensile Strength (ksi)
this evaluates the function for a ultimate tensile strength of 185 ksi neub3 : $=\mathrm{f}(43, \mathrm{C} 33, \mathrm{C} 22, \mathrm{C} 11, \mathrm{C} 00)=0.12$

## Appendix G: Guidance Pulley Mounting Plate Tear-Out Analysis

## Guidance Pulley Mounting Plate, TEAR-OUT ANALYSIS:

GIVEN: The Provided mounting plate design, and the forces induced on the guidance pulley in the pulley mechanism design.

FIND: 1.) The minimum wall thickness for mounting holes to design against failure due to tear-out
2.) The weight of the plate

ASSUMPTIONS: 1.) The material of the plate is acrylic


Figure 1: Part Model of Mounting Plate with Aircraft Clamps in Place
Where: The aircraft clamps will be clamped to the rear triangle of the bycicle, and the guidance pulley will be mounted in the four mounting holes.

Before we can begin our tearout analysis we must first determin the forces that the mounting bracket will be subjected to, refer to figure 2 below for a visual representation of these forces.


Figure 2: Forces acting on pulley
Where:
$\mathrm{F}_{1}=$ the tension force acting through the cable as a result of the spring force
$\mathrm{Fx}_{\mathrm{t}}=$ the total force acting in the x direction
$\mathrm{Fy}_{\mathrm{t}}=$ the total force acting in the y direction
$\theta_{3}=$ the angle between the $x$-axis and the force through the cable between the pulley and
the crank
$\theta_{4}=$ the angle between the $x$-axis and the cable running from the guidance pulley to the
spring housing

## KNOWN VARIABLES:

$\mathrm{F}_{1}:=27.5 \mathrm{lbf}$
$\theta_{4}:=2.148 \mathrm{deg}$

## CALCULATIONS:

## $X$ and $Y$ components of Forces

$\mathrm{Fx}_{4}:=\mathrm{F}_{1} \cdot \cos \left(\theta_{4}\right)=27.481 \cdot \mathrm{lbf}$
$\mathrm{Fy}_{4}:=\mathrm{F}_{1} \cdot \sin \left(\theta_{4}\right)=1.031 \cdot \mathrm{lbf}$

To calculate $\theta_{3}$ we need to determine the position of the crank for the instance in which the most force will be applied through the cable, this will occur at the crank angle at which the crank is inline with the cable, at this point the spring will be at its maximum extension, and thus exerting the maximum amount of force through the cable.
$X_{1}:=4 \mathrm{in}$
$\mathrm{Y}_{1}:=20 \mathrm{in}$
$D_{p}:=2.117 \mathrm{in}$

$$
\mathrm{r}_{\mathrm{p}}:=\frac{\mathrm{D}_{\mathrm{p}}}{2}
$$

Adj $:=X_{1}+r_{p}$
opp $:=Y_{1}$
$\theta_{3}:=\operatorname{atan}\left(\frac{\text { opp }}{\text { Adj }}\right)=75.806 \cdot \operatorname{deg}$
$\mathrm{Fx}_{3}:=\mathrm{F}_{1} \cdot \cos \left(\theta_{3}\right)=6.743 \cdot \mathrm{lbf}$
$\mathrm{Fy}_{3}:=\mathrm{F}_{1} \cdot \sin \left(\theta_{3}\right)=26.66 \cdot \mathrm{lbf}$
since both instances of the $F_{1}$ force act in the same $x$-direction they can be summed to find the total x -component force acting on the pulley:
$\mathrm{Fx}_{\mathrm{t}}:=\mathrm{Fx}_{3}+\mathrm{Fx}_{4}=34.224 \cdot \mathrm{lbf}$
since the two instances of the $\mathrm{F}_{1}$ force are acting in opposite y -directions, $\mathrm{Fy}_{3}$ must be subtracted from $\mathrm{Fy}_{4}$.
$\mathrm{Fy}_{\mathrm{t}}:=\mathrm{Fy}_{4}-\mathrm{Fy}_{3}=-25.63 \cdot \mathrm{lbf} \quad+$
the negetave indicates that the total $y$-force will be acting in the downward direction.
These forces act at the pulley center of rotation, and can be considard as torques acting about each mounting hole. These torques will then cause forces on the aircraft clamp holes, see figure 3 below:


Figure 3: Representation of Forces and Pulley Geometry.

Where: $P_{c}=$ The pulley center of rotation
$x=$ The horizontal distance from $P_{c}$ to pulley mounting holes 1 and 4
(represented as $T_{1}$ and $T_{4}$ )
$\mathrm{xx}=$ The horizontal distance from $\mathrm{P}_{\mathrm{c}}$ to pulley mounting holes 2 and 3
$y=$ The vertical distance from $P_{c}$ to the pulley mounting holes
$T_{1}=$ The torque caused about pulley mounting hole 1.
$\mathrm{T}_{2}=$ The torque caused about pulley mounting hole 2 .
$\mathrm{T}_{3}=$ The torque caused about pulley mounting hole 3 .
$\mathrm{T}_{4}=$ The torque caused about pulley mounting hole 4.
$\mathrm{F}_{\mathrm{x} 4}=$ The x component of force acting at bracket mounting hole 4 .
$\mathrm{F}_{\mathrm{y} 4}=$ The y component of force acting at bracket mounting hole 4.
$\mathrm{Fx}_{4}=$ The force acting paralell to right edge of mounting plate.
$\mathrm{Fy}_{4}{ }^{4}=$ The force acting perpendicular to right edge of plate.
The bracket mounting holes are labled sequentially in a counter-clockwise direction. Holes 3 and 4 have similar force lables, while holes 1 and 2 only have x and y components labled. This is due to the orientation of the holes and the force components we will be considering. The force labels at each hole represent the same information displayed above for hole 4, according to the holes appropriate subscripts.


Figure 4: Length Variables for Mounting Plate.

Where: $\mathrm{X}_{11}=$ The horizontal distance from aircraft clamp hole 1 to the right set of pulley mounting holes.
$\mathrm{X}_{12}=$ The horizontal distance from aircraft clamp hole 1 to the left set of pulley mounting holes
$X_{21}=$ The horizontal distance from the center of aircraft clamp hole 2 to the right set of pulley mounting holes.
$X_{22}=$ The horizontal distance from the center of aircraft clamp hole 2 to the left set of pulley mounting holes
$X_{31}=$ The horizontal distance from the center of aircraft clamp hole 3 to the right set of pulley mounting holes
$X_{32}=$ The horizontal distance from the center of aircraft clamp hole 3 to the left set of pulley mounting holes
$X_{41}=$ The horizontal distance from the center of aircraft clamp hole 4 to the right set of pulley mounting holes
$X_{42}=$ The horizontal distance from the center of aircraft clamp hole 4 to the left set of pulley mounting holes
$Y_{11}=$ The vertical distance from the center of aircraft clamp holes 1 and 2 to the center of the upper set of pulley mounting holes
$Y_{12}=$ The vertical distance from the center of aircraft clamp hole 1 and 2 to the center of the lower set of pulley mounting holes
$Y_{31}=$ The vertical distance from the center of aircraft clamp hole 3 to the center of the upper set of pulley mounting holes
$Y_{32}=$ The vertical distance from the center of aircraft clamp hole 3 to the center of the lower set of pulley mounting holes
$Y_{41}=$ The vertical distance from the center of aircraft clamp hole 4 to the center of the upper set of pulley mounting holes
$Y_{42}=$ The vertical distance from the center of aircraft clamp hole 4 to the center of the lower set of pulley mounting holes

## GIVENS FOR TEAR-OUT:

| $\mathrm{x}_{11}:=2.62 \mathrm{in} \quad \mathrm{x}_{2}$ | $\mathrm{x}_{21}:=2.35 \mathrm{in}$ | $\mathrm{x}_{31}:=2.99 \mathrm{in}$ | $\mathrm{x}_{41}:=0.2 \mathrm{in}$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{x}_{12}:=2.06 \mathrm{in} \quad \mathrm{x}_{2}$ | $\mathrm{x}_{22}:=2.92 \mathrm{in}$ | $\mathrm{x}_{32}:=3.56 \mathrm{in}$ | $\mathrm{x}_{42}:=0.37 \mathrm{in}$ |
| $\mathrm{y}_{11}:=5.28 \mathrm{in}$ |  | $\mathrm{y}_{31}:=4.1 \mathrm{in}$ | $\mathrm{y}_{41}:=1.22 \mathrm{in}$ |
| $\mathrm{y}_{12}:=1.73 \mathrm{in}$ |  | $\mathrm{y}_{32}:=0.75 \mathrm{in}$ | $\mathrm{y}_{42}:=4.77 \mathrm{in}$ |
| $\mathrm{y}:=\frac{3.55}{2} \mathrm{in}=0.045 \mathrm{~m}$ |  | $\begin{aligned} & =1.242 \mathrm{in}-.25 \\ & =\mathrm{xx}-.57 \mathrm{in}=0 . \end{aligned}$ | $.987 \cdot \mathrm{in}$ |
| $\mathrm{Fy}_{\mathrm{t}}=-25.63 \cdot \mathrm{lbf}$ | $\mathrm{Fx}_{\mathrm{t}}=3$ |  |  |

TORQUE CALCULATION ON MOUNTING HOLES:
$\mathrm{T}_{1 \mathrm{x}}:=\mathrm{Fx}_{\mathrm{t}} \cdot \mathrm{y}=60.747 \cdot \mathrm{lbf} \cdot \mathrm{in}$
$\mathrm{T}_{1 \mathrm{y}}:=\mathrm{Fy}_{\mathrm{t}} \cdot \mathrm{x}=-10.688 \cdot \mathrm{lbf} \cdot \mathrm{in}$
$\mathrm{T}_{1}:=\mathrm{T}_{1 \mathrm{x}}+\mathrm{T}_{1 \mathrm{y}}=50.06 \cdot \mathrm{lbf} \cdot \mathrm{in}$

$$
\begin{gathered}
\mathrm{T}_{2 \mathrm{x}}:=\mathrm{Fx}_{\mathrm{t}} \cdot \mathrm{y}=60.747 \cdot \mathrm{lbf} \cdot \mathrm{in} \quad \mathrm{~T}_{2 \mathrm{y}}:=\mathrm{Fy}_{\mathrm{t}} \cdot \mathrm{xx}=-25.297 \cdot \mathrm{lbf} \cdot \mathrm{in} \\
\mathrm{~T}_{2}:=\mathrm{T}_{2 \mathrm{x}}+\mathrm{T}_{2 \mathrm{y}}=35.451 \cdot \mathrm{lbf} \cdot \mathrm{in}
\end{gathered}
$$

$\mathrm{T}_{3 \mathrm{x}}:=\mathrm{Fx}_{\mathrm{t}}-\mathrm{y}=-60.747 \cdot \mathrm{lbf} \cdot \mathrm{in} \quad \quad \mathrm{T}_{3 \mathrm{y}}:=\mathrm{Fy}_{\mathrm{t}} \cdot \mathrm{xx}=-25.297 \cdot \mathrm{lbf} \cdot \mathrm{in}$
$\mathrm{T}_{3}:=\mathrm{T}_{3 \mathrm{x}}+\mathrm{T}_{3 \mathrm{y}}=-86.044 \cdot \mathrm{lbf} \cdot \mathrm{in}$

$$
\mathrm{T}_{4 \mathrm{x}}:=\mathrm{Fx}_{\mathrm{t}}-\mathrm{y}=-60.747 \cdot \mathrm{lbf} \cdot \mathrm{in} \quad \mathrm{~T}_{4 \mathrm{y}}:=\mathrm{Fy}_{\mathrm{t}} \cdot \mathrm{x}=-10.688 \cdot \mathrm{lbf} \cdot \mathrm{in}
$$

$$
\mathrm{T}_{4}:=\mathrm{T}_{4 \mathrm{x}}+\mathrm{T}_{4 \mathrm{y}}=-71.435 \cdot \mathrm{lbf} \cdot \mathrm{in}
$$

FORCES ACTING ON AIRCRAFT CLAMP MOUNTING HOLES:
FOR AIRCRAFT CLAMP 1:

$$
\begin{aligned}
& \mathrm{F}_{\mathrm{y} 1}:=\frac{\mathrm{T}_{1}}{\mathrm{x}_{11}}+\frac{\mathrm{T}_{2}}{\mathrm{x}_{12}}+\frac{\mathrm{T}_{3}}{\mathrm{x}_{12}}+\frac{\mathrm{T}_{4}}{\mathrm{x}_{11}}=-32.718 \cdot \mathrm{lbf} \\
& \mathrm{~F}_{\mathrm{x} 1}:=\frac{\mathrm{T}_{1}}{\mathrm{y}_{11}}+\frac{\mathrm{T}_{2}}{\mathrm{y}_{11}}+\frac{\mathrm{T}_{3}}{\mathrm{y}_{12}}+\frac{\mathrm{T}_{4}}{\mathrm{y}_{12}}=-74.833 \cdot \mathrm{lbf}
\end{aligned}
$$

FOR AIRCRAFT CLAMP 2:

$$
\begin{aligned}
& \mathrm{F}_{\mathrm{y} 2}:=\frac{\mathrm{T}_{1}}{\mathrm{x}_{21}}+\frac{\mathrm{T}_{2}}{\mathrm{x}_{22}}+\frac{\mathrm{T}_{3}}{\mathrm{x}_{22}}+\frac{\mathrm{T}_{4}}{\mathrm{x}_{21}}=-26.422 \cdot \mathrm{lbf} \\
& \mathrm{~F}_{\mathrm{x} 2}:=\frac{\mathrm{T}_{1}}{\mathrm{y}_{11}}+\frac{\mathrm{T}_{2}}{\mathrm{y}_{11}}+\frac{\mathrm{T}_{3}}{\mathrm{y}_{12}}+\frac{\mathrm{T}_{4}}{\mathrm{y}_{12}}=-74.833 \cdot \mathrm{lbf}
\end{aligned}
$$

## FOR AIRCRAFT CLAMP 3:

$$
\begin{aligned}
& \mathrm{F}_{\mathrm{y} 3}:=\frac{\mathrm{T}_{1}}{\mathrm{x}_{31}}+\frac{\mathrm{T}_{2}}{\mathrm{x}_{32}}+\frac{\mathrm{T}_{3}}{\mathrm{x}_{32}}+\frac{\mathrm{T}_{4}}{\mathrm{x}_{31}}=-21.36 \cdot \mathrm{lbf} \\
& \mathrm{~F}_{\mathrm{x} 3}:=\frac{\mathrm{T}_{1}}{y_{31}}+\frac{\mathrm{T}_{2}}{y_{31}}+\frac{\mathrm{T}_{3}}{y_{32}}+\frac{\mathrm{T}_{4}}{y_{32}}=-189.115 \cdot \mathrm{lbf} \\
& \mathrm{Fy}_{3}^{\prime}:=\mathrm{F}_{\mathrm{y} 3} \cdot \sin (60 \mathrm{deg})+\mathrm{F}_{\mathrm{x} 3} \cdot \cos (60 \mathrm{deg})=-113.056 \cdot \mathrm{lbf}
\end{aligned}
$$

$$
\mathrm{Fx}_{3}^{\prime}:=\mathrm{F}_{\mathrm{y} 3} \cdot \cos (60 \mathrm{deg})+\mathrm{F}_{\mathrm{x} 3} \cdot \sin (60 \mathrm{deg})=-174.459 \cdot \mathrm{lbf}
$$

## FOR AIRCRAFT CLAMP 4:

$$
\begin{aligned}
& \mathrm{F}_{\mathrm{y} 4}:=\frac{\mathrm{T}_{1}}{\mathrm{x}_{41}}+\frac{\mathrm{T}_{2}}{\mathrm{x}_{42}}+\frac{\mathrm{T}_{3}}{\mathrm{x}_{42}}+\frac{\mathrm{T}_{4}}{\mathrm{x}_{41}}=-243.614 \cdot \mathrm{lbf} \\
& \mathrm{~F}_{\mathrm{x} 4}:=\frac{\mathrm{T}_{1}}{\mathrm{y}_{41}}+\frac{\mathrm{T}_{2}}{\mathrm{y}_{41}}+\frac{\mathrm{T}_{3}}{\mathrm{y}_{42}}+\frac{\mathrm{T}_{4}}{\mathrm{y}_{42}}=37.076 \cdot \mathrm{lbf} \\
& \mathrm{Fy}_{4}^{\prime}:=\mathrm{F}_{\mathrm{y} 4} \cdot \sin (60 \mathrm{deg})+\mathrm{F}_{\mathrm{x} 4} \cdot \cos (60 \mathrm{deg})=-192.438 \cdot \mathrm{lbf} \\
& \mathrm{Fx}_{4}^{\prime}:=\mathrm{F}_{\mathrm{y} 4} \cdot \cos (60 \mathrm{deg})+\mathrm{F}_{\mathrm{x} 4} \cdot \sin (60 \mathrm{deg})=-89.698 \cdot \mathrm{lbf}
\end{aligned}
$$

## teAR OUT CALCULATIONS:

Using equation 4.9 from pg 185 of Robert L. Norton's Machine Design Text we have the shear stress equation to be used in a tearout analysis, equation 4.9 is reproduced below.
$\tau_{\text {xy }}:=\frac{P}{A_{\text {shear }}}{ }^{\prime}$
Where P is the load applied to the hole being analized for tearout, and $\mathrm{A}_{\text {shear }}$ is the area of material being sheared, in this case it is the width of the mounting plate $\left(w_{1}\right)$ multiplied by the wall thickness ( t ), and multiplied by 2 to account for both sides of the hole, that is

$$
\begin{aligned}
& A_{\text {shear }}:=2 \cdot w_{1} \cdot t^{\prime \prime} \\
& t_{1}:=.25 \mathrm{in}
\end{aligned}
$$

substituting the ultimate tensile strength of the assumed material for $\mathrm{T}_{\mathrm{xy}}$, and rearanging to solve for the minimum wall thickness we have:
For the assumed material of acrylic, from page 1026 of Robert L. Norton's Machine Design Text we have an ultimate tensile strength ,and ultimate compressive strength of.


## TEAR-OUT CONCLUSION:

To ensure design uniformity, we will need to choose the largest required thickness as a required minimum wall thickness for the mounting plate, thus we will choose a minimum wall thickness of 0.035 inches.

## WEIGHT CALCULATION:



Figure 5: Dimensions of Plate, For Weight Calculation

## GIVENS:

$\gamma_{\text {acrylic }}:=1.18$
Specific gravity of acrylic, from table A-11 pg. 1026 of Robert L. Norton's Machine Design text.
$P_{h 20}:=1000 \frac{\mathrm{~kg}}{\mathrm{~m}^{3}} \quad$ Density of water
$\rho_{\text {acrylic }}:=\rho_{\mathrm{h} 20} \cdot \gamma_{\text {acrylic }}=1180 \frac{\mathrm{~kg}}{\mathrm{~m}^{3}} \quad$ Density of acrylic
$\mathrm{w}_{1}:=7.5 \mathrm{in}$
The width of the top of the plate
$\mathrm{h}:=7.5 \mathrm{in}$
The maximum height of the plate
$\theta:=60 \mathrm{deg}$
$\mathrm{w}_{2}:=3.17 \mathrm{in}$
$\mathrm{w}_{\mathrm{t}}:=\mathrm{w}_{1}-\mathrm{w}_{2}=4.33 \cdot \mathrm{in}$
$\mathrm{t}_{4}=.25 \mathrm{in}$
$\mathrm{D}_{1}:=.17 \mathrm{in}$
$\mathrm{L}_{1}:=.58 \mathrm{in}$
$L_{2}:=.05 \mathrm{in}$

## VOLLUME AND WEIGHT OF PLATE:

$$
\begin{aligned}
& \mathrm{V}_{\mathrm{h}}:=\pi \cdot\left(\frac{\mathrm{D}_{1}}{2}\right)^{2} \cdot \mathrm{w}_{1}=0.17 \cdot \mathrm{in}^{3} \quad \text { Volume of } 1 \text { guidance pulley mounting hole } \\
& \mathrm{V}_{\mathrm{ah}}:=\mathrm{L}_{1} \cdot \mathrm{~L}_{2} \cdot \mathrm{t}_{1}=7.25 \times 10^{-3} \cdot \mathrm{in}^{3} \quad \text { Volume of } 1 \text { aircraft clamp mounting hole } \\
& \mathrm{V}_{\mathrm{p}}:=\left[\left(\mathrm{h} \cdot \mathrm{w}_{2} \cdot \mathrm{t}_{1}\right)+\left(\frac{\mathrm{w}_{\mathrm{t}} \cdot \mathrm{~h}}{2} \cdot \mathrm{t}_{1}\right)\right]-4 \cdot \mathrm{~V}_{\mathrm{ah}}-4 \cdot \mathrm{~V}_{\mathrm{h}}=9.293 \cdot \mathrm{in}^{3} \quad \text { Total volume of plate } \\
& \text { weight } \mathrm{p}_{\text {plate }}:=\rho_{\text {acrylic }} \cdot \mathrm{g} \cdot \mathrm{~V}_{\mathrm{p}}=0.396 \cdot \mathrm{lbf} \quad \text { Total weight of plate }
\end{aligned}
$$

Here we can see that the weight of the acryilic plate will not be a design issue

## Appendix H: Decision Matrix



Appendix I: Bill of Materials


| ITEM NO. | PART NUMBER | DESCRIPTION | QTY. |
| :---: | :---: | :---: | :---: |
| 1 | U-Channel |  | 2 |
| 2 | spring mounting bracket |  | 1 |
| 3 | Double Pully |  | 2 |
| 4 | spring anchor |  | 4 |
| 5 | machine screw nut hex_ai |  | 12 |
| 6 | Spring |  | 2 |
| 7 | Sliding Block |  | 2 |
| 8 | hexbolt_ai |  | 4 |
| 9 | nexnut_ai |  | 4 |
| 10 | hexscrew_ai |  | 4 |
| 11 | pan slot head_ai |  | 4 |
| 12 | pulley mounting bracket |  | 1 |

## Appendix J: List of Purchased Materials

| Item | Supplier | Image |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Guidance <br> pulley | MSC Industrial <br> Supply |  |  |  |




| Spring <br> Anchors | Century Spring |  |
| :---: | :---: | :---: |

## Appendix K: Explanation of Spread Sheet Analysis

The following document is meant to display analysis completed on the Torsion bar design for the hamstring muscle assistance device. It is comprised of two sections, the first is numerical analysis of stress and deflection of the bar which is represented by the spread sheet analysis attached.

## Stress at end of torsion bar:

The stress in a torsion bar can be calculated through the use of Equation 1, shown below:

$$
\begin{equation*}
S_{T}=\frac{16 T}{\pi D^{3}} \tag{14}
\end{equation*}
$$

Equation I 1: Stress in a Torsion Bar

The highest stress in the torsion bar will be at the ends where the design of the torsion bar will step down from a circular cross-section into a square cross section. To calculate the stress at this point we first must find an equivalent diameter for the square cross section this can be achieved through the use of equation 6.7 d combined with the equation for $\mathrm{A}_{95}$ of a square cross section in Figure 6-25c of Robert L. Norton's Machine Design text book, on pages 363 and 364 respectively. Using this equivalent diameter a corrected endurance limit can be found using 6.6 combined with correction factors outlined in equations $6.7 \mathrm{a}-\mathrm{f}$ along with table $6-4$, which can be found on pages 362-367 of the machine design text.

## Safety Factor for torsion bar:

The safety factor for a torsion bar can be calculated based on Equation 2 produced below:

$$
\begin{equation*}
n=\frac{\pi D^{3}}{32 K_{f s}\left(\frac{T_{a}}{S_{n}}+\frac{T_{m}}{\sigma_{e}}\right)} \tag{19}
\end{equation*}
$$

Equation I 2: Safety Factor for a Torsion Bar

Where D is the equivalent diameter of the torsion bar square attachment section, $\mathrm{T}_{\mathrm{a}}$ is the alternating torque component, $\mathrm{T}_{\mathrm{m}}$ is the mean torque component, $\mathrm{K}_{\mathrm{fs}}$ is the fatigue stress concentration factor, $\mathrm{S}_{\mathrm{n}}$ is the corrected endurance limit of the material, and $\sigma_{\mathrm{e}}$ is the yield strength of the material.
$\mathrm{K}_{\mathrm{fs}}$ can be calculated by first calculating $\mathrm{K}_{\mathrm{t}}$, the geometric stress concentration factor, which can be calculated from Equation 3 below:

$$
A \times\left(\frac{r}{d}\right)^{b}
$$

Equation I 3: Stress Concentration Factor

Where $r$ is the notch radius, $d$ is the equivalent diameter of the square attachment end, A and b are constants which can be obtained from figure C-3 on page 1033 of Robert L. Norton's Machine Design Text book. To ensure an accurate calculation we generated a curve fit polynomial using Mathcad, using this polynomial we were able to determine the A and b values for any D/d ratio. D/d being the ratio of the Torsion bar diameter (D) to the equivalent diameter of the square cross section (d).
To find the fatigue stress concentration factor we first need to determine the notch sensitivity q , which can be equated from equation 6.13 on page 375 of Robert Norton's Machine Design text book reproduced below:

$$
\begin{gathered}
q=\frac{1}{1+\frac{\sqrt{a}}{\sqrt{r}}} \\
\text { Equation I 4: Notch Sensitivity }
\end{gathered}
$$

Where q is the notch sensitivity a represents the Neuber's constant which for steels can be found from table 6-6 on page 378 of Robert Norton's Machine Design text book. And r represents the notch radius.

Once we have calculated the notch sensitivity we can proceed to calculate the fatigue stress concentration factor from equation 6.11 b on page 375 of Robert Norton's Machine Design text book, reproduced below:

$$
K_{f}=1+q\left(K_{t}-1\right)
$$

Equation I 5: Fatigue Stress Concentration Factor
Where $\mathrm{K}_{\mathrm{t}}$ is the geometric stress concentration factor as calculated previously, and q is the notch sensitivity as calculated previously.
Using this information we can calculate the safety factor using Equation 2 above.

## Appendix L: Spreadsheet Analysis

## Stainless Steel

## Angle of Deflection



| SL＇L | SL89 ${ }^{\text {T }}$ | SZ9＇โ | SZ9s＇I | ¢＇L | SLEt ${ }^{\text {c }}$ | SLE＇T | SZTE＇T | SでT | SL8I＇T | SZI＇L | SZ90＇โ | โ | SLE60 | SL8＊0 | SZT8＊0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $90^{\circ} 0$ | L0＇0 | $80^{\circ}$ | OT＊ | てT0 | カt＇0 | LİO | OZ＊ | カで0 | $00^{\circ}$ | $\angle \varepsilon^{\circ}$ | $9{ }^{\circ} 0$ | $65^{\circ} 0$ | 9L0 | T0＇โ | $9 \mathrm{e}^{\prime}$ I |
| 900 | LO＇0 | 80.0 | OT． 0 | It\％ | カt＇0 | 9T．0 | $65^{\circ}$ | ャで0 | 6で0 | $98^{\circ}$ | St＇0 | $85^{\circ} 0$ | SLO | 86.0 | てと＇โ |
| $90^{\circ}$ | LO＇0 | $80^{\circ}$ | 60.0 | tio | $\varepsilon \tau 0$ | $99^{\circ}$ | $65^{\circ} 0$ | とでo | 8で0 | ¢ع＊ | 切0 | $95^{\circ} 0$ | $\varepsilon L^{\circ} 0$ | 96.0 | 6で「 |
| 900 | LO＇0 | 80.0 | 60.0 | It\％ | \＆โ＇0 | St． 0 | 8 L 0 | てで0 | $87^{\circ}$ | $\downarrow \varepsilon^{\circ}$ | $\varepsilon \overbrace{}^{\circ}$ | Ss．0 | TLO | 76．0 | 9で「 |
| 900 | LO＇0 | $80^{\circ}$ | $60 \cdot 0$ | It\％ | $\varepsilon \tau 0$ | St．0 | 8 t 0 | てで0 | LでO | દと＊ | で○ | \＆s．0 | 69.0 | 16．0 | とでโ |
| 900 | 90\％ | LO＇0 | $60 \cdot 0$ | OT．0 | てL。 | St．0 | $8 \mathrm{~T}^{\circ}$ | しで0 | 9で0 | てと＊ | 切0 | てs．0 | $\angle 9.0$ | 68.0 | 6I＇โ |
| SO\％ | $90^{\circ}$ | LO＇0 | $80 \%$ | OT\％ | てT0 | tio | $\angle T 0$ | Lで0 | sで0 | てと＊ | O＊＊ | TSO | $99^{\circ}$ | $98^{\circ}$ | 9I＇โ |
| SO\％ | 90\％ | $\angle 0^{\circ}$ | 80.0 | OT．0 | で○ | tio | $\angle T 0$ | OでO | sでo | โع० | $68^{\circ}$ | $66^{\circ} 0$ | t9．0 | 78.0 | $\varepsilon \tau^{\prime} \tau$ |
| S0．0 | $90^{\circ}$ | LOO | 80 | $60 \%$ | Ito | $\varepsilon \tau 0$ | 91．0 | OでO | ャで0 | $00^{\circ}$ | $88^{\circ}$ | $85^{\circ} 0$ | 29.0 | 28.0 | OT＇โ |
| S0\％ | 900 | $\angle 0^{\circ}$ | $80 \%$ | $60 \%$ | It\％ |  | 91．0 | 6100 | とで0 | 6で0 | $98^{\circ}$ | $95^{\circ} 0$ | 09.0 | $6 L^{\circ}$ | 90＇โ |
| S0\％ | 900 | $90 \cdot 0$ | 800 | $60 \%$ | Ito | \＆โ＇0 | St．0 | 8 c 0 | とで0 | $88^{\circ}$ | ¢¢＇0 | $5 \mathrm{StO}_{0}$ | $85^{\circ}$ | $\angle L O$ | ع0＇โ |
| S0\％ | S0\％ | $90 \cdot 0$ | L0＇0 | $60 \%$ | OT\％ | てT0 | St．0 | 8t\％ | てで0 | Lで0 | เع＊0 | 切0 | $99^{\circ}$ | カL＊O | 00＇โ |
| to 0 | S0\％ | 90.0 | $\angle 0^{\circ}$ | 80.0 | OT0 | 2T0 | ちT0 | LTO | しで0 | 920 | દと＊ | でロ | SS．0 | てLO | $\angle 6.0$ |
| ＋0．0 | S0＇0 | $90 \%$ | LO＇0 | 80.0 | OT＇0 | IT0 | ちT0 | LTO | Lで0 | sでo | てع｀0 | でO | \＆ร．0 | OLO | 76．0 |
| ＋0．0 | S0\％ | $90 \cdot 0$ | LO＇0 | 80.0 | $60 \cdot 0$ | It．0 | \＆1．0 | 9t＇0 | OZO | szo | เع＇0 | $68^{\circ}$ | Ts．0 | $\angle 9^{\circ}$ | 06.0 |
| ＋0．0 | S0\％ | S0\％ | 90\％ | $80 \%$ | $60^{\circ}$ | It．0 | \＆โ．0 | 9t\％ | 610 | ャで0 | $0 \chi^{\circ}$ | $88^{\circ}$ | $66^{\circ}$ | ¢9．0 | $\angle 8.0$ |
| ＋0．0 | S0\％ | SO\％ | 900 | LO＇0 | $60^{\circ}$ | OT． 0 | てT0 | Sto | 850 | દで0 | $67^{\circ}$ | Lع० | $\angle \rightarrow 0$ | 29.0 | 78.0 |
| $\stackrel{\circ}{+}+00$ | t0 0 | SO． 0 | $90 \%$ | LO＇0 | $80 \%$ | OT． 0 | てT．0 | カt゚O | 850 | てで0 | $87^{\circ}$ | ऽ．0 | $97^{\circ}$ | 09.0 | 18．0 |
| to 0 | ＋0．0 | SO\％ | $90 \%$ | LO＇0 | $80^{\circ}$ | $60^{\circ}$ | IT0 | カİO | $\angle 10$ | Lで0 | 9 9\％0 $^{0}$ | ャع＊ | 切0 | $85^{\circ}$ | $\angle L O$ |
| ع0＇0 | ＋0．0 | SO\％ | SO\％ | $90 \cdot 0$ | $80^{\circ}$ | $60^{\circ}$ | It．0 | Et＇0 | 91.0 | OZO | ¢で0 | てع0 | でO | ¢s．0 | tL＇0 |
| ع0\％ | ＋0\％ | 70．0 | S0\％ | $90 \%$ | L0＇0 | $60^{\circ}$ | OT．0 | \＆t｀o | $99^{\circ}$ | $65^{\circ}$ | 七で0 | โ $\varepsilon^{\circ}$ | $00^{\circ}$ | \＆ร．0 | LLOO |
| ع0\％ | t0 0 | t0 0 | SO\％ | 90.0 | LO＇0 | $80^{\circ}$ | OT． 0 | で○ | Sto | 850 | とでo | $0 \chi^{\circ}$ | $88^{\circ}$ | OS．0 | $89^{\circ}$ |
| ع0\％ | ع0\％ | ＋0．0 | SO\％ | $90 \cdot 0$ | L0＇0 | $80^{\circ}$ | $60 \%$ | てİ0 | カto | 8 T 0 | てで0 | 8 8＇0 $^{0}$ | $9 \mathrm{c}^{\circ}$ | $8 \mathrm{t}^{\circ}$ | 59.0 |
| ع0\％ | ع0＇0 | t0 0 | t0 0 | SO\％ | 90.0 | LO＇0 | 60.0 | LTO | $\varepsilon \tau 0$ | $\angle T 0$ | Lで0 | Lて＇O | ऽ¢．0 | $96^{\circ}$ | 59\％ |
| ع0\％ | ع0＇0 | t0 0 | ＋0．0 | SO\％ | $90 \%$ | LO＇0 | 60.0 | OTO | \＆โ．0 | 9 T 0 | OでO | sて＇0 | દદ＇0 | Etio | $85^{\circ}$ |
| ع0\％ | ع0＇0 | ع0＇0 | to 0 | SO\％ | $90 \%$ | $\angle 0.0$ | 80.0 | Ot＇0 | てT0 | Sto | $66^{\circ}$ | ャで0 | โع＇0 | 切0 | SS．0 |
| 20\％ | ع0＇0 | ع0＇0 | to 0 | to 0 | SO\％ | $90 \cdot 0$ | 80.0 | 600 | LTO | $\dagger$ to | $8 \mathrm{~L}^{\circ}$ | とでo | $67^{\circ}$ | $88^{\circ}$ | てS＇0 |
| 20\％ | ع0＇0 | ع0＇0 | t0 0 | to 0 | S0\％ | $90^{\circ}$ | $\angle 0^{\circ}$ | 600 | T10 | $\varepsilon \tau 0$ | $\angle 10$ | でO | Lて＇0 | $9 \varepsilon^{\circ}$ | $8{ }^{\circ} 0$ |
| 200 | 20＊ | ع0＇0 | ع0\％ | to 0 | SO\％ | $90 \%$ | $\angle 0 \cdot 0$ | 800 | OT． 0 | 2T0 | Sto | OてO | sて＇0 | $\downarrow \varepsilon^{\circ}$ | Stio |
| 200 | 20＊0 | ع0＊0 | ع0\％ | to 0 | to 0 | SO．0 | $90 \cdot 0$ | LOO | $60 \%$ | It．0 | カto | 810 | ャで0 | โع＇0 | でフ |
| 200 | 20＊0 | 200 | ع0＊0 | ع0｀0 | to 0 | SO．0 | $90 \cdot 0$ | LOO | $80 \%$ | It 0 | $\varepsilon \tau 0$ | $\angle \mathrm{CO}$ | てで0 | 670 | $6 \varepsilon^{\circ}$ |
| 10\％ | 10\％ | 20＊ | 20＊ | 20｀0 | ع0\％ | ع0\％ | ＋0．0 | SO\％ | 90\％ | LO\％ | $60 \%$ | ITO | St．0 | 61．0 | 9で0 |


|  |  |  |  |  |  |  |  | †T8．0 | I | 969L9 0 | $L{ }^{\circ}$ |  |
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|  |  |  |  |  | $(\mp \tau) \frac{\varepsilon \Omega^{u}}{L 9 \tau}={ }^{L} S$ |  |  | $(\% 66)^{\text {qe！｜｜}}$ \％ |  | －nns | peolo |  |
|  |  |  |  |  |  |  |  |  |  |  | S＇Z6 |  |
| 65＊89Lてを | てて＇L90をE | S8＊66をદદ | ヤL｀ヤLLEと | LS＇દOZ七¢ | દでદ0ん๖¢ | Lで089¢E | しで089Sを | Lて＇089SE | Lて＇089SE | Lて＇089Sを | 9ZIZ＇089Sを |  |
| L৮S¢9s＊0 | ZSOSTS＊0 | 9SSt9to | T90カでガ0 | 99¢\＆9と＊ | TLOELE＇0 | SLSて9で0 | 80てIで0 | S8ST9T＊0 | 60LIT＂0 | 七6S090＇0 | S06600t0＊0 | ：（u！）puə su！funow fo ${ }^{\text {nnba }} \mathrm{p}$ |
| $\angle 0$ | SLE9＊0 | SLS 0 | SZIS＊0 | Sto | SL8E＊ | ¢てع0 | SZ9で0 | でO | SLET＊O | SLOO | SZTO＊0 |  |
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| 86＇てヤ8を¢ | SS＇t08tt | ャع＊090т9 | LS＇ゅをて98 | L8ELZT | て＇Z0S66I | S＇ZSI8E\＆ | でと9Ltヶ9 | 8TOTStT |  | L6SSISLZ | 88889を\＆も6S | 8 |
| 86＇てヤ8\＆と | ss＇t08tt | 七ع090т9 | LS＇ゅعて98 | L8ELZT | て＇Z0S66I | S＇乙SI8\＆દ | て＇と9Ltヶ9 | 8TOTStT | でを¢9tt | L6SSISLZ | 88889を\＆七6S | S $L^{\circ} L$ |
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| 86＇てヤ8\＆と | ss ${ }^{\text {ctostt }}$ | 七ع＊090т9 | TS＇ャ ${ }^{\text {cos98 }}$ | L8ELZT | て＇Z0S66T | S＇ZST8を¢ | でと9Ltヶ9 | 8TOTStT |  | L6SSISLZ | 88889と\＆t6S | SL＇S |
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| 86＇てヤ8をと | ss＇t08tt | 七ع090т9 | LS＇ゅをて98 | L8ELZT | て＇Z0S66T | ¢＇ZST8を¢ | でと9Ltヶ9 | 8TOTStT |  | L6SSTSLZ | 88889を\＆ヤ6S | $\varepsilon$ |
| 86＇てヤ8をと | ss ${ }^{\text {ctosttt }}$ | ャع＊090т9 | TS＇も ${ }^{\text {cos98 }}$ | L8ELZT | て＇Z0S66L | S＇ZST8\＆¢ | でと9Ltヵ9 | 8TOTSカT | で\＆ | L6SSISLて | 88889ع\＆t6S | SL＇Z |
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| 86＇てヤ8\＆と | ss＇t08tt | ャع090т9 | LS＇ゅをて98 | L8ELZT | て＇Z0S66I | S＇ZSโ8દદ | でと9Ltヶ9 | 8TOTS力T | でを¢9tt | L6SSTSLZ | 88889\＆\＆ヤ6S | て |
| 86＇てヤ8を์ | ss＇t08tt | ャع＊090т9 |  | L8\＆LZT | て＇Z0S66I | ¢＇乙SI8\＆દ | でと9Ltヶ9 | 8TOTSちT |  | L6SSISLて | 88889を\＆ヤ6S | SL＇I |
| 86＇てヤ8をと | ss＇t08tt | ャع＇090т9 | LS＇ャعて98 | L8\＆LてT | て＇Z0S66I | S＇ZSI8\＆\＆ | でと9Ltヶ9 | 8TOTSカT | でを¢9tt | L6SSTSLZ | 88889を\＆ヤ6S | S＇L |
| 86＇てヤ8\＆と | ss＇t08tt | ャع090т9 | LS＇ゅعて98 | L8ELZT | て＇Z0S66I | S＇ZSโ8દદ | でと9Ltゅ9 | 8TOTS力T | で\＆く9tt | L6SSTSLZ | 88889\＆\＆ヤ6S | Sて＇I |
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| 86｀てヤ8\＆と | ss＇t08tt | 七ع090т9 | โS＇ゅをて98 | L8ELZT | て＇Z0S66T | S＇ZST8દと | て＇を9Ltヶ9 | 8TOTS力T |  | L6SSTSLZ | 88889を\＆も6S | Sで0 |
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|  | ¢9＇ऽ ${ }^{\text {S }}$（T0を | LL 68て0 | 86 80ヶ0¢ | TL｀を๕S0¢ | 8ガt990を | 68＇T080ع | 65 9 ¢760E | 8ع＊660tを | SI｀t9ZTE | 66＊てをカtを | ST｀9T9tを | $\varepsilon$ | ऽ8＇ててOZを | でદ | てદ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| － | 9L6Zてと | L8L | S86 | 6ヵT | S66 | S0 | ＋000 | 60 | カT06I6\％ | 6I | દZO | 8て | ¢ | Lعऽ999＊0 | ても0919＊0 |
| L＇L | SL | SLS＇L | SZTS＇L |  | S $\angle 8$＇$^{\text {L }}$ | ૬Zદ＇โ | ¢Z9て＇T |  | SLE | SLO＇I | SZTO＇T | S6．0 | SL88＇0 | SZ8＇0 | SZ9L｀0 |
| SL＇T | SL89 | Sて9＇โ | SZ9S＇โ | S＇L | SLEt＇โ | SLE＇โ | SてIE＇โ | Sて＇T | SL8I＇工 |  | SZ90＇T |  | SLE6＇0 | SL8＇0 | SてI8＊0 |
| 七L＇Z9をて | ヤく｀とt9て | 9ZT「 | LL8＇ヤऽรを | S99＊ | 7L | I＇0 | SLS＊89LS | Sく9 | 76．988L | L60 | ¢ $\mathrm{c}^{\text {cill }}$ | Lİ6をS¢โ | てL｀S099T | 88 | どもヤ8t9て |
|  |  |  |  |  |  |  |  |  |  |  |  |  | てL＇S099］ |  | とガヤ8t9て |
| カぐて |  | 9 | LL8 | 599 | V | $\angle 9$ | S $\angle 5$ •89 ${ }^{\text {S }}$ | SL | 76＊988L | L60＇tナ \％6 | S＇E8LIT | LI＇6をऽรโ | 991 | 902 | โ92 |
| \＆Z | カL＇Et92 | 9ZT | LL8 | S9 | t | $\angle$ | SLS＇89LS | SL | 76 ${ }^{\circ} 9882$ | L60＇tナE6 |  | LI＇6६SET | てL＇S099］ | 88＇てL90て | 97 |
| ヤL＇て9をて | ヤL | 9 | LL8 | S9 |  | L9 | SL |  |  | $\angle 6$ |  | LI＇6をSEL | てL＇S099］ | Z | \％ |
| ヤL＇て9をて | カL＇とt9て | 9てI＇TL6て | LL8＇†ऽรع | S99＊ | 七L＇St\＆t | L9T．066t | S $\angle 5.89 \angle 5$ | SL | 七6 | L60＇tナE6 | ऽと8IIL | LI＇6๕SET | てL｀S099T | 88＇てL90て | どヤヤ8t9て |
| ＇z9をて | 七ぐ¢カ9て | 9てT＇tく6て | LL8＇ヤऽร์ | 599＇L08E | 七L＇St¢ | L9โ．066t | SLS 896 | SL | 76．988L | L60＇tナE6 | ¢ $¢ 8$ ILI | ＜l＇6६ऽ\＆โ | てL＇S099T | 88＇ZL902 | 97 |
| とて | ヤL | 92 | LL8 | S9 | t | L9 | S | S | 76＇988L | L60＇tワE6 | S＇E8LIT | Lİ6をSEL | てL＇S099T | Z | 2 |
| 七L＇て9をて | ヤく＇とt9て | 9てT「TL6て | LL8 | 599 | $\dagger L$ | L9T．066t | S $\angle 5$＇89LS | SL | 76 | L60＇tナE6 | ¢＇ع8ItI |  | てL＇S099T | 88＇ZL902 | とがヤ8t9て |
| て9をて | ヤぐ¢カ9て | 9てt＊TL6 | LL8＇ヤऽร¢ | S99＇L088 | ヤL＇St¢ | L9T＊066 | SLS＇89 | SL | 76．988L | L60＇tナ ${ }^{\text {c }}$ | S＇દ8ILI | LT＊6をS¢โ | てL｀S099］ | 88＇ZL902 | T92 |
| ャL＇て9をて | ヤL | 92 | LL8＇ヤऽร์ | ¢99＇L088 | 七L｀SちEt | L9T．066t | SL |  | 76．988L | L | ¢＇E8LIT | Lİ6をร¢โ | てL｀S099 | Z | どヤヤ8t9て |
| ヤL＇z9をて | カL＇とt9\％ | 97 | LL8 | S99 | 7 | 49 | SL | SL | 76 | L60 | ¢ | LI＇6६SEL | てLS09 | 88＇ZL90Z | L92 |
| ヤL＇て9をて | ヤく＇とカ9て | 9てT「TL6て | LL8＇ヤऽร์ | 599 | ヤL＇St\＆t | L9โ．066t | S $\angle$ ¢ $89 /$ |  | 76．988L | L60＇tナE6 | ¢ $¢ 8$ ItI | ［＇6६ऽรโ | てL｀S099T | 88＇ZL90Z | t92 |
|  | カL | 9 | LL8＇もऽ\＆¢ | S9 | 七L｀StEt | $\angle$ | SL | S | t6 | L | S＇E8LIT | I | てL｀S099 | Z | ¢ |
| ヤL | ヤL＇¢t9\％ | 9ZT | 8 | S9 |  | LS | SL | SL | t6 | L60 | S | L | てL＇S099T | 88＇ZL90て | 92 |
| ૪L＇て9とて | ヤL＇¢カ9Z | 9てt＇tL6て | LL8＇tSを | 599＇L088 | 七＇St¢ | L9t＇066 |  | S $\angle 99^{\circ} \mathrm{LT}$ | 76．988L | L60＇tナE6 | ¢ $\mathrm{c}^{\text {cilli }}$ |  | てL｀S099］ | 88＇ZL902 | － 8 ¢T9て |
| て9をて | ヤく＇とカ9て | 92 | LL | ¢9 | 七L | L9โ．06 | SL | SL | 76 | L60＇tナE6 | S | бદऽદโ | てL＇S099 | 902 | 92 |
| 七L＇て9とて | ヤL＇¢t9\％ | 9で「 | LL8 | S99＇ | VL | L9T．066 | SLS＇89 | SL | 七6 | $\angle 60$ | ¢＇દ8ILT | LT＊6\＆ร¢โ | てL｀S099 | 88＇ZL90Z | どヤヤ8t9て |
| 七L＇て9をて | ヤぐとカ9て | 9てT「TL6て | LL8＇もSદ | S99＇L08 | $\downarrow L$＇StEt | L9t．066 | S $\angle$＇89 ${ }^{\text {c }}$ | S $\angle 9.1$ LL | 76.9882 | L60＇tナE6 | ¢ $¢ 8$ ItI | ＜l＊ 6 ¢¢\＆โ | てL＇S099T | 88＇ZL902 | とがヤ8t9て |
| ヤL＇て9とて | ヤL＇¢カ9て | 971 | LL8 | S99＇L08 | ヤL | ＜9T．066 | SLS＇89 | S | t6 | L60＇tナE6 | ¢＇と8tul |  | てL｀¢099 | 88＇ZL902 | どヤヤ8T9て |
| 七L＇て9をて | ヤく＇とt9て | 9てI＇L | LL8＇t | S99＇L | 7L | L9T＊066 | SLS＇89 | SL | t6 | L60＇tナE6 | S．ع8ItI | LT＇6\＆ | てL＇S099 | 88＇てL90Z | とガヤ8t9て |
| ャL＇て9とて | ヤく＇とt9て | 9てT＇โL6て | LL8＇†ऽદ | S99＇L08 | tL＇StEt | L9T＇066 | SLS＇89LS | SL | 882 | L60＇tヤE6 | ऽ＇E8ILT | LT＇6६ऽ\＆โ | てL＇S099 | 88＇ZL90Z | とガヤ8T9て |
| 七L＇て9عZ | カL｀¢t9て | 9てI＇TL6て | LL8＇七ऽ\＆¢ | S99＇L08E | tL＇StEt | L9T＇066t | SLS＇89L | S $29{ }^{\circ} \mathrm{LT}$（ | 76＇988 | L60＇tもE6 | S＇88ILI | LT＊6¢SET | てL｀S099 | 88＇てL902 | どもヤ8T9て |
| ヤL＇て9をて | ヤく＇とカ9て | 9てt＇L | LL8 | S99＇L | 七L＇SカEt | $\angle 9$ |  | SL | 76．988 | $\angle 60{ }^{\circ} \mathrm{t}$ ¢ | $\mathrm{S}^{\prime}$ | L「6をS | てL｀S099T | 88＇ZL90Z | どヤヤ8t9て |
| 七L＇て9とて | ヤL＇とt9 | 9で「 | LL8＇ | S99＊ | ঢL＇St¢ | L9t．066 | SLS 8965 | S $\angle 99^{\circ} \mathrm{LT}$ | 76．988L | L60＇tte6 | ¢ ¢8ILI | くl＇6६ऽรโ | てL｀¢099 | 88＇てL902 | とガヤ8t9て |
| 七L＇て9とて |  | 9てT「Tく6て | LL8＇ヤऽร์ | 599＇L08E | tL＇St¢t | L9T．066t | SLS＇89LS | S $\angle 9.1$ L 19 | 76．988L | L60＇tte6 |  |  | てL｀S099］ | 88＇ZL902 | どヤヤ8t9て |
| ヤL＇て9をて | ヤく＇とカ9て | 9てt＇tL6 | LL8＇t | S99＇L08 | ヤL＇ | L9t＇066 | SLS＇89LS | S S9$^{\circ}$ | 76．988L | L60＇tナE6 | ¢ $\mathrm{c}^{\text {cilli }}$ |  | てL｀S099T | 88＇ZL90Z | どヤヤ8t9て |
| ヤL＇て9とて | カL＇¢t9\％ | 9てI＇Tく6て | LL8＇tSદ | S99＇L088 | tL＇St¢t | L9t．0667 | SLS＇89LS | S $\angle 99^{\circ} \mathrm{LL}$ | 76．988L | L60＇tte6 | s．E8tII | LT＊6をS\＆โ | てL＇S099 | 88＇てL90て | どヤヤ8t9て |
| ヤL＇て9をて | ヤぐとt9て | 9てT「Tく6て | LL8＇tऽ\＆と | S99＇L08E | 七L＇St\＆t | L9โ 066t | S $\angle 5$＇89LS | S $\angle 9.2 T \angle 9$ | 76．988L | L60＇tナE6 | ¢ $\mathrm{c}^{\text {ctul }}$ | LT＊6を¢\＆โ | てL＇S099T | 88＇ZL902 | とがヤ8t9て |
| 七L＇て9とて | 七＜＇¢t9て | 9てT「Tく6て | LL8＇ヤऽร์ | 599＊L08E | 七L＇StCt | L9โ．066t | SLS＇89LS | S $\angle 9 \times 1 / 29$ | 76．988L | L60＇tte6 | s＇દ8ILI |  | てL｀S099］ | 88＇ZL902 | どヤヤ8t9て |
| 七L＇て9عて | カL＇Et92 | 9てT「Tく6て | LL8＇七ऽ\＆¢ | 599＊L08E | カL＇StEt | L9T．066t | SLS＇89LS | S $\angle 9.1$ L $\angle 9$ | 76．988L | L60＇tte6 | s＇88tIT | LT＊6をS\＆โ | てL｀S099］ | 88＇てL90て | どヤヤ8t9て |
| 七＜＇て9とて | カL＇とt9\％ | 9てT＇TL6て | LL8＇tऽ\＆と | 599＇L08E |  | L9T＇066ヵ | SLS＇89LS | S $29 \times 1 / 29$ | 76 ${ }^{\prime} 988$ | L60＇tヤ¢6 | ¢＇E8ILI | LI＇6६૬¢โ | ZL｀S099T | 88＇ZL90Z | とガヤ8T9て |

## Safety Factor

| 6¢＇89Lてを | てでL90を¢ | 58＇66をદと | †く＇tLLEと | โs＇ع0乙૪ | દでと0＜ヵ¢ | โて＇089¢を | โて＇089¢を | โて＇089¢を | tz 0895¢ | โで089¢を | を9でで089¢を |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| โて6ちt9＇T | ¢ع0乙t9＇t | Z609LS＇I | とてt9とs＇โ | くtt | 90tてカガ「 | โ七8t88＇โ | ヤ881を＇โ | ャをてせてて＇I | L80ZLT「T | 908186＇0 | L998＜ṫt＇0 |  |
| tโZ898．0 | カtz8980 | ttz8980 | カtて8980 | かtz8980 | カtて8980 | カIZ898＊0 | カIZ8980 | カtて8980 | カtて898＊0 | カtz8980 | દとちtて8980 |  |
| とโ8てもく＇I | ¢¢670＜${ }^{\text {T }}$ | 9¢ऽร99＇โ | Lヤ8LT9＇T | S8995＇t | ยtz60s＇โ | 9รをと切＇L |  | 908t8て＇I | 802861＇t | カt06く6＇0 | 6IT－3t¢でカ－ |  |
| Szo＇0 | Szo＇o | Szo＇o | Szo＇o | Szo＇o | szo＇o | Szo＇o | Szo＇0 | Szo＇o | szo＇o | Szo＇0 | szo 0 | （и！）sn！peı чวпои |
| 6عIEて＇0－ | 166てZ＇0－ | 9LLてで0－ | LStで̇o－ | －L6Iで0－ | 6IZIて＊0－ | 8866100－ | I88LI＇0－ | をてİt 0 － | 58I80\％－ | てSose＇0－ |  | ənje＾q |
| 6L89t80 | toss 0 | 98OSs80 | 908t980 | SS00L8＇0 | І七LZ88＊0 | 2060 | 9¢8てを6＇0 | LEtt860 | 60S090＇T | てヤ8＜t＜${ }^{\circ}$ | LIT686＇85E－ | әп｜e＾$\forall$ |
| ST928＇โ | 818tをと＇L | 698Stع＇I | S6t85E＇T | L9ZSLE＇T | 8tt $\angle 6 \varepsilon^{\prime} \tau$ | T9โ8てヤ＇โ | ¢દLナ＇L | SLTLtS＇I | LZ8L89＇โ | 6290＇z | 6LE66988t＇9 | p／o |
| LtSS9s 0 | ZSOSTS＂0 | 9SSt9to | T90ってt＇0 | 99¢\＆9ع0 | TLOETع＇0 | SLsz9z＇0 | 80てIで0 | S8St9to | 60tut 0 | ャ6S090＇0 | £S06600t0 0 | ：（u！）pua Su！punou fo ${ }^{\text {Anba }} \mathrm{p}$ |
| LO | SLE9 0 | SLS＇0 | SZIS 0 | Sto | SL8E＇0 | sze 0 | ş9zo | 2\％ | SLEL＇0 | S $\angle 0^{\circ} 0$ | SZTOO | ：（u！）puz suḷunow fo uo！suəm！p əp！s |
| SLO | SL89 0 | Sz9 0 | š9s．0 | s．0 | SLEt＇0 | SLE＇0 | Sてİ\％ | sz＇0 | SL8T0 | SZT＇0 | ¢̌90 0 | （u！）．1eq uo！ 5.107 fo 0 |
| โ0－3T6＇ゅ | T0－318 ${ }^{\text {¢ }}$ ¢ | T0－368＇乙 | โ0－3Zでて | T0－367＇โ | 20－3L66 | 20－797＇9 | て0－ヨLt＇ | て0－Э79＇โ | ع0－эt9＇s | ع0－360＇T | S0－3SL＇$\varepsilon$ | 8 |
| โ0－3T6＇t | 10－3T8＇$\varepsilon$ | โ0－368＇乙 | โ0－3で「て | T0－367＇โ | 20－3＜6．6 | 20－э9て＇9 | て0－ヨLナ＇ ¢ | て0－эて9＇โ | ع0－эt9｀ | ع0－360＇โ | S0－3¢ ${ }^{\text {¢ }}$ ¢ | SL＇L |
| โ0－3T6＇t | โ0－эт8＇દ | โ0－368＇て | โ0－ヨマでて | T0－36t＇L | 20－3＜6．6 | 20－эヲて＇9 | 20－3८ナ $\varepsilon$ | 20－эて9＇โ | ع0－эт9｀ऽ | ع0－360＇โ | ¢0－Э¢ ¢ $^{\text {¢ }}$ | S＇L |
| โ0－3T6＇t | 10－378＇$\varepsilon$ | โ0－368＇乙 | โ0－3で「て | 10－367＇โ | 20－3L6＇6 | 20－э97＇9 | 20－ヨ८t＇$\varepsilon$ | マ0－Эて9＇โ | ع0－эt9＇s | ع0－360＇โ | ¢0－Э¢ ${ }^{\text {¢ }}$ ¢ | Sz＇L |
| โ0－3T6＇t | 10－318＇$\varepsilon$ | โ0－368＇て | т0－3で「て | T0－367＇โ | 20－3＜6＇6 | 20－э97＇9 | て0－3Lt＇ | て0－Эて9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3ç＇$\varepsilon$ | $L$ |
| โ0－3T6＇t | โ0－3t8＇$\varepsilon$ | โ0－368＇乙 | โ0－ヨマでて | T0－367＇โ | 20－3L6．6 | 20－э9て＇9 | て0－ヨLt＇\＆ | て0－эて9＇โ | ع0－эt9｀ | ع0－360＇โ |  | SL＇9 |
| โ0－3T6＇t | 10－3T8＇$\varepsilon$ | โ0－368＇乙 | T0－3で「て | T0－367＇โ | 20－3L6．6 | 20－э9て＇9 | て0－3Lt＇ と | て0－Эマ9＇โ | ع0－эt9＇s | ع0－360＇I | S0－ЭSL＇غ | S＇9 |
| โ0－3T6＇t | 10－318＇$\varepsilon$ | โ0－368＇て | т0－3で「て | T0－367＇โ | 20－3＜6＇6 | 20－э97＇9 | て0－ヨ८t＇ ¢ | て0－ヨて9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3c ${ }^{\prime}$＇ | S2＇9 |
| โ0－3T6＇t | 10－3T8＇$\varepsilon$ | โ0－368＇乙 | โ0－3で「て | T0－367＇โ | 20－3＜6．6 | 20－э97＇9 | て0－3Lt＇ | て0－Эマ9＇โ | ع0－эt9＇s | ع0－360＇I | S0－3¢ ${ }^{\text {¢ }}$ ¢ | 9 |
| โ0－3T6＇t | 10－318＇$\varepsilon$ | โ0－368＇て | โ0－3で「て | T0－367＇โ | 20－3＜6．6 | 20－э97＇9 | て0－3Lt＇ ¢ | 20－ヨて9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3ç＇$\varepsilon$ | SL＇S |
| โ0－3T6＇t | โ0－3т8＇દ | T0－368＇乙 | โ0－ヨマでて | T0－36t＇L | 20－3＜6．6 | 20－эヲて＇9 | て0－ヨLt＇\＆ | 20－эて9＇โ | ع0－эт9＇ऽ | ع0－360＇โ |  | s＇s |
| โ0－3T6＇t | 10－318＇$\varepsilon$ | โ0－368＇て | т0－3で「て | 10－367＇โ | 20－3＜6．6 | 20－э97＇9 | て0－3Lt＇ | て0－ヨて9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3c ${ }^{\prime}$ ¢ | Sて＇S |
| โ0－3T6＇t | 10－3T8＇$\varepsilon$ | โ0－368＇乙 | โ0－ヨで「て | T0－367＇โ | 20－3L6．6 | 20－э97＇9 | て0－3Lt＇ | て0－Эマ9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3¢ ${ }^{\text {¢ }}$ ¢ | 5 |
| โ0－3T6＇t | โ0－3т8＇$\varepsilon$ | โ0－368＇乙 | т0－ヨマでて | T0－367＇โ | 20－3＜6．6 | 20－э9て＇9 | て0－ヨLナ＇ ¢ | て0－эて9＇โ | ع0－эt9｀ | ع0－360＇โ | ¢0－3sL＇ ¢ | SL＇t |
| โ0－3T6＇t | 10－3T8＇$\varepsilon$ | โ0－368＇乙 | 10－3で「て | T0－367＇โ | 20－3＜6．6 | 20－э97＇9 | て0－ЭLt＇ と | て0－Эマ9＇โ | ع0－эt9＇ऽ | ع0－360＇โ | S0－ЭSL＇غ | S＇t |
| โ0－3T6＇t | 10－318＇$\varepsilon$ | โ0－368＇て | 10－3で「て | T0－367＇โ | 20－3L6＇6 | 20－э97＇9 | て0－3Lt＇ | マ0－ヨマ9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3c ${ }^{\text {¢ }}$ ¢ | Sて＇t |
| โ0－3T6＇t | 10－3T8＇$\varepsilon$ | โ0－368＇乙 | 10－3で「て | T0－367＇โ | 20－3＜6．6 | 20－э97＇9 | て0－3Lt＇ と | て0－Эマ9＇โ | ع0－эt9＇ऽ | ع0－360＇โ | S0－3¢ ${ }^{\text {¢ }}$ ¢ | † |
| โ0－3T6＇t | 10－318＇$\varepsilon$ | โ0－368＇て | 10－3で「て | T0－367＇โ | 20－3L6＇6 | 20－э97＇9 | て0－3Lt＇ | て0－ヨて9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3c ${ }^{\prime}$＇ | SL＇$\varepsilon$ |
| โ0－3T6＇t | 10－378＇$\varepsilon$ | โ0－368＇乙 | โ0－3で「て | 10－367＇โ | 20－3L6＇6 | 20－э9て＇9 | 20－Э८ナ ¢ | て0－Эて9＇โ | ع0－эt9＇s | ع0－360＇โ | ¢0－Э¢ ${ }^{\text {¢ }}$ ¢ | ¢＇$\varepsilon$ |
| โ0－3T6＇t | 10－318＇$\varepsilon$ | โ0－368＇て | 10－3で「て | T0－367＇โ | 20－3＜6．6 | 20－э97＇9 | て0－3Lt＇ と | て0－Эマ9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3¢ ${ }^{\text {¢ }}$ ¢ | Sて＇દ |
| โ0－3T6＇t | 10－378＇$\varepsilon$ | โ0－368＇乙 | โ0－3で「て | 10－367＇โ | 20－3L6＇6 | 20－э9て＇9 | 20－ヨLt＇ ¢ | て0－Эて9＇โ | ع0－эt9＇ऽ | ع0－360＇โ | ¢0－3¢ ${ }^{\text {¢ }}$ ¢ | $\varepsilon$ |
| โ0－3T6＇も | โ0－эт8＇દ | โ0－368＇て | โ0－ヨマて＇て | T0－36t＇โ | 20－3＜6．6 | 20－э9て＇9 | 20－3८ナ $\varepsilon$ | 20－эて9＇โ | ع0－эт9｀ऽ | ع0－360＇โ | ¢0－Э¢ ¢ $^{\text {¢ }}$ | SL＇z |
| โ0－3T6＇t | 10－318＇$\varepsilon$ | โ0－368＇て | 10－3で「て | T0－367＇โ | 20－3＜6＇6 | 20－э97＇9 | 20－3८ナ $\varepsilon$ | て0－ヨて9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3c ${ }^{\text {¢ }}$ ¢ | S＇Z |
| โ0－3T6＇t | 10－3T8＇$\varepsilon$ | โ0－368＇乙 | T0－3で「て | T0－367＇โ | 20－3＜6．6 | 20－э97＇9 | て0－3Lt＇ と | て0－Эマ9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3¢ ${ }^{\text {¢ }}$ ¢ | Sでて |
| โ0－3T6＇t | โ0－3т8＇$\varepsilon$ | โ0－368＇乙 | т0－ヨマでて | T0－367＇โ | 20－3＜6．6 | 20－э9て＇9 | 20－3८ナ $\varepsilon$ | 20－эて9＇โ | ع0－эt9｀ऽ | ع0－360＇โ |  | 2 |
| โ0－3T6＇t | 10－318＇$\varepsilon$ | โ0－368＇て | 10－3で「て | T0－367＇โ | 20－3L66 | 20－э97＇9 | て0－ヨLt＇ ¢ | て0－ヨて9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3ç＇$\varepsilon$ | SL＇I |
| โ0－3T6＇t | 10－378＇$\varepsilon$ | โ0－368＇乙 | โ0－3で「て | 10－367＇โ | 20－3L66 | 20－э9て＇9 | 20－Э८ナ ¢ | マ0－Эて9＇โ | ع0－эt9＇s | ع0－360＇โ | ¢0－Э¢ ${ }^{\text {¢ }}$ ¢ | S＇T |
| โ0－3T6＇t | 10－3T8＇$\varepsilon$ | โ0－368＇乙 | โ0－3で「て | T0－367＇โ | 20－3＜6．6 | 20－э97＇9 | て0－3८ナ $\varepsilon$ | て0－Эマ9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3¢ ${ }^{\text {¢ }}$ ¢ | Sて＇T |
| โ0－3T6＇t | 10－3t8＇$\varepsilon$ | โ0－368＇乙 | โ0－3で「て | 10－367＇โ | 20－3＜6＇6 | 20－э97＇9 | て0－3Lt＇ ¢ | 20－ヨて9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3ç＇$\varepsilon$ | I |
| โ0－3T6＇t | 10－3T8＇$\varepsilon$ | โ0－368＇乙 | T0－3で「て | T0－367＇โ | 20－3＜6．6 | 20－э97＇9 | 20－3८ナ $\varepsilon$ | て0－Эマ9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－ЭSL＇غ | SLO |
| โ0－3T6＇t | 10－318＇$\varepsilon$ | โ0－368＇て | T0－3で「て | T0－367＇โ | 20－3L66 | 20－э97＇9 | 20－3८ナ $\varepsilon$ | て0－ヨて9＇โ | ع0－эt9＇s | ع0－360＇โ | S0－3c ${ }^{\prime}$＇ | so |
| โ0－3T6＇t | โ0－318＇$\varepsilon$ | โ0－368＇乙 | 10－3で「て | 10－367＇โ | 20－3L6＇6 | 20－э9て＇9 | 20－Э८ナ $¢$ | マ0－Эて9＇โ | ع0－эт9＇¢ | ع0－360＇โ | ¢0－Эs ${ }^{\text {＇}}$ ¢ | s20 |
|  |  |  |  |  |  |  |  |  | 1eg uo | ！5101 fo 10 |  | （4！） 7 |


| 00ع | ¢9＇SくT0を | LL＇68z0を | 86：80t0を | Tく‘をદร0¢ | $8 \mathrm{t}^{\prime} \mathrm{t} 990 \mathrm{E}$ | 68＇T080ع | 6s＇9t60ع | 8ع＇660tを | ST「T9てTを | 66＇てをヤtを | St＇9t9tを | St＇てT8TE | ¢8＇ててOZを | 8＊＊ 0 ¢ててを | 8． L6ちてを |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| عLZLL6＇I | โ̧zて96＇โ |  | 8SLOE6＇I | 60てカt6＇L | ع90＜68＇โ | 6976L8 | ¢9L098＇L | SLちtt8＇T | とてદเて8＇โ | 80Z008＇L | LT08LL＇T | \＆t9tSL | 6Z86Zく＇I | ع9t¢0L＇โ | － |
| $8^{\circ}$ | 七tて89 | †TZ898＊ | tIZ898 | tIZ898 | tโZ898 | TZ8 | †tZ898＊ | ¢tZ898 | カtて | かさて898＊0 | $8^{\circ}$ | tZ898＊0 | 0 | 0 | †tZ8980 |
| てT9Sで＇て | It\＆80T | 99t060＇て | LعOZLO | 9L6ZSO＇て | ৪て乙દદ०＇て | てદLてT0 | くtちt66 | て0Z696 | t66St | t＜9tて6 | てLT968＇โ | SSI698＇I | 6090t8 ${ }^{\text {I }}$ | しゃてO⿺8「 | ع9LLLL＇I |
| SZO＇0 | szo 0 | Szo＇0 | szo＇0 | SZO＇0 | Szo 0 | ¢zo＇o | SZO＇0 | szoo | SZO＇0 | szo＇o | szo 0 | Szo＇o | Sて0＇0 | szo＇o | SてO＊ |
| £โ七¢で0 | さても¢で0 | 8てヤをで0 | S\＆t¢で0 | てももをで0 | 9ttをで0－ | 6tナEて＇ | TStEで0－ | StEで0 | 9ttをで0 | Lعセદで | てても¢で0 | 66\＆\＆て＇ | 9¢\＆て | ১โદદて | てもてをで0－ |
| てع | カ七てZと8＊0 | LTSZを8＊0 | 七て8てを8＊0 | ع＜İદ8＇0 | 89 | IZOt\＆8＇0 | LtSt¢8＊0 | カtISE80 | L†8¢88＊0 | てL9988＊0 | TS9LE8＇0 | 0 | ともてOt8＇0 | 0 |  |
| カせてもくでし | દદ | દદ | LS | Lても08て＇I | Et | Ltto8でI | 6S | ZI | 9tIZ6て＇I | 60 | £9886て＇โ | I | ZLもLOE＇I | I | ع068tદ＇โ |
|  |  | 18tてLて＇I |  |  |  | SO | ャ000Z0＇โ | 60S696＇0 | カt06T6＇0 | 6TS898＇0 | عZ08t8＇0 | 8てSL9L＇0 | 0 | LES999＇0 |  |
| L＇I | SLE9＇โ | ＇I | SZTS＇L |  | SL8E＇T |  | て＇I |  | SLET＇T | S＜O＇I | SZTO＇T |  | $88^{\circ}$ | 0 | SZ92．0 |
| SL | SL |  | SZ9S＇L |  |  |  |  |  |  |  |  |  | SLE60 |  |  |
| 00＋3t | 00 | 00 | 00 | 00 | 00＋ヨヤT「と | 00＋ヨLL | 00＋ヨとt＇て | 00＋ヨZT＇て | 00 | 00＋3LS＇L | $00+\exists \varepsilon \varepsilon \cdot \tau$ |  | โ0－Эを¢＇6 | T0－799 ${ }^{\text {L }}$ | T0－761．9 |
| 00＋3 | 00＋ヨ | 00＋3 | 00＋ | 00＋ | $00+\exists \downarrow \tau$＇$\varepsilon$ | 00 | 00 | 00＋ | 00 | 00＋3LS＇T | 00＋ | 00＋ | โ0－Эを¢＇6 | 20－799＇L | โ0－361 9 |
| 00＋ヨtr＇ | 00＋ヨ26 | 00 | 00＋ | 00＋ | 00 | 00＋ | 00＋ヨとt て | 00＋ | 00＋ 0 ¢8 | $00+3 \angle \mathrm{~S}$＇$\tau$ | 00＋ヨとを | 00 | 6 | $99^{\circ} \mathrm{L}$ | 10－361．9 |
| $00+3 t t$ S | 00＋ヨ26 | $00+\exists 2 \downarrow$ | 00＋396 | 00＋ | $00+3 t \tau \cdot \varepsilon$ | $00+3 \angle L$ | 00＋ヨをt＇て | 00＋ | 00＋ヨย8 | ＋ $3 \angle \mathrm{C}$＇I | 00＋ | 00＋ヨZT＇T | 10－3t¢＇6 | 10－799 | 10－361．9 |
| 00＋3 | 00＋326 | 00＋3 | $00+3$ | 00＋ | $00+3 t \tau \cdot \varepsilon$ | 00＋ | 00＋ヨをt＇て | 00 | 00＋ | 00 | 00 | 00 | โ0－Эを¢＇6 | โ0－799＇L | 0－367＇9 |
| 00＋3 | $00+\exists$ | 00＋ | 00＋ | 00＋ | $0+\exists \downarrow \tau$＇$\varepsilon$ | 00＋ | 00＋ $0^{\text {ctr }}$－ | 00＋ | 00＋ | $00+3 \angle 5$ | 00＋ | 00＋ | โ0－Эを¢＇6 | 10－799＇L |  |
| 00＋3 | 00＋326 | 00＋ヨ | $00+3$ | 00＋ | ＋ | 00＋ | 00＋ヨをt＇て | 00＋ | 00＋${ }^{\text {¢ }}$ 88 | $00+3 \angle \mathrm{~S}$＇T | 00＋ヨยع | 00＋ヨてT＇T | 10－Эャع＇6 | 20－799＇L | 10－3619 |
| 00＋3 | $00+326$ | 00＋ | 00＋396 | 00 | 00＋ヨ | 00 | 00＋ヨをt＇て | 00 | 00＋ | 00＋$\angle 25^{\prime}$ T | 00＋ | 00＋ヨZT＇T | 6 | 799 ${ }^{-}$ | 10－361．9 |
| $00+3 t t$ S | 00＋ヨ26 | 00＋ヨで | 00＋396 | $00+3 t 5 \cdot \varepsilon$ | $00+3 t \tau \cdot \varepsilon$ | 00＋3 | 00＋ $0^{\text {ctr }}$－ | 00＋ |  | てz969s＇L | 00＋ヨยع | 00＋ | T0－3tع＇6 | 10－399＊ | 10－361＇9 |
| $00+3$ ¢ ${ }^{\text {c }}$ | 00＋ヨ26 | $00+\exists 2 \downarrow$ | 00＋ 3 | 00＋ | 00＋ | 00＋ヨ | 00＋ヨとt て | 00＋ | 00＋ 0 ¢8 | $00+3 \angle 5 \cdot \tau$ | 00＋ | 00＋ | โ0－Эャを＇6 | 10－799＇L | 10－361．9 |
| $00+3$ ¢ ${ }^{\text {c }}$ | 00＋326 | 00＋ヨ | $00+$ | 00＋ヨ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | ＋ | $00+$ | 00＋ | โ0－Эも¢＇6 | 20－799＇L | 0－76t＇9 |
| 00＋3 | 00＋ヨZ6 | 00＋ヨ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | โ0－Эを¢＇6 | 10 | 20－36T•9 |
| 00＋3 | 00＋326 | 00＋ヨ | 00＋ | 00 | $00+\exists \downarrow$＇＇$¢$ | 00＋ | 00＋ヨEt | 00＋ | 00＋${ }^{\text {c }}$ 88 | $00+3 \angle$ | 00＋ | 00＋ | 10－Эャع＇6 | 20－399 ${ }^{\text {L }}$ | 10－36199 |
| $00+$ | 00＋ヨZ6 | 00＋ | 00＋ | $00+$ | $00+\exists \downarrow \tau$＇ | 00＋ | 00＋ヨとt て | 00 | 00＋ 0 ¢8 | 00＋ $3 \angle 5$ | 00＋ | 00＋ | 6 | 999 | 10－361．9 |
| $00+3$ ¢ ${ }^{\text {c }}$ | 00＋ヨ26 | 00＋ヨてカ | 00＋ 3 | 00＋ | $00+\exists t \tau \cdot \varepsilon$ | $00+3 L L ' 冖$ | 00＋ヨとt て | 00＋ヨてT＇て | $00+3$ ¢8＇$\tau$ | $00+\exists \angle \mathrm{S}$＇$\tau$ | $00+\exists \varepsilon \varepsilon$ | 00＋ヨてT | โ0－Э¢ | 10－399 | 10－361．9 |
| $00+3 t t$ ¢ | 00＋ヨ | 00＋ヨ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | $00+3 \angle 5$ | 00＋ | 00＋ | 0－ | T0－ | 10－361＇9 |
| 00＋ $3 t t$＇S | 00＋ | 00＋3 | 00＋39 | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 0 | t0 | 0－367＇9 |
| 00＋3 | 00＋ヨ | 00＋ | 00＋ | 00 | 00＋ヨャT＇$¢$ | 00＋ | 00＋ | 00 | 00＋ | 00＋ヨLS | 00＋ | 00＋ | 10－ | T0 | โ0－36โ•9 |
| 00＋3 | $00+326$ | 00＋ヨ | 00＋796 | 00＋ | 00 | 00 | 00＋ヨとt | 00 | 00＋ヨย8 | 00 | 00＋ | 00 | โ0－Эャع＇6 | 99 | 10－361＇9 |
| 00＋ $3 t t$＇S | 00＋ヨ26 | 00＋ヨで | 00＋ $396 \cdot \varepsilon$ | 00＋3ts | $00+3 t \tau \cdot \varepsilon$ | $00+3 \angle L$ | 00＋ヨをt＇て | 00＋ヨZL | 00＋${ }^{\text {c }} 8$ | 00＋ $3 \angle 5$ | 00＋ヨยع | 00＋ヨZ1 | 10－Эャを | 10－799 | 0－ |
| $00+3$ ¢ ${ }^{\text {c }}$ | $00+\exists 26{ }^{\text { }}$ | 00＋ヨで | $00+796 \cdot \varepsilon$ | $00+3 t 5 \cdot$ | $00+\exists t \tau \cdot \varepsilon$ | $00+3 \angle L ' 冖$ | 00＋ヨとt て | 00＋ヨで | 00＋ 0 ¢8 | $00+\exists \angle \mathrm{S}$＇$\tau$ | 00＋ヨとを | 00＋ヨマT | 10－ | 10－799 | 10－361．9 |
| $00+3 t t$ ¢ | $00+326$ | 00＋ヨで | 00＋ 3 | 00＋3ts | $00+3 t \tau \cdot \varepsilon$ | $00+3 \angle L ' 冖$ | 00＋ヨをtて | 00＋ | 00＋ | $00+3 \angle 5 \cdot \tau$ | 00＋ | $00+\exists 2 T$ 「 | 0 | 20－799 | 0－76\％ 9 |
| 00＋3 | 00＋ | 00＋ | 00＋ | 00＋ | ＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | 00＋ | T0－ | T0－ | 10－361．9 |
| 00＋3tr＊ | $00+\exists Z 6{ }^{\text {¢ }}$－ | 00＋ | 00 | 00＋ | 00 | 00＋ | 00＋ | 00 | 00＋ | 00＋ $3 \angle 5$ | 00＋ | 00＋ヨてT＇T | T0－3tع＇6 | T0 | 10－3619 |
| $00+3$ ¢ ${ }^{\text {c }}$ | 00＋ヨて6 | 00＋ヨで | $00+796 \cdot \varepsilon$ | 00＋ | $00+\exists t \tau \cdot \varepsilon$ | 00＋ | 00＋ヨとt て | 00＋ | $00+3 ¢ 8$＇$\tau$ | $00+3 \angle \mathrm{~S}$＇$\tau$ | 00＋ヨとを | 00＋ | T0－3tを＇6 | 10－399＊ | 10－361．9 |
| $00+3 t t$ S | 00＋ヨZ6＇t | 00＋ヨてt＇t | 00＋ $396 \cdot \varepsilon$ | $00+\exists \downarrow \varsigma^{\prime} \varepsilon$ | $00+3 t \tau \cdot \varepsilon$ | $00+3 L L ' \tau$ | 00＋ヨをt＇て | 00＋ヨで「て | $00+3 \varepsilon 8$＇$\tau$ | $00+3 \angle 5 \cdot \tau$ | $00+\exists \varepsilon \varepsilon$ | $00+\exists Z \tau$ | T0－3tを＇6 | 10－399＊ | 10－361． |
| 00＋ $3 t t$ S | $00+\exists Z 6{ }^{\text {¢ }}$－ | 00＋ヨてt＇t | 00＋ $796 \cdot \varepsilon$ | $00+3 \mathrm{t}$＇$\varepsilon$ | $00+3 t \tau \cdot \varepsilon$ | $00+3 \angle L ' Z$ | 00＋ヨをt＇て | 00＋ヨZT＇て |  | $00+3 \angle \mathrm{~S}$＇T | $00+\exists \varepsilon \varepsilon$ | 00＋ヨてT＇T | T0－Эャを | 10－399 | 0－764•9 |
| $00+3 t t \cdot$ S | $00+\exists Z 6{ }^{\text {¢ }}$－ | 00＋ヨてt＇t | 00＋ $396 \cdot \varepsilon$ | $00+3 \mathrm{t}$＇$\varepsilon$ | $00+3 t \tau \cdot \varepsilon$ | $00+3 \angle L ' Z$ | 00＋ヨをt＇て | 00＋ヨZT＇て | 00＋${ }^{\text {c }} 8$ | $00+3 \angle \mathrm{~S}$＇T | $00+\exists \varepsilon \varepsilon$ | 00＋ヨてT＇T | 10－3ヤを | T0－799 | 0－36 |
| $00+3$ ¢ ${ }^{\text {cos }}$ | $00+\exists Z 6{ }^{\text {¢ }}$－ | 00＋ヨてt＇t | 00＋396 | 00＋ЭtS | $00+3 t \tau \cdot \varepsilon$ | $00+3 \angle L$ | 00＋ $0^{\text {ctr }}$－ | 00＋ヨてT＇て | 00＋ $0^{2} 8$ | $00+\exists \angle \mathrm{S}$＇$\tau$ | $00+\exists \varepsilon \varepsilon$ | 00＋ヨてT＇t | 10－3ャع＇6 | 10－399 | 10－361．9 |
| $00+3 t t$ S | 00＋ヨZ6＇t | 00＋ヨで「 | 00＋ $396 \cdot \varepsilon$ | $00+\exists \mathrm{t}$＇$\varepsilon$ | $00+3 t \tau \cdot \varepsilon$ | $00+3 \angle L ' Z$ | 00＋ヨをt＇て | 00＋ヨZT＇て |  | $00+3 \angle \mathrm{~S}$＇T | $00+\exists \varepsilon \varepsilon \cdot \tau$ | 00＋ヨてT＇T | T0－3tع＇6 | 10－399＇L | 0－3619 |
| $00+3$ ¢ $0^{\text {c }}$ | $00+\exists Z 6{ }^{\prime} \downarrow$ | $00+\exists$ です | $00+796 \cdot \varepsilon$ | $00+\exists \downarrow \varsigma^{\prime} \varepsilon$ | $00+\exists t \tau \cdot \varepsilon$ | $00+3 \angle L ' 冖$ | 00＋ヨとt て | 00＋ヨで＇て | $00+3 ¢ 8$＇$\tau$ | $00+\exists \angle 5^{\prime} \tau$ | $00+\exists$ ¢＇$\tau$ | 00＋ヨZT「โ | T0－3tを＇6 | 10－399＇L | 10－36199 |
| 00＋ヨカt＇s | $00+\exists Z 6{ }^{\prime} \downarrow$ | $00+\exists$ です | $00+796 \cdot \varepsilon$ | $00+\exists \downarrow \varsigma^{\prime} \varepsilon$ | $00+\exists t \tau^{\prime} \varepsilon$ | $00+3 \angle L ' 冖$ | $00+3 \varepsilon t$ て | $00+\ni$ くて＇て | $00+3 \varepsilon 8 \cdot \tau$ | $00+\exists \angle \mathrm{S}$＇$\tau$ | $00+\exists \varepsilon \varepsilon \cdot \tau$ | $00+\exists Z T \cdot \tau$ | 10－3tを＇6 | 10－399＇L | 10－36199 |

## 6063 Aluminum

## Angle of Deflection

| OSL80 | SZI8＊0 | 00S $L^{\circ} 0$ | S $289^{\circ} 0$ | OSZ9．0 | Sz9s 0 | 00050 | SLEt＇0 | OSLE＇0 | SZTE＊0 | OOSて＇0 | S $588 \mathrm{~T}^{\circ} 0$ | OSZT＇0 | SZ900 | （4！） 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $60 \cdot \varepsilon$ | 91．t | $\varepsilon L$ S | てT8 | 68 ＇II | てT「8 | ع0＇62 | てS＇6t | 七＜＇t6 | とで06I | カガカ9t | 98． 29 ¢ | ¢0．tetL | 98．9688ıT | Sot |
| 20｀$\varepsilon$ | $90 \cdot$＇ | 09 ¢ | $\varepsilon 6 \%$ | โ9＇โ1 | $69.2 \tau$ | ャع＊8て | ャع＇8＞ | 9s．68 | T＜＇¢8 | $8 \varepsilon^{\circ} \mathrm{\varepsilon}$ ¢ | โ6てをャโ | てI＇tSZL | 66＇S9091T | sz＇0T |
| ¢6＇て | $96 . \varepsilon$ | 96＇S | $\varepsilon L^{\circ} L$ | てع＇ıI | $9 て ゙ く \tau$ | S9＇Lて | 91＇くt | Lع＇$<8$ | 8T＇T8โ | てとでカ | 96＊6ET | 61＇LLOL |  | OL |
| L8＇Z | L8＇$\varepsilon$ | てع＇ऽ | ts．L | to＇tI | \＆8．9โ | 56．92 | 86 ＇St | 61＇s8 | ¢9＇9くt | Lて＇tet | て0＇६9ยโ | 9て＇0069 | とて＇totolt | SL＇6 |
| 08.2 | LL＇$\varepsilon$ | 6 L ＇S | ¢ ¢ ${ }^{\text {c }}$ | 92.0 ¢ | 0 0ヶ9 | 9 9\％9て | $08 . t \square$ | $00 \cdot \varepsilon 8$ | で「てくし | でOで | L0．8てをโ | દと＇દて૮9 | ऽ¢＇દLSLOT | S．6 |
| \＆L＇乙 | L9＇$\varepsilon$ | ¢0＇s | St＇L | $\angle \square^{\circ} 0$ | 96 S | Ls＇š | て9＇\＆ヶ | 28．08 | 65＇L9T | St＇60t | てT•®6てT | 0t＇9tc9 | 8ヵ＇でくt0 | SZ＇6 |
| 59＇z | L¢＇$\varepsilon$ | t6＇t | 96.9 | ${ }_{61}$ OT |  | $88 . \downarrow て$ | らがで | 79．8L | 90 ＇६9โ | 60＇86を | LT＇8SてT | くガ69¢9 | 09 ＇tโ6T0 | 6 |
| $85^{\prime} \mathrm{Z}$ | くヤ゙غ | 8L＇も | $\angle L \cdot 9$ | L6． 6 | OT＇sI | $66^{\prime} \dagger$ ¢ |  | St．9L | \＆ऽ＇8SI | ع0＇$\angle 8 \varepsilon$ | てて＇とてて！ | SS＇Z6T9 | てL＇08066 | SL＊8 |
| Ts＇て | L®＇$غ$ | เ9＇ャ | LS＇9 | 29.6 | $\angle 9 . \downarrow \tau$ | 0s＇\＆z | 60\％ 0 | Lでもく | 00 ＇tSI | 86 ＇SLE | Lで88けt | 29＇st09 | ヤ8：6ちて96 | S＇8 |
| \＆゙て | Lでદ | Ts＇t | $88^{\prime} 9$ | ャع＇6 | ャでけ | โ8＇で | โ6．88 | 80＇ZL | くが 6 TI | て6＇t9を | てع＇ยऽธT | 698885 | 96：8でと¢6 | Sで8 |
| 9 9＇て $^{\text {c }}$ | $\angle \tau \cdot \varepsilon$ | LE＇も | 619 | $90 \cdot 6$ | โ8＇$¢ \tau$ | で＇てて | عL＇L¢ | 06.69 | カ6＇tカI | 98 ¢ $¢ ¢$ | Lع＇8ItI | 9＜＇t99s | 60＇88506 | 8 |
| 8 8＇て $^{\text {c }}$ | L0＇$\varepsilon$ | \＆て＇も | 66 S | 8L＇8 | $8 \varepsilon^{\prime} \varepsilon \tau$ |  | ¢s＇9¢ | TL＇L9 |  | $08 . て \downarrow$ ¢ | で「と80T | ع8＇t8ts | LでLSLL8 | SL＇L |
| しでて | L6＇z | OT＇カ | 08.5 | $67 \cdot 8$ | ャ6てT | $\varepsilon \iota^{\circ} \mathrm{Oz}$ | L¢＇ऽ | \＆¢＇¢9 | 88 ＇ऽ¢ | ヤく＇tદを | くヵ8t0T | 06．LOES | દと＇92678 | S＇L |
| カt＇z | L8＇ | $96 \cdot \varepsilon$ | t9＇s | Lて＇8 | Ts＇てI | ＋0．0て | $6 \chi^{\prime} \downarrow \varepsilon$ | ૬¢＇६¢ | ธع＇tદโ | 69＇0てを | 乙ऽ．ยโOT | L60¢TS | St＇S6078 | SZ＇L |
| $90 \cdot$ \％ | 8L＇z | 28＇$\varepsilon$ | Lt＇s | ع6．L | 80 ＇てI | ¢¢＇6โ | โ0＇६ย | 9โ＇t9 | て8＇9てT | \＆9＇60¢ | 85＇8＜6 | t0＇ts6t | 8S＇t9z6L | L |
| $66^{\prime}$ | $89{ }^{\circ}$ | $69^{\circ} \varepsilon$ | てて｀ | t9 ${ }^{\circ}$ | S9＇It | 99.81 | ¢8＇โ¢ | 86.85 | 6でてZI | LS＇862 | ع9＇と๒6 | IT＇LLL | 0L＇をとも9 | SL＇9 |
| 26．I | $85^{\prime}$ Z | ¢s＇$غ$ | ع0＇s | $9 \varepsilon^{\circ} \mathrm{L}$ | てでした | $\angle 6.2 \tau$ | 99．0¢ | 6L＇9s | 9ぐくtI | Ts．L82 | 89 ＇806 | 81．009t | 28＇zo9\＆ | S＇9 |
| カ8＇โ | $8{ }^{\circ} \mathrm{C}$ | นナ $\varepsilon$ | \＆8＇$\downarrow$ | $80^{\circ} \mathrm{L}$ | 6L＇0T | $8 \chi^{\prime}<\tau$ | $88^{\circ} 62$ | T9＇ts | カでとโ！ | St＇9Lて | عL＇¢L8 | Sて＇とてtt | 76＇TLLOL | Sで9 |
| $\angle L \cdot \tau$ | $88^{\prime}$＇ | $8{ }^{\prime}$＇$\varepsilon$ | 79＇t | 64＇9 | $980 \tau$ | $65^{\prime} 9 \tau$ | $0 ¢ \cdot 8 乙$ | ででて | Tく ${ }^{\text {¢ }}$ ¢ | 68 ＇s9z | 8L＇888 | てど9ちても | L0＇tb6L9 | 9 |
| $69^{\prime}$ I | $8 て ゙ て$ | $\dagger \dagger^{\prime} \varepsilon$ | St＇t | LS＇9 | 26.6 | 06 S | で̇して | ャて＇0s | 8T＇t0T | ャع＇tsz | ع8＇६08 | 68＇690t | 61．0tts9 | SL＇S |
| て9＇โ | $8 \mathrm{I}^{\prime} \mathrm{Z}$ | $00 \cdot \varepsilon$ | sz＇t | દて＇9 | 676 | OZ＇st | t6＇sz | 90.88 | 59．66 | $8 て$ をャて | 88＇89 | 9 t ＇Z68E | โع＇6くてて9 | S＇s |
| SS＇I | $80 \cdot$ \％ | L8＇て | 90 ＇t | t6＇s | $90 \cdot 6$ | TS＇t | 92＇ャて | $\angle 8.5 \bigcirc$ | てT＇s6 | てて＇て\＆て | દ6＇દદL | ¢¢＇STLE | ど「8tt6s | Sて＇S |
| $\angle \checkmark^{\prime}$ I | $86^{\prime}$ I | \＆L＇乙 | $\angle 8 . \varepsilon$ | 99 ¢ | \＆9＊8 | 乙8＇$\chi^{\text {¢ }}$ | 85＇をて | $69 . \varepsilon \square$ | 6¢＇06 | 9T‘tてZ | 86869 | 09 8८¢¢ | ¢s．＜T99s | 5 |
| 0ヵ＇I | $88^{\prime}$ T | $65^{\prime}$ て | L9＇$\varepsilon$ | $8 \varepsilon^{\prime}$ S | OZ＇8 | $\varepsilon \tau^{\prime} \varepsilon \tau$ | 0ガてて | OS＇切 | 90.98 | OT＊Otて | ع0＇t99 | L9＇т9を์ | 89＇98Lદร | SL＇t |
| દદ＇โ | $8 L^{\prime}$＇ | 9 t ＇ | $88^{\circ} \mathrm{E}$ | OT＇S | LL＇L | カカでて | てでして | てع＇6を | ع¢＇t\％ | 50．66I | 80＇629 | ヤく＇t8tを | 08＇S¢60s | s＇t |
| Sて＇T | 89＇$\tau$ | てと＇て | $6 て$ ¢ | น8＇$\downarrow$ | દと＇L | SL＇tI | カ0．0て |  | 00＇LL | 66.88 L | عโ＇t6s | L8＇L008 | て6＇もてて8ヵ | Sて＇t |
| 81＇โ | $65^{\circ} \mathrm{L}$ | 81＇て | $60^{\circ} \varepsilon$ | \＆ร＇† | 06.9 | 90.15 | $98.8 \tau$ | S6＇も | くがてL | ع6\％9LT | $6{ }^{1} 6 \mathrm{SS}$ | 88.0 ¢82 | t0＇t6zSt | $\dagger$ |
| It＇T | $66^{\prime}$ T | S0＇z | $06 \%$ | Sて＇も | $\angle \rightarrow 9$ | $\angle 800$ | $69.2 \tau$ | 9L＇てを | ャ6\％ 29 | L8．59T | ャて＇ぃてs | ¢6＇と¢9\％ | くT＇を9ちで | SL＇$\varepsilon$ |
| ع0＇โ | $6 \varepsilon^{\prime} \tau$ | T6＇${ }^{\text {I }}$ | TL＇z | $96 \cdot \varepsilon$ | ＋0＇9 | 89.6 | โ¢9\％ | $85^{\circ} 0 \varepsilon$ | โヵ＇\＆9 | \％8＇tSt | 6て＇68t | て0・くぃて | 6でてを96を | ¢＇¢ |
| 96.0 | 6て＇T | $\angle L ' \tau$ | ts＇て | $89^{\circ} \varepsilon$ | t9＇s | 86.8 |  | 0ヶ＊8て | 88.85 | 9L＇をカT | $t \varepsilon$＇tSt | 6000¢z | しヤ＇T0898 | Sて＇દ |
| 88.0 | 6T＇ธ | ＋9＇โ | てと＇て | $0{ }^{\circ} \mathrm{\varepsilon}$ | 8 T ¢ | 6て＇8 | St＇tI | で＇92 | ¢ $\varepsilon^{\prime \prime}$ ¢ | 0く＇そ६โ | 686 ¢ヶt |  | \＆¢．0८6๕์ | $\varepsilon$ |
| $65^{\circ} 0$ | $66^{\circ}$ | $60^{\circ}$ โ | SS＇T | 9 9＇て | St＇$\varepsilon$ | ¢¢｀¢ | \＆ヵ＊ | くがくI | ャて＇9を | 9t＇88 | $65^{\circ} 6 \mathrm{LZ}$ | ガSくカT | て0＇Lt9 ${ }^{\text {coz }}$ | て |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  | （4！） 7 |


| OOSL＇T | SL89 ${ }^{\text { }}$ | OSZ9 ${ }^{\text { }}$ | SZ9s ${ }^{\text {¢ }}$ | 000s ${ }^{\text {T}}$ | SLEt＇T | OSLE＇L | SZTE＇L | OOSて＇し | SL8T ${ }^{\text {¢ }}$ | OSZİโ | SZ90＇I | 0000 ${ }^{\prime}$ | SLE6＊ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 61.0 | てで0 | 9で0 | $00^{\circ}$ | $98^{\circ}$ | でロ | LS ${ }^{\circ}$ | 19＊0 | 七く＇0 | 16．0 | ¢ ¢ ${ }^{\text {c }}$ | で「 | 18＇โ | ऽદ＇て |
| 61.0 | てで0 | sて＇0 | $0 \mathrm{O}^{\circ}$ | ¢¢＇0 | 切0 | OS ${ }^{\circ}$ | $09^{\circ}$ | $\varepsilon L^{\circ}$ | 68.0 | IT＇$\downarrow$ | $6 \varepsilon^{\prime}$ I | LL＇I | $6 て ゙ て$ |
| 810 | Lで0 | sで0 | $67^{\circ}$ | ャع＊ | Ot＇0 | $8{ }^{\circ} 0$ | $85^{\circ}$ | TLO | $\angle 8.0$ | 80＇โ | $9 \varepsilon^{\prime}$ I | $\varepsilon L^{\prime}$ I | カでて |
| 8t．0 | しで0 | ャで0 | $87^{\circ}$ | દと＊ | $6 \varepsilon^{\circ}$ | $\angle \square^{\circ}$ | $\angle S^{\circ} 0$ | $69^{\circ}$ | 58.0 | SO＇I | てと＇โ | 89＇โ | 8t＇て |
| $8 \mathrm{I}^{\circ}$ | OZ＇0 | ャで0 | $87^{\circ}$ | て¢＊ | $88^{\circ}$ | $97^{\circ}$ | SS＇0 | $\angle 9^{\circ}$ | ع80 | て0＇โ | 6 6＇I $^{\text {l }}$ | t9＇I | てT＇て |
| $\angle T 0$ | Oで0 | とで0 | Lて＇0 | てと＇0 | Lع＇0 | Sto | tS．0 | 59\％ | 08.0 | 00＇โ | Sて＇I | 09＇I | LO＇て |
| $\angle T 0$ | 610 | てで0 | 920 | โع＇0 | $9 \varepsilon^{\circ}$ | 切0 | 乙S＇0 | 79 0 | 8L0 | L6．0 | てて＇し | $99^{\prime}$ I | 10＇て |
| $9{ }^{\text {\％}} 0$ | 610 | てで0 | sて＇0 | $0{ }^{\circ} 0$ | ¢ $\underbrace{\circ}$ | でフ | ts 0 | 29＊0 | 9 $L^{\circ} 0$ | 七6．0 | 6I＇I | TS＇I | $96 \cdot$ T |
| 910 | $85^{\circ}$ | Lて＊ | szo | $67^{\circ}$ | 七ع＊ | 切0 | $67^{\circ}$ | 090 | 七ぐO | 26．0 | SI＇I | $\angle \square^{\prime}$ | 06＇ |
| St＇0 | $8 \mathrm{I}^{\circ}$ | OZ＇0 | ャで0 | $87^{\circ}$ | દと＇0 | Ot＇0 | $8 \mathrm{t}^{\circ}$ | $85^{\circ}$ | てL＇O | 68.0 | てI＇โ | $\varepsilon \iota^{\prime}$ T | S8＇T |
| St＇0 | LI＇0 | O2＇0 | とで0 | LでO | てع＇0 | $6 \varepsilon^{\circ}$ | $\angle \square^{\circ}$ | $\angle S^{\circ}$ | OLO | $98^{\circ}$ | 80＇I | $8 \varepsilon^{\prime}$ I | 6L＇T |
| カT0 | LTO | $65^{\circ}$ | てて＊ | 920 | โع＇0 | Lع＇0 | Sto | ¢S＊ | $\angle 9^{\circ}$ | 78.0 | SO＇I | $\downarrow \varepsilon^{\prime}$ I | $\varepsilon L^{\prime}$ I |
| 七T0 | 910 | $65^{\circ}$ | てで0 | $92^{\circ}$ | $0 \chi^{\circ}$ | $98^{\circ}$ | 切0 | દร＊ | ¢9\％ | 18．0 | て0＇โ | $0 \chi^{\prime}$ I | 89＇โ |
| Et＇0 | ST＇0 | $8 \mathrm{I}^{\circ}$ | で0 | sでo | $67^{\circ} 0$ | ¢ $\underbrace{\circ}$ | でロ | TS＊ | ع9＊0 | 8LO | $86^{\circ}$ | Sて＇I | て9＇โ |
| عt＇0 | St．0 | LTO | Oて＇0 | ャで0 | 8で0 | ャع＊ | 切0 | 05．0 | โ9\％ | 9L＇0 | S6．0 | Lて＇I | LS＇I |
| てT0 | カto | LTO | OZO | とで0 | Lて＇0 | દと＇0 | $6 \varepsilon^{\circ}$ | $8 \mathrm{t}^{\circ}$ | $65^{\circ}$ | $\varepsilon L^{\circ}$ | 26．0 | LI＇T | LS＇I |
| てT0 | カT＊ | $9{ }^{\circ} 0$ | 6I．0 | てで0 | $9{ }^{\text {200 }}$ | โع＇0 | $88^{\circ}$ | $9 \operatorname{to}^{\circ}$ | $99^{\circ}$ | OLO | $88^{\circ}$ | てT＇I | St＇t |
| てT0 |  | St．0 | $85^{\circ}$ | Lて＊ | sでo | $0 \chi^{\circ}$ | $98^{\circ}$ | カガO | ts．0 | L9\％ | 58.0 | 80＇I | 0t＇ |
| IT0 | \＆โ0 | Sto | $\angle T 0$ | O2＇0 | ャで0 | $62^{\circ}$ | ¢¢＇0 | でて | 乙S．0 | 59\％ | 18.0 | t0＇I | $\downarrow \varepsilon^{\prime}$ ¢ |
| It．0 | てL．0 | $\dagger$ T0 | $\angle \mathrm{T} 0$ | O2＇0 | とで0 | 8 8＊0 $^{0}$ | દと＊ | 切0 | OS．0 | $29^{\circ}$ | 8LO | $66^{\circ}$ | 6 6＇I $^{\text {l }}$ |
| OT．0 | てT0 | カT0 | 91．0 | $65^{\circ}$ | てで0 | Lて＇O | て¢ 0 | 680 | $87^{\circ}$ | $65^{\circ}$ | SLOO | S6．0 | とて＇โ |
| OT． 0 | ［10 | \＆1．0 | St＇0 | $8 \mathrm{~T}^{\circ}$ | Lで0 | sて＇0 | โع＇0 | $\angle \varepsilon^{\circ}$ | $96^{\circ}$ | $\angle S^{\circ} 0$ | TLO | 16．0 | LT＇T |
| $60 \cdot 0$ | It＇0 | てT0 | tio | $\angle T 0$ | O2＇0 | ャで0 | 6 6＊0 $^{\circ}$ | ऽ¢0 | とャ0 | tS＇0 | $89^{\circ}$ | $98^{\circ}$ | てT＇T |
| $60 \cdot 0$ | OT＇0 | てT0 | tio | $9{ }^{\circ} \mathrm{O}$ | 610 | とで0 | $8 \mathrm{Cl}^{\circ}$ | $\downarrow \subset \circ$ | 切0 | TS．0 | 79 0 | 28.0 | 90＇โ |
| $80 \cdot 0$ | OT＇0 | IT0 | \＆โ＇0 | St．0 | $8 \mathrm{I}^{\circ}$ | てで0 | 9 9＊0 $^{\circ}$ | て¢＊ | $6 \varepsilon^{\circ}$ | $66^{\circ}$ | 19＊0 | 8LO | T0＇โ |
| 80.0 | $60^{\circ}$ | IT0 | てT＊ | St．0 | $\angle T 0$ | で0 | sて＇0 | $0{ }^{\circ}$ | $\angle \varepsilon^{\prime} 0$ | 9t＊ | $85^{\circ}$ | $\varepsilon L^{\circ} 0$ | S6．0 |
| $\angle 0.0$ | $60^{\circ} 0$ | OT．0 | てT0 | $\dagger$ T0 | $9{ }^{\text {\％}} 0$ | 610 | とで0 | $87^{\circ}$ | ऽ ${ }^{\circ} 0$ | Etio | tS 0 | $69^{\circ}$ | 68.0 |
| $\angle 0 \cdot 0$ | $80^{\circ}$ | $60 \cdot 0$ | tio |  | St＇0 | $8 \mathrm{I}^{\circ}$ | てで0 | LでO | દદ＇0 | Ot＇0 | TS．0 | 59.0 | 78.0 |
| $90 \cdot$ | LO＇0 | $60^{\circ}$ | OT． 0 | てT0 | 七I\％ | $\angle T 0$ | O2＇0 | sて＇0 | 0．0 | $88^{\circ}$ | $\angle \square^{\circ}$ | 09.0 | 8LO |
| 90.0 | LO＇0 | 80.0 | $60^{\circ}$ | ITO | عt＇0 | $9{ }^{\circ} \mathrm{O}$ | 61．0 | とで0 | $82^{\circ}$ | ऽ¢＊ | tro | $99^{\circ} 0$ | $\varepsilon \angle \circ 0$ |
| 90.0 | 90\％ | $\angle 0^{\circ}$ | $60^{\circ}$ | OT． 0 | てI＇0 | St．0 | $\angle T 0$ | で0 | $9{ }^{\prime} 0$ | て¢0 | 切0 | 乙， 0 | $\angle 9^{\circ}$ |
| to 0 | ＋0\％ | SO＇0 | $90^{\circ}$ | LO＇0 | 80 | OT．0 | てT＊ | カT0 | $\angle L^{\circ} \mathrm{O}$ | てで0 | LでO | ऽ¢＊ | Sto |

## Stress at end of Torsion Bar

| 9It | 6tSLT | S69LI | LS8LT | 9808โ | 6६て8T | 0＜t8T | OtL8T | 89Z6T | 8976I | 89て6T | 89Z6I | 885 29761 | 6S＇L9Z6I |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ¢¢0＜＇T | દร $¢ 9$＇ | 6tt9＇โ | 2T9＇t | T9Ls＇I | t98s＇โ | IZ6t＇T | ててカガT | 8t88＇$\tau$ | 88tع＇L | てカカでし | IZLT＇T | 8508t860 | 98LtET＂0 |  |
| Z8980 | Z8980 | Z8980 | Z8980 | 28980 | Z8980 | Z8980 | Z8980 | Z8980 | Z8980 | 28980 | 28980 | Ettz8980 | カtて898＊0 |  |
| 2018＇โ | 8LLL＇T | 8てtく＇ | 670 ${ }^{\text {c }}$ I | S¢99＇I | 8LT9＇T | 699s＇L | Z60S＇L | を切＇T | ZL9E＇I | \＆โ8て＇T | 2861＇T | ttt06L60 | 6It－3と＇t－ |  |
| SてO＊ | SZO＊ | sて0＇0 | Szo＇0 | szo 0 | SZO＇0 | SZO＇0 | SZO＇0 | SZO＇0 | SZO＇0 | Szo＇0 | SZO＇0 | SZO＇0 | SZO＇0 | （u！）sn！peı पכұои |
| โદદて ${ }^{-}$ | 七てをで0－ | †t\＆で0－ | 66てZ＇0－ | 8Lてで0－ | 9tてで0－ | L6Iで0－ | てZIで0－ | 6661 ${ }^{\circ}$ | 88Lİ0－ | でちT「0－ | 6180 $0-$ | દZSOsE＊${ }^{-}$ | TS8T ${ }^{\text {LOE }}$ | әnje＾q |
| てヤ8＊0 | ても力80 | 69t80 | tos80 | SS80 | \＆T980 | TOL80 | LZ880 | 2060 | 8てع600 | tt860 | S090＇ | とてヤ8LTく0 | โ686＇858－ |  |
| 8てTE＇โ | 68tع＇ | โ92を＇โ | 8t¢ ${ }^{\prime}$ T | tStE＇I | S8SE＇โ | ६SLE＇ | †L6と＇โ | て8で「 | S\＆Lt＇I | ZLtS＇I | 8L89 ${ }^{\text {T }}$ | 8668790＇て | 66988โ＇9 | p／o |
| 59990 | 9t90 | SS9s 0 | TSIS 0 | 9t9ガ0 | てぃちナ0 | 9¢980 | เદtع＊0 | 979でo | てZIでO | 9t9to | ILIT0 | とt650900 | 6600t0 0 | （！）pua Su！qunow fo＾！nbap |
| OSZ8．0 | Sz9Lo | 000 ${ }^{\circ} 0$ | SLE9＇0 | OSLS＇O | SZIS 0 | 00St＇0 | SL8E0 | OSてع＇0 | SZ9で0 | 0002＇0 | SLEL｀O | OSLO＇O | SZTO＊O | ：（u！）pua su！qunow to uo！suam！p әp！s |
| OSL80 | SZT80 | OOSL＇0 | SL890 | OSZ9．0 | SZ950 | 000 ${ }^{\circ}$ | SLEt＇0 | OSLE＇0 | SてTع00 | 00Sて＇0 | SL8t＇0 | OSZT0 | SZ90＊0 | （u！）．eq uo！s．at fo |
| StZ¢¢ | 998Et | 699s | 9てZZL | LعZ96 | と6Ъてદโ | 08006T | ع0LL8乙 | L8Z89t | ع8を978 | 90＋ 32 | 90＋3S | てL6ttolz | 80＋ヨร8＇L | 8 边 |
| ऽโて¢¢ | 998Et | 6995s | 9てzてL | Lعて96 | £6ちてદโ | 080061 | ع0LL8乙 | L8Z89t | ع8\＆978 | 90＋32 | 90＋35 | てL6ttolz | 80＋3¢8＇L | SL＇L |
| SIZS¢ | 9988t | 6995s | 9てzてL | Lદて96 | と6ちて\＆ป | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋32 | 90＋35 | てL6ttolz | 80＋3¢8＇L | SL |
| STZSદ | 998Et | 699s | 9てZZL | L६て96 | と6Ъてદโ | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋ 3 Z | 90＋3S | てL6ttolz | 80＋ヨย8＇L | sz＇L |
| STZSદ | 998Et | 699s | 9てZZL | L६て96 | と6Ъてદโ | 08006I | ع0LL8乙 | L8Z89t | ع8६978 | 90＋$\ddagger$ Z | 90＋3S | てL6tTOLて | 80＋ 3 ¢8 ${ }^{\circ}$ | L |
| StZ¢¢ | 998Et | 6995s | 9てZZL | L६て96 | と6Ъてદโ | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋ 3 Z | 90＋3S | てL6ttolz | 80＋ $8^{8} 8^{\circ} \mathrm{L}$ | SL＇9 |
| SIZ¢¢ | 9988t | 6995s | 9てzてL | Lદて96 | と6†て¢ป | 08006I | ع0LL8乙 | L8789t | ع8¢978 | 90＋32 | 90＋3¢ | てL6tT0Lて | 80＋3E8＇L | ¢9 |
| SIZS¢ | 9988t | 6995s | 9てzてL | Lદて96 | と6†て¢โ | 08006I | ع0LL8乙 | L8789t | ع8¢978 | 90＋32 | 90＋35 | てL6ttolz | 80＋3¢8＇L | Sで9 |
| StZ¢¢ | 998Et | 699s | 9てZZL | Lદて96 | と6ちてદโ | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋ 32 | 90＋35 | てL6ttolz | 80＋ヨย8＇L | 9 |
| SIZS¢ | 9988t | 6995s | 9てzてL | Lદて96 | と6†て¢ป | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋32 | 90＋3¢ | てL6tT0Lて | 80＋3E8＇L | SL＇S |
| SIZS¢ | 9988t | 6995s | 9てzてL | Lદて96 | と6†て¢ป | 08006I | ع0LL8乙 | L8789t | ع8¢978 | 90＋32 | 90＋35 | てL6ttolr | 80＋388＇L | ¢＇s |
| StZ¢¢ | 998Et | 699s | 9てZZL | Lદて96 | と6ちてદโ | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋ 3 Z | 90＋3S | てL6tTOLて | 80＋ 3 ¢8＇L | sて＇s |
| SIZSદ | 9988t | 6995s | 9てzてL | Lદて96 | と6ちて\＆ป | 08006T | ع0LL8乙 | L8789t | ع8¢978 | 90＋32 | 90＋35 | てL6ttolz | 80＋ 3 ¢8＇L | S |
| STZSદ | 998Et | 699s | 9てZZL | Lદて96 | と6ちて\＆ป | 08006I | ع0LL8乙 | L8て89t | ع8¢978 | 90＋ 3 Z | 90＋35 | てL6ttolz | 80＋ヨย8＇L | SL＇t |
| SIZS¢ | 9988t | 6995s | 9てZてL | Lદて96 | と6ちて\＆โ | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋32 | 90＋35 | てL6ttolz | 80＋3E8＇L | st |
| SIZSદ | 9988t | 6995s | 9てZてL | Lદて96 | と6ちて\＆ป | 08006I | ع0LL8乙 | L8789t | ع8¢978 | 90＋ヨZ | 90＋3S | てL6ttolz | 80＋3¢8＇L | Sでも |
| SIZS¢ | 998Et | 6995s | 9てZてL | Lદて96 | と6†て¢ป | 08006โ | ع0LL8乙 | L8789t | ع8¢978 | 90＋32 | 90＋3S | てL6tT0Lて | 80＋3¢8＇L | † |
| SIZSદ | 998Et | 6995s | 9てZZL | Lદて96 | と6†て¢โ | 08006I | ع0LL8乙 | L8789t | ع8¢978 | 90＋32 | 90＋35 | てL6ttolz | 80＋ $388^{\circ} \mathrm{L}$ | SL＇$\varepsilon$ |
| StZ¢¢ | 998Et | 699s | 9てZZL | Lદて96 | と6ちてદโ | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋ 3 Z | 90＋3S | てL6ttolz | 80＋ヨ¢8＇L | ¢ $\mathrm{s}^{\text {c }}$ |
| SIZS¢ | 998Et | 6995s | 9てZてL | Lદて96 | と6†て¢ป | 08006โ | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋32 | 90＋3¢ | てL6tT0Lて | 80＋3¢8＇L | Sでદ |
| SIZSદ | 998Et | 6995s | 9てzてL | Lદて96 | と6†て¢โ | 08006I | ع0LL8乙 | L8789t | ع8¢978 | 90＋32 | 90＋35 | てL6ttolz | 80＋ $388^{\circ} \mathrm{L}$ | $\varepsilon$ |
| SIZSદ | 998Et | 6995s | 9てZZL | Lદて96 | と6ちて\＆亡 | 08006I | ع0LL8乙 | L8789t | ع8¢978 | 90＋ 3 Z | 90＋3S | てL6ttolz | 80＋ヨย8＇L | SL＇z |
| SIZSદ | 998Et | 6995s | 9てZてL | Lદて96 | と6Ъて\＆โ | 08006I | ع0LL8乙 | L8789t | ع8¢978 | 90＋32 | 90＋39 | てL6ttolz | 80＋3¢8＇L | s＇z |
| STZSદ | 998Et | 699s | 9てZてL | L६て96 | と6ちて\＆亡 | 08006I | ع0LL8乙 | L8て89t | ع8६978 | 90＋ヨZ | 90＋35 | てL6ttolz | 80＋ヨร8＇L | sz＇て |
| STZSદ | 998Et | 699s | 9てZZL | Lદて96 | と6ちてદโ | 08006I | ع0LL8乙 | L8Z89t | ع8६978 | 90＋32 | 90＋3S | てL6tTOLて | 80＋ 3 ¢8＇L | て |
| SIZSદ | 998Et | 6995s | 9てZてL | Lદて96 | と6ちて\＆亡 | 08006I | ع0LL8乙 | L8789t | ع8¢978 | 90＋32 | 90＋35 | てL6ttolz | 80＋3¢8＇L | SL＇I |
| STZSを | 998Et | 699ss | 9てzてL | Lદて96 | と6ちて\＆โ | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋ヨて | 90＋3S | てL6tT0Lて | 80＋3E8＇L | S＇t |
| SIZSE | 9988t | 6995s | 9てzてL | Lદて96 | と6ちて\＆โ | 08006I | ع0LL8乙 | L8789t | ع8¢978 | 90＋32 | 90＋3¢ | てL6ttolz | 80＋3E8 ${ }^{\circ}$ | Sて＇โ |
| STZSદ | 998Et | 699s | 9てZZL | Lદて96 | と6ちてદโ | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋ 3 Z | 90＋3S | てL6ttolz | 80＋ヨย8＇L | I |
| SIZSદ | 998Et | 6995s | 9てzてL | Lદて96 | と6†て¢ป | 08006โ | ع0LL8乙 | L8Z89t | ع8¢978 | 90＋32 | 90＋3¢ | てL6tT0Lて | 80＋3¢8．L | SLO |
| SIZSદ | 998Et | 6995s | 9てzてL | Lદて96 | と6†て¢ป | 08006I | ع0LL8z | L8789t | ع8¢978 | 90＋ヨZ | 90＋35 | てL6ttolz | 80＋ 3 ¢8．$L$ | so |
| SIZSE | 998Et | 6995s | 9てzてL | Lદて96 | と6ちて\＆亡 | 08006I | ع0LL8乙 | L8Z89t | ع8¢978 | $90+32$ | 90＋35 | てL6tTOLZ | 80＋ヨع8＇L | szo |
|  |  |  |  |  |  |  |  |  |  |  | （！sd） 小eg uo！suo u u ssadis |  |  | （u！） 7 |


| SてT9T | 6LT9T | 9とて9I | S6て9โ | LSE9T | Lてヤ9 | 88t9 | 6S59T | દદ99T | ITL9T | 〉6＜9T | 1889］ | †L69 | ELOLT | 6LTLL | ع6ZLT |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $900{ }^{\circ}$ | 6T66 ${ }^{\text {T }}$ | عLL6 ${ }^{\text { }}$ | とて96＊ | 89t6 ${ }^{\text {T }}$ | 8086 ${ }^{\text {T }}$ | てヤI6「 | TL68 ${ }^{\text {T}}$ | E6L8＇โ | 8098 ${ }^{\text {T }}$ | STも8 $\tau$ | عLZ8＇โ | 2008 ${ }^{\text {² }}$ | 8LL＇L | 9tS ${ }^{\prime}$＇ | 86てL｀T |
| 28980 | Z898＊0 | 28980 | 2898＊0 | Z898＊ | Z898＊0 | て8980 | て8980 | 2898＊0 | 2898 0 | Z898．0 | 28980 | 2898＊ | 2898 0 | Z8980 | Z8980 |
| L8SI＇て | ヤてもし「て | 9Sてİて | と801て | S060² | ZLO＇Z | દSO＇乙 | てદદ0｀て | LZTO｀て | 七T66＊ | Z696 ${ }^{\text { }}$ | 976 ${ }^{\circ}$ | LIZ6 ${ }^{\text {I }}$ | 1968 ${ }^{\text {L }}$ | Z698 ${ }^{\text {L }}$ | 90t8 ${ }^{\text {² }}$ |
| SZO＊0 | SZO＊0 | SZO＊0 | SZO＊0 | SZO＊ | SZO＊0 | ऽてO＊ | SZO＊0 | SZO＊0 | SZO＊ | SZO＊0 | SZO＊ | SZO＊0 | SZO＊ | SZO＊ | SZO＊0 |
| 七\＆で0－ |  | ても\＆で0－ | てもとで0－ | とャをで0－ | とゅをて＇0－ | 七七عで0－ | Stをで0－ | Sャをで0－ | StEて＇0－ | SカEで0－ | StEて＇0－ | 七七とて＇0－ | てもعで0－ | 七\＆で0－ | 9とをで0－ |
| 9TE80 | 8โદ8＊0 | てع8＊0 | ててを8＊0 | Sてを8＊0 | 8て\＆8＊0 | てદદ8＊0 | 9عદ8＊0 | 七\＆80 | StE8＊0 | IS\＆8＊0 | 8Sを8＊0 | L9E8＊ | LLE80 | 88を80 | てOt8＊ |
| LTLて | 6ZLZ | てもくでし | SSLて「し | LLでし | L8Lでし | 七08て＇โ | とて8でし | カカ8て「 | 898て＇し | と68て＇โ | して6て＇し | ЄS6て＇โ | 686て＇L | 6Z0¢＇L | SLOE＇L |
| StLt | カてカ | SELE＇L | とてદ＇し | SてLて＇โ | ててでし | STLT＇T | してI＇し | SOLO＇โ | て0＇โ | S696＊0 | 6T6．0 | S898＊0 | 8T8．0 | SL9L＇0 | LTL＇O |
| OSZ8＇ | SZ9L＇L | 000 ${ }^{\text {T }}$ | SLE9 $\tau$ | OSLS ${ }^{\text {L }}$ | SZIS ${ }^{\text {c }}$ | 00St ${ }^{\text {c }}$ | S $\angle 8$ E $^{\text {L }}$ | OSZと＇I | Sて9でโ | 000て＇I | SLEL＇โ | OSLO＇T | SZT0 $\downarrow$ | 00560 | S $\angle 88^{\circ} 0$ |
| OSL8＇I | SZT8 ${ }^{\text {L }}$ | OOSL＇亡 | SL89＇โ | 0SZ9 ${ }^{\text {T }}$ | SZ9s ${ }^{\text {¢ }}$ | 000＇${ }^{\text {T}}$ | SLEt $\tau$ | OSLE＇I | SてTE I | 00Sて＇โ | SL8T＇T | OSZİI | SZ90T | 0000｀ | SLE60 |
| โع8ะ | し・とてても | 8．TL9力 | L 28 TS | － 78 LS |  | L 8872 | 「＇tナて8 | 6．LLE6 | カELOT | OLEZL | S9EtT | Lて891 | 7886T | 9SLEZ | sてL8Z |
| โع8ะ | 「・とてても | 8 | L＇L8IS | I＇も8LS | S $2 \angle L 79$ | L＇88てL | 「＇tナて8 | 6．LLE6 | t\＆ | 0LEZT | S9 | Lて891 | 7886T | 9SLEZ | Z |
| โع8ะ | し・とてても | 8．1L9 | L＇L8IS | I＇も8LS | S $2 \angle L 79$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | カELOT | OLEZL | S9EtT | Lて891 | 7886T | 9SLEZ | sてL8Z |
| โع8ะ | し・とてても | 8＇TL9力 | L＇L8IS | I＇t8Ls | S．$\angle \angle\rangle 9$ | L887L | 「切て8 | 6．LLE6 | ヤعLOT | 0＜とてT | S9EtT | して89โ | 7886I | 9SLEZ | ऽてL8Z |
| โع8ะ | し・とてても | 8．TL9 | L＇L8TS | I＇も8LS | S $2 \angle L 79$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | カELOT | 0LEZT | S9EtT | Lて891 | 7886T | 9SLEZ | sてL8Z |
| โદ8\％ | ・とててて | 8 | $L$ | I＇ | 5 | $L$ | 「＇tナて8 | 6．LLE6 | t | OL | S9 | Lて8 | 7886L | 9SLEZ | て |
| โع8ะ | ・とててて | 8．TL9力 | L＇L8ts | I＇t8Ls | S $2 \angle L \square 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEZT | S9ともT | Lて891 | 7886L | 9SLEZ | sてL8Z |
| โع8ะ | し・とてても | 8＇TL9力 | L＇L8IS | I＇t8Ls | S．$\angle \angle\rangle 9$ | L887L | 「切て8 | 6．LLE6 | カعLOT | 0んとてT | S9をもT | して89โ | 7886I | 9SLEZ | sZL8Z |
| โع8ะ | し・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | S $2 \angle L \square 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9EtT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | 「・とてても | 8＇TL9力 | L＇L8IS | I＇t8Ls | S $2 \angle L \square 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャ | OL | S9E | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | 「・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | S $2 \angle L \square 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9ともT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | ・とてても | 8．TL9力 | L＇L8ts | I＇t8Ls | S．$\angle \angle\rangle 9$ | L887L | 「切て8 | 6．LLE6 | カعLOT | 0んとてT | S9をもT | して89โ | 7886I | 9SLEZ | sZL8Z |
| โع8ะ | 「・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | S $2 \angle L \square 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9ともT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | し・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | S $2 \angle L \square 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9EtT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | 「・とてても | 8．TL9力 | L＇L8IS | I＇t8Ls | s．$\angle \angle 79$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9ともT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | ・とてても | 8．TL9力 | L＇L8ts | I＇t8Ls | S．$\angle \angle\rangle 9$ | L887L | 「切て8 | 6．LLE6 | カعLOT | 0んとてT | S9をもT | して89โ | 7886I | 9SLEZ | sZL8Z |
| โع8ะ | 「・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | S $2 \angle L \square 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9ともT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | 「・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | S $2 \angle L \square 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9ともT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | し・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | S $2 \angle L \square 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9ともT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | ・とてても | 8＇TL9力 | L＇L8ts | I＇t8Ls | S．$\angle \angle 79$ | L887L | 「切て8 | 6．LLE6 | カعLOT | 0んとてT | S9をもT | して89โ | 78861 | 9SLEZ | sZL8Z |
| โع8ะ | 「・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | S $2 \angle L \square 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9ともT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | 「・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | s．$\angle \angle 79$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9ともT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | 「・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | s．$\angle \angle 79$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9をもT | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | し・とてても | 8．1L9力 | L＇L8IS | I＇ヤ8Ls | s．$\angle \angle\rangle 9$ | L88ZL | 「切て8 | 6．LLE6 | ャعLOT | 0んとてT | S9\＆tT | Lて89โ | 78861 | 9SLとて | sZL8Z |
| โع8ะ | し・とてても | 8．1L9 | L＇L8IS | I＇t8Ls | s．$\angle \angle 79$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | ャعLOT | 0LEてT | S9をtL | Lて891 | 7886L | 9SLEZ | sZL8Z |
| โع8ะ | ・とててて | 8．TL9 | L 28 LS | I＇t8Ls | S．$\angle \angle \rightarrow 9$ | L＇88ZL | 「切て8 | 6．LLE6 | 七\＆LOT | 0LEZT | S9ともT | して89 | 7886L | 9SLとて | sZL8Z |
| โع8ะ | 「・とてて૪ | 8．1L9力 | L＇L8IS | I＇ヤ8Ls | S $\angle \angle 779$ | L＇88ZL | 「＇カナて8 | $6{ }^{\circ} \angle L E 66$ | ャعLOT | 0LEZT | S9をt | L2891 | 78861 | 9¢Lとて | SてL8Z |
| โع8ะ | 「・とてても | 8＇LL97 | L＇L8IS | I＇ヤ8LS | S．$\angle \angle \square 9$ | L＇88ZL | 「＇カナて8 | 6＊LLE6 | 十ELOT | 0LEZT | S9EtI | L2891 | 7886T | 9SLEZ | SてL8Z |
| โع8ะ | ・とてても | 8．TL9 | L＇L8ts | I＇t8Ls | S $\angle \angle \square 79$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | 七\＆LOT | 0LEZT | S9ともT | して891 | 7886 | 9̧LEZ | SZL8Z |
| โع8ะ | ・とてても | 8．TL9 | L 28 LS | I＇t8Ls | S．$\angle \angle \rightarrow 9$ | L＇88ZL | 「切て8 | 6．LLE6 | 七\＆LOT | 0LEZT | S9ともT | して891 | 7886 | 9̧LEZ | SZL8Z |
| โع8ะ | 「・とてても | 8＇tL9t | L＇L8IS | I＇も8LS | s．$\angle \angle 79$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | カELOT | OLEZL | S9とt | Lて891 | 7886T | 9SLEZ | sZL8Z |
| โع8ะ | 「・とてても | 8＇tL9t | L＇L8IS | I＇ヤ8LS | s．$\angle \angle \rightarrow 9$ | L＇88ZL | 「＇tナて8 | 6．LLE6 | 七ELOT | OLEZL | S9EtT | Lて89โ | 7886T | 9SLEZ | sZL8Z |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Safety Factor

| I＇6ヵS | E＇S69LI | 9＊9S8LT | をعLI＇9808L | 9＊8\＆て8T | で0くも8T | OtL8T | 9＇ 29761 | 9＇ 29761 | 9＊ 29 26I | 9＊ 29261 | てT88S＊ 29761 | 885＇L926T | p uо pəseq＜－－（！sd）7！w！｜әכue»nриә рәұวә」ло |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 92SL9＇I | 26tt9 $\tau$ | E0ZT9＊ | ZLI609LS＇I | てヤ9\＆S ${ }^{\text {T }}$ | STZ67＇T | IIてカヤ＇I | ヤ8ヤ8¢＇โ | ヤ88TE＇โ | とてももでI | 60ZLT＇I | 9LLS08T86＊0 | LS8LIEI＇0 |  |
| L2898＊ | L2898＊0 | LZ898＊0 | と\＆ヤLて898＊0 | LZ898＊0 | LZ898＊0 | LZ898＊0 | LZ898＊0 | LZ898＊0 | LZ898＊0 | LZ898＊0 | عとヤTて898＊0 | とヵTて898＊0 | （b） 1 ！！＾！！suas yJion |
| 9LLLL＇T | โ8てもL＇โ | E670 ${ }^{\circ}$ T | દ9ES\＆99＇โ | S8LT9 ${ }^{\text {T }}$ | S899＇${ }^{\text {T }}$ | LZ60S＇L | 9てEカt「 | 七てL9¢＇T | TET8て＇T | LZ861＇T | L80tナ06L6 0 | 6IL－ヨع＇カー |  |
| SZO＊0 | SてO＊0 | SZO＊O | SZO＊0 | SZO＊0 | SZO＊0 | SZO＊0 | SZO＊O | SZO＊O | SZO＊ | SZO＇0 | SZO＊0 | SZO＊0 | （u！）sn！pe＾पכұou |
| 七てをで0－ | ャTとて ${ }^{-}$ | 66てて ${ }^{\circ}$ | E8SLLZで0－ | 9ヵてで0－ | L6Lて＇0－ | てZIで0－ | 6661＊0－ | 88LI＇0－ | てIちT＊${ }^{\circ}$ | 6T80＇0－ | 6ZZSOSE＊－ | TS81＊${ }^{\text {² }}$ | ən｜e＾q |
| STちも80 | 889t8＊0 | ヤOS8＊ | દદ9E0SS800 | Iとโ980 | 900 ${ }^{\circ}{ }^{\circ}$ | ヤLて8800 | 2060 | ヤ8て\＆60 | カヤヤ860 | TS090＇โ | を6てZヤ8LTL＇0 | T686 ${ }^{\text {8 }}$ SE－ | วnje＾$\forall$ |
| 68โE＇L | ST9てE＇I | Z8t¢์ I | とヤ69\＆SヤE＇L | 6ヤ8S\＆$\tau$ | LZSLE＇I | StL6E＇I | 9T8てガโ | S\＆くも「 | LTLもS＇I | ع8L89＇โ | と6L668290て | 七66988I＇9 | p／O |
| ヤ09โ9 0 | SSS9S＊0 | SOSTS 0 | で9SSt9t0 | 90カで0 | LSE9E0 | LOETE＇0 | 8Sて9で0 | 80てLで0 | 8ST9T＊0 | 60LIT＊0 | STEも6S090＊0 | T6600T0＊0 | ：（u！）puə su！qunow fo＾！nbəp |
| SZ9LO0 | 000 20 | SLE9 0 | OSLS ${ }^{\circ}$ | SZTS 0 | OOSガO | S $\angle 88^{\circ} 0$ | OSZE 0 | Sて9て＇0 | 0002＇0 | SLEL＇O | OSLO 0 | SZTO＊O | ：（u！）puə su！zunow fo uo！suəu！p әр！s |
| SてT8＊0 | OOSLO | SL89 0 | 0SZ9＊0 | SZ9S＊0 | OOOS 0 | SLEtio | OSLE＊ | SてTE＊O | 00Sて＇0 | SL8T0 | OSZİ0 | Sて90＊0 | （u！）leq uo！sıot fo |
| て0－30て＇と | T0－قカS＇て | T0－3 ${ }^{\text {－}}$＇T | T0－367＇T | T0－360＇T | て0－369 | て0－ヨャT「S | て0－ヨદて＇と | て0－36L＇L | ع0－ヨLE＇8 | ع0－368＇て | 七0－36S ${ }^{\text {S }}$ | S0－ヨย6 ${ }^{\text {c }}$ | 8 |
| し0－ヨ0て＇ | T0－ヨャS＇乙 | โ0－3 ${ }^{\circ}$＇T | T0－コ67＇T | 20－360 | 20－369 | てO－ヨャレ・ | て0－ヨદて＇દ | 20－ $36 L^{\circ}$ | ع0－ヨLદ＇8 | と0－ヨ68＇て | ヤ0－ 36 S ¢ | S0－ヨย6＇โ | SL＇L |
| โ0－ヨ0て＇と | T0－ヨャS＇乙 | T0－ヨ ${ }^{\circ}{ }^{\circ}$ L | T0－ヨ67＇L | T0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャT•S | て0－ヨદて＇と | 20－ $36 L^{\prime}$ T | ع0－ヨLE＇8 | ع0－368＇乙 | カ0－ 36 S ¢ | S0－ヨย6 $\tau$ | S＇L |
| し0－ヨ0て＇ | T0－ヨャS＇乙 | T0－3 ${ }^{\text {－}}$＇ | T0－367＇T | โ0－360＇โ | て0－369 | てO－ヨャT「S | て0－ヨદて＇と | 20－36L＇T | ع0－ヨLと＇8 | と0－368＇乙 | ヤ0－ 36 S ¢ | S0－ヨย6＇โ | Sて＇L |
| て0－ 30 ＇ | T0－ヨャS | T0－3 ${ }^{\text {c }}$＇ | โ0－367＇T | 20－360 | 20－369 | てO－ヨャレ＇S | て0－ヨદて＇દ | 20－ $36 L^{\circ}$ | ع0－ヨLદ＇8 | と0－ヨ68＇て | ヤ0－ 36 S ¢ | S0－ヨย6＇โ | L |
| โ0－ヨ0て＇と | T0－ヨtS＇乙 | โ0－3 ${ }^{\circ}$＇L | T0－367＇T | T0－360T | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャT•S | て0－ヨદて＇と | 20－ $36 L^{\prime}$ T | ع0－ヨLE＇8 | と0－368＇て | カ0－ 36 S ¢ | S0－ヨย6 $\tau$ | SL9 |
| โ0－ヨ0て＇と | T0－ヨャS＇乙 | T0－ $3 \angle 6{ }^{\text {＇}}$ | T0－ヨ6＊＇T | T0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | て0－ヨャT•S | て0－ヨદて＇と | 20－36L＇T | ع0－ヨLع＇8 | と0－368＇乙 | カ0－36S＇S | S0－ヨદ6 $\tau$ | S＇9 |
| て0－ 30 ＇ | T0－ヨャS | T0－ $3 \angle 6{ }^{\text {＇}}$ | T0－ヨ67＇T | โ0－760 | て0－ 369 | てO－ヨャT•S | て0－ヨદて | 20－36L＇T | ع0－ヨLع＇8 | と0－ $368^{\circ}$ て | カ | S0－ヨย6．L | Sて＇9 |
| โ0－ヨ0て＇غ | T0－ヨャS＇乙 | T0－3 ${ }^{\text {¢ }}$＇ | T0－367＇T | โ0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャT・ら | て0－ヨદて＇と | 20－ $36 L^{\circ}$ | ع0－ヨLદ＇8 | と0－ヨ68＇乙 | 70－36S＇S | S0－ヨย6 ${ }^{\text {¢ }}$ | 9 |
| โ0－ヨ0て＇と | T0－قャS＇乙 | T0－ $3 \angle 6{ }^{\text {＇}}$ | T0－ヨ6＊＇T | T0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャT•S | て0－ヨદて＇と | 20－36L＇T | ع0－ヨLE＇8 | と0－368＇て | カ0－ 36 S ¢ | S0－ヨย6 $\tau$ | SL＇S |
| し0－ヨ0て＇ | T0－ヨャS＇乙 | โ0－3 ${ }^{\circ}$－ | โ0－ $367^{\circ}$ L | 20－360 | て0－369 | てO－ヨャT「ら | て0－ヨદて＇દ | 20－ $36 L^{\circ}$ | ع0－ヨLE＇8 | と0－ヨ68＇て | ヤ0－ 36 S ¢ | S0－ヨย6＇โ | S＇S |
| し0－30て＇ | T0－ヨカS＇乙 | T0－ヨ ${ }^{\text {－}}$＇ | T0－367＇โ | โ0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャT・ら | て0－ヨદでと | 20－ $36 L^{\prime}$ L | ع0－ヨLع＇8 | と0－ $368^{\circ}$ て | 70－36S＇S | S0－ヨย6＇โ | Sて＇S |
| โ0－ヨ0て＇と | T0－قャS＇乙 | T0－ $3 \angle 6{ }^{\text {＇}}$ | โ0－ヨ67＇T | T0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャT•S | て0－ヨદて＇と | 20－36L＇T | ع0－ヨLE＇8 |  | カ0－36S ${ }^{\text {S }}$ | S0－ヨย6 $\tau$ | S |
| โ0－ヨ0て＇と | T0－قャS＇乙 | T0－ヨ ${ }^{\circ}{ }^{\circ}$ L | T0－ヨ67＇L | T0－360 | 20－369 | てO－ヨャT•S | て0－ヨદて＇દ | 20－36L＇T | ع0－ヨLع＇8 | と0－ $368^{\circ}$ て | カ0－ 36 S ¢ | S0－ヨย6＇โ | $S L{ }^{\prime}$ |
| し0－ヨ0て＇ | T0－ヨャS＇て | T0－3 ${ }^{\text {－}}$＇T | T0－367＇T | 20－360 | 20－769 | てO－ヨャT＇S | て0－ヨદて＇と | 20－36L＇T | ع0－ヨLE＇8 | と0－368＇乙 | カ0－36S＇S | S0－ヨย6＇โ | S＇カ |
| โ0－ヨ0て＇と | T0－ 3 ¢ $\mathrm{S}^{\prime}$ | T0－3 ${ }^{\text {－}}$＇ | T0－367＇T | โ0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャT•S | て0－ヨદて＇દ | 20－36L＇T | ع0－ヨLと＇8 | と0－368＇乙 | 70－36S＇S | S0－ヨย6＇โ | Sでも |
| โ0－ヨ0て＇と | T0－ 3 ¢ $\mathrm{S}^{\text {C }}$ | T0－3 $26^{\text {＇}}$ | T0－367 $\tau$ | T0－360＇T | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャT•S | て0－ヨદて＇દ | 20－36L＇T | ع0－ヨLع＇8 | と0－368＇乙 | 70－36S＇S | S0－ヨย6＇โ | ฤ |
| โ0－ヨ0て＇と | T0－ヨャS＇乙 | T0－ $3 \angle 6{ }^{\text {＇}}$ | โ0－ $36 \nabla^{\circ} \tau$ | T0－360＇โ | 20－369 | てO－ヨヤT「ら | て0－ヨદて＇غ | 20－36L＇T | ع0－ヨLE＇8 | と0－368＇て | カ0－ 36 S ¢ | S0－ヨย6 $\tau$ | S $\angle \cdot \varepsilon$ |
| โ0－ヨ0て＇と | T0－ヨャS＇乙 | T0－ $3 \angle 6{ }^{\text {＇}}$ | โ0－ヨ67＇โ | T0－360＇โ | 20－369 | てO－ヨャT•S | て0－ヨદて＇と | 20－36L＇T | ع0－ヨLદ＇8 | と0－368＇乙 | カ0－36S＇S | S0－ヨย6 $\tau$ | S＇E |
| โ0－ヨ0て＇દ | T0－ヨャS＇乙 | T0－3 ${ }^{\text {¢ }}$＇ | T0－ヨ67＇T | โ0－360＇โ | 20－ $369^{\circ}$ | てO－ヨャT＇S | て0－ヨદて＇غ | 20－ $36 L^{\circ}$ | ع0－ヨLદ＇8 | と0－ヨ68＇乙 | ヤ0－ 36 S ¢ | S0－ヨย6＇โ | ¢て＇દ |
| โ0－ヨ0て＇غ | T0－قャS＇乙 | T0－3 ${ }^{\text {¢ }}$＇ | โ0－コ67＇T | T0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャレ＇S | て0－ヨદて＇غ | 20－36L＇T | E0－ヨLE＇8 | と0－368＇乙 | ヤ0－ 36 S ¢ | S0－ヨย6＇โ | $\varepsilon$ |
| โ0－ヨ0て＇દ | T0－ヨャS＇乙 | T0－3 ${ }^{\text {－}}$＇T | T0－367＇L | T0－360＇L | Z0－369 | てO－ヨャT＇S | て0－ヨદて＇غ | 20－36L＇T | E0－ヨLE＇8 | と0－368＇乙 | カ0－ 36 S ＇ | S0－ヨย6＇โ | SL＇Z |
| โ0－ヨ0て＇と | T0－ヨャS＇乙 | T0－ $3 \angle 6{ }^{\text {＇}}$ | โ0－ $36 \nabla^{\prime}$ L | T0－360＇T | 20－ $369^{\circ} \mathrm{L}$ | て0－ヨャT•S | て0－ヨદて＇દ | 20－36L＇T | ع0－ヨLع＇8 | と0－ヨ68＇乙 |  | S0－ヨย6 $\tau$ | S＇Z |
| โ0－ヨ0て＇と | T0－ヨャS＇乙 | T0－ $3 \angle 6{ }^{\text {＇}}$ | T0－ $367^{\circ}$ L | T0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャT•S | て0－ヨદて＇と | 20－36L＇T | ع0－ヨLع＇8 | と0－368＇乙 | カ0－36S＇S | S0－ヨย6 $\tau$ | Sて＇Z |
| し0－ヨ0て＇ | โ0－ヨャ¢ | T0－ヨ ${ }^{\text {¢ }}$＇ | โ0－ヨ67＇T | 20－360＇ | Z0－369 | てO－ヨャT•S | て0－ヨદて | 20－36L＇T | ع0－ヨLE＇8 | ع0－368 | カ0－36S＇S | S0－ヨย6 $\tau$ | 乙 |
| โ0－ヨ0て＇દ | T0－ヨャS＇乙 | T0－3 ${ }^{\text {c }}$＇ | โ0－ヨ67＇T | โ0－360＇โ | て0－ $369^{\circ}$ | て0－ヨャT＇S | て0－ヨદて＇દ | 20－ $36 L^{\circ}$ T | ع0－ヨLE＇8 | ع0－ 368 ＇乙 | ヤ0－ 36 S ¢ | S0－ヨย6＇โ | SL＇T |
| โ0－ヨ0て＇と | T0－ 3 ¢ $\mathrm{S}^{\prime}$ | T0－3 ${ }^{\text {－}}$＇ | T0－367＇T | T0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | て0－ヨャT＇S | て0－ヨદて＇દ | 20－36L＇T | ع0－ヨLE＇8 | と0－368＇乙 | 70－36S＇S | S0－ヨย6＇โ | S＇T |
| て0－ヨ0て＇と | T0－قャS＇て | T0－3 ${ }^{\text {－}}$＇T | T0－367＇T | โ0－360＇โ | て0－369 | て0－ヨャT＇S | て0－ヨદて＇と | 20－36L＇T | ع0－ヨLと＇8 | と0－368＇乙 | 70－76S＇S | S0－ヨย6＇โ | Sて＇T |
| โ0－ヨ0て＇غ | T0－ヨャS＇乙 | T0－ $3 \angle 6{ }^{\text {＇}}$ | โ0－ $36 \nabla^{\prime}$ L | T0－360T | て0－369 | て0－ヨャT＇S | て0－ヨદて＇と | 20－ $36 L^{\prime}$ T | ع0－ヨLE＇8 | ع0－368＇乙 | カ0－ 36 S ¢ | S0－ヨย6 $\tau$ | T |
| โ0－ヨ0て＇と | T0－ヨャS＇乙 | T0－3 ${ }^{\text {¢ }}$＇ | โ0－ $36 \nabla^{\prime}$ L | T0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | て0－ヨャT＇S | て0－ヨદて＇と | 20－ $36 L^{\prime}$ T | ع0－ヨLE＇8 | と0－ヨ68＇乙 | カ0－ 36 S ¢ | S0－ヨย6 ${ }^{\text {¢ }}$ | SLO |
| โ0－ヨ0て＇દ | T0－ヨャS＇乙 | T0－3 ${ }^{\text {¢ }}$＇ | โ0－ヨ67＇L | T0－360＇โ | 20－ $369^{\circ} \mathrm{L}$ | て0－ヨャT＇S | て0－ヨદて＇દ | 20－ $36 L^{\circ}$ T | ع0－ヨLE＇8 | ع0－ 368 ＇乙 | ヤ0－ 36 S ¢ | S0－ヨย6＇โ | S．0 |
| โ0－ $30 \chi^{\circ}$ ¢ | T0－ヨャS＇乙 | T0－3 ${ }^{\text {－}}$＇T | T0－36カ＇L | T0－360＇L | 20－ $369^{\circ} \mathrm{L}$ | てO－ヨャI＇S | て0－ヨદて＇と | 20－36L＇T | ع0－ヨLE＇8 | ع0－368＇乙 | 70－36S＇S | S0－ヨદ6＇L | Sて＇0 |
|  |  |  |  |  |  |  |  |  |  | leg u | O！S」O 10 」OłJe | 人1才fes | （u！） |

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|}
\hline 9＇ちてT9t \& で6くT9T \& 9とて9โ \& T｀ऽ6z9โ \& L＇9¢を9โ \& I＇さてカ9「 \& －88t9T \& T＇6S59T \& ع＇દદ99โ \& カ＇ITく9T \& 6．E6L9T \& を＇T889T \& T＇ャL69］ \& 96＇ZLOLT \& T8．8LTLI \& 9＇Z6ZくT \& ¢＇SİLT <br>
\hline ع0900＇z \& 98T66＇L \& LZLL6＇I \& SZZ96 ${ }^{\text {T }}$ \& 9＜9t6 ${ }^{\text {T }}$ \& 9LOE6＇I \& โでT6．I \& 90＜68＇โ \& LZ6L8＇โ \& 9＜098 ${ }^{\text {² }}$ \& 8tโt8＇โ \& てعIZ8＇โ \& IZ008＇I \& LT08LL＇T \& عt9力SL＇T \& を86Zく＇T \& 9七\＆0＜＇I <br>
\hline tZ8980 \& LZ8980 \& tZ898＊0 \& tZ898＊0 \& tZ8980 \& tZ8980 \& tZ898＊ \& IZ8980 \& LZ8980 \& t२8980 \& IZ898＊ \& tZ8980 \& tZ8980 \& †tZ898＊0 \& †tZ8980 \& LZ898＊0 \& TZ8980 <br>
\hline †L8St＇て \& でてけだて \& T9SてI＇て \& โદ80I＇て \& Lt060＇て \& tOZLO＇z \& 867S0＇て \& દてદદ0て \& とLZTO＇z \& でT66＇I \& 2696＇I \& 66St6 ${ }^{\text {＇}}$ \& L9IZ6＇I \& てTI968 ${ }^{\text {I }}$ \& SST698＇I \& T90t8＇${ }^{\text {I }}$ \& 七て018＇I <br>
\hline SZO．0 \& Szo \& SZO．0 \& 0 \& 0．0 \& szo 0 \& szo 0 \& 20 \& Szo＇0 \& sZ0．0 \& $0^{\circ}$ \& szo 0 \& 0 \& ¢Z0＊ \& sZ0 \& でO\％ \& ¢て0＊0 <br>
\hline L6とをで0－ \& SOtEz ${ }^{-}$ \& \＆โt¢て＇0－ \& てZヤをて「0－ \& 8てヤをで0－ \& ¢¢tદて＇0－ \& ItナEて＇0－ \& 9tt\＆て＇0－ \& 6tヤEで0－ \& LStEz＇0－ \& StEz＇0－ \& StEz＇0－ \& カャをで0－ \& ててもをで0－ \& 66を\＆z＇0－ \& 9とをて＇0－ \& เદとで0－ <br>
\hline 6StE80 \& 8LTE80 \& てع800 \& ヤてて\＆8＊0 \& てSてદ8＊0 \& て8て¢80 \& Lโદદ8＇0 \& Lऽह£80 \& ZOt\＆8＇0 \& †StE8＇0 \& ヤT¢E80 \& S8SE80 \& L99と80 \& TS9LE80 \& †て88¢80 \& カてOt80 \& 86Tヶ80 <br>
\hline S9TLZ＇I \& S8ZLZ＇T \& ヤちtLでT \& \＆SSLZ＇I \& \＆0LLて＇I \& 998LZ＇I \& で08て＇I \& เ\＆Z8て＇I \& St78でT \& 9L98て＇T \& โદ68て＇โ \& SIZ6て＇I \& โ\＆ऽ6て＇T \& £9886て＇T \& ヤ88て0と＇T \& $\angle \square \angle O \varepsilon ' T$ \& SLZTE＇T <br>
\hline 9 9tt ${ }^{\text {ctit }}$ \& L6とてヤ＇T \& L७ELE＇T \& 86ててع＇โ \& 8ヵてLでT \& 66IZて＇T \& 60t＜t＇T \& 660ZT「I \& SOLO＇T \& て0＇T \& TS6960 \& T06T60 \& てS89800 \& عZ08t8＇0 \& 8てSL9L0 \& EOLTL＇O \& †59990 <br>
\hline OSZ8＇โ \& SZ9L＇I \& 000 ${ }^{\prime}$ I \& SLE9＇โ \& OSLS＇T \& SZIS＇I \& OOSt＇${ }^{\text {L }}$ \& S $\angle 8 \varepsilon^{\prime}$ T \& OSZと＇โ \& SZ9て＇T \& て＇I \& SLET＇T \& OSLO＇T \& SZTO＇I \& O0S60 \& SL88 \& OSZ8＇0 <br>
\hline 0S 28 T \& SZT8＇T \& 00SL＇T \& S $\angle 89^{\prime}$ T \& OSZ9＇T \& SZ9s＇T \& 000s＇I \& SLEt＇T \& OSLE＇$\tau$ \& SてTE＇T \& 00Sて＇โ \& S $\angle 8$ T＇T \& OSZT ${ }^{\text {d }}$ \& SZ90＇โ \& 0000＇โ \& SLE60 \& OS $\angle 8{ }^{\circ} 0$ <br>
\hline 00＋ヨてヤ \& 00＋ヨัน \& 00＋ヨ78 \& 00＋3ss＇て \& 00＋ $36 \chi^{\prime}$ て \& 00＋350＇z \& 00＋3と8 \& 00＋3Z9＇โ \& 00＋3¢t＇T \& 00＋ 39 ＇$^{\text {T }}$ \& 00＋360＇T \& T0－3Lぢ6 \& －0－ヨてT \& T0－306＇9 \& โ0－3t8＇s \& 0－3¢8＇t \& $6^{\prime}$ <br>
\hline 00＋ 32 \& 00＋ヨut＇ \& 00＋32 \& 00＋ヨss＇z \& 0 \& 00＋3SO＇Z \& $00+3 \varepsilon 8 \cdot \tau$ \& 00＋ЭZ9＇โ \& 00＋${ }^{\text {ct }}$＇T \&  \& 00＋360 \& โ0－3Lナ＇6 \& －0－Э \& －306＇9 \& T0－3t8＇5 \& 0－3 \& 796 $\varepsilon$ <br>
\hline $00+$ \& $00+\exists[\tau \cdot \varepsilon$ \& 00＋ヨ \& 00＋ヨSs＇て \& 00＋36て \& 00＋Э50 \& \& 00＋ヨて \& \& － \& 00＋360 \& \& \& －306．9 \& T0－3t8＇ऽ \& 0－3 \& $96^{\bullet} \varepsilon$ <br>
\hline 00＋ \& $00+\exists \tau \tau \cdot \varepsilon$ \& $00+328$ て \& 00＋قs¢＇z \& 00＋ 36 \& 00＋ヨso＇z \& 00＋388 \& 00＋ヨマ9 \& $00+3$ E \& 00＋ヨ92＇I \& 00＋360＇T \& \& \& 6＇9 \& โ0－эโ8＇ऽ \& 0－3 \& <br>
\hline $00+$ \& 00＋ヨนโ＇ \& 00＋3Z8＇て \& 00＋ヨss＇z \& \& 00＋350＇Z \& 0 \& 00＋ヨZ9＇โ \& 00＋ヨとt \& 00＋ 99 て \& 00＋360＇โ \& โ0－3＜t＇6 \& L0－Эてt 8 \& －069 \& T0－3t8＇ऽ \& －3 \& $6^{\text {¢ }}$ <br>
\hline 00＋ヨて \& 00＋ヨนโ＇ \& $00+378$ \& 00＋ヨss＇z \& 00＋ヨ6て＇て \& 00＋3s0＇z \& 00＋ 88 $^{\prime}$ \& 00＋Э ${ }^{\text {cos }}$＇ \& $00+3 \mathrm{E}$ \& 00＋792＇ \& 00＋360 \& 0－3L \& 0－3てT•8 \& －706．9 \& T0－3t8＇ऽ \& O－ \& 96＇$\varepsilon$ <br>
\hline $00+$ \& $00+\exists[\tau \cdot \varepsilon$ \& 00 \& 00＋Эss＇z \& 00＋362 \& 00＋ヨs0＇て \& 00＋ヨย \& 00＋ヨて \& $00+38$ \& 00＋コ92 \& 00＋360 \& － \& \& 6.9 \& T0－3t8＇ऽ \& 10－3ع \& $6^{\text {＇}}$ <br>
\hline $00+$ \&  \& 00＋ヨZ8＇て \& 00＋ヨsc＇z \& 00＋362 \& 00＋コร0 \& 00＋ヨદ8 \& 00＋Эて9 \& 00＋ヨと \& 00＋ヨ9て＇T \& 00＋360＇T \& \& \& 6.9 \& โ0－3ז8＇ऽ \& $0-3 \mathrm{~s}$ \& $\varepsilon$ <br>
\hline $00+$ \& $00+\exists \tau \tau \times$ \& 00＋ヨて8＇て \& 00 \& 0 \& 00＋350＇乙 \& 0 \& 00＋ヨZ9＇T \& 00＋ヨEt \& 00＋Э9て＇โ \& 00＋360＇I \& T0－3 2 ¢ 6 \& \& 6．9 \& โ0－3t8＇ \& 10－Эと8 \& 96＇$\varepsilon$ <br>
\hline 00＋ \& 00＋ヨัโ「と \& 00 \& 00＋ヨss＇z \& 00＋ヨ6て＇て \& 00＋3S0＇z \& 00＋ヨย8 \& 00＋ヨZ9＇T \& 00＋ヨとt \& 00＋ヨ92 \& ＋360 \& 10－3＜ \& －0－3てT「8 \& 706＇9 \& โ0－Э78＇S \& 10－Эを8 \& $\checkmark^{\prime}$ <br>
\hline $00+$ \& \& 00＋ヨて8＇ \& 00＋3ss＇z \& 00＋762 \& 00＋ヨS0＇て \& $00+\exists \varepsilon$ \& 00＋ヨて \& 00＋ヨとt \& 00＋ヨ9 \& 00＋ 360 \& －3く \& \& ＇9 \& 10－3t8 \& 0－3ع8 \& $\varepsilon$ <br>
\hline $00+$ \&  \& $00+\exists Z 8$＇て \& 00 \& 00＋36て＇て \& 00＋3S0＇Z \& 0 \& 00＋ヨマ9＇ \& 00＋ $0^{\text {ct }}$ \& 00＋392＇T \& 00＋360＇T \& 10－ゴヤ 6 \& \& $6{ }^{\circ}$ \& โ0－3t8＇ऽ \& 10－3と8 \& $\varepsilon$ <br>
\hline $00+$ \& 00 \& 00＋ヨマ8 \& 00＋ヨss＇て \& 00＋36て＇て \& 00＋3S0＇乙 \& 0 \& 00＋ヨZ9＇T \& 00＋ヨとt \& 00＋ヨ9て＇I \& 00＋360 \& T0－3＜ \& \& －306＇9 \& โ0－3t8＇ \& 10－Эを \& 96＇$\varepsilon$ <br>
\hline 00＋ \& 0 \& 00＋ \& 00 \& 0 \& 00＋3SO＇Z \& 00＋3¢8 \& 00＋ヨZ9＇T \& 00＋ヨغt \& 00＋Э9て＇โ \& ＋360 \& \& 0－3てT8 \& 7069 \& T0－3t8＇ऽ \& โ0－3と8＇t \& 996 $\varepsilon$ <br>
\hline $00+$ \& \& 00＋ヨて8＇て \& 00＋3Ss＇て \& 00＋362 \& 00＋ヨs0＇て \& \& \& \& \& 00＋360 \& － \& \& 06＇9 \& โ0－3t8＇ \& 10－Эを \& 96 <br>
\hline $00+$ \&  \& 00 \& 00＋ヨSs＇て \& 00＋ヨ6て＇て \& 00＋3so＇r \& 00＋3¢8＇ \& 00＋ヨて9＇โ \& 00＋ヨEt \& 00＋コ92 \& 00＋ 360 ＇ \& 32 \& －ЭZT「8 \& 069 \& โ0－3ז8＇ऽ \& 0－3ع8 \& 0－396＇ <br>
\hline $00+$ \& $00+\exists \tau \tau `$ \& 00＋ヨて8＇て \& 00 \& 00＋ 367 ＇て \& 00＋350＇Z \& 00＋3 \& \& 00＋ $0^{\text {ct }}$ \& 00＋Э9て＇I \& 00＋360 \& － \& \& 706＇9 \& โ0－3t8＇ \& 0－38 \& $\varepsilon$ <br>
\hline $00+$ \& 00＋ヨut＇ \& 00 \& 00＋ヨss＇て \& 00＋36て＇て \& 00＋ヨS0＇z \& $00+3 \varepsilon 8$ \& 00＋そて9 \& 00＋ $0^{\text {ct }}$ \& ＋Э9て＇โ \& ＋360 \& － \& － \& 7069 \& โ0－3t8＇ \& 10－Эと8 \& ${ }^{\text {® }}$ <br>
\hline $00+$ \& \& 00＋ヨマ8 \& 00＋3Ss＇2 \& \& \& \& \& $00+3 \varepsilon$ \& 00＋ 992 \& 00＋360 \& － \& \& $06^{\circ} 9$ \& โ0－3t8＇ऽ \& 0－コ¢8 \& 0－396＇ <br>
\hline $00+$ \& 0 \& 00＋ヨ \& 00 \& 00＋36て＇て \& 00＋350＇て \& 00 \& 00＋ヨZ9＇โ \& 0 \& 00＋ $0^{\text {a }}$ L \& 00＋360 \& 20－3LT＇6 \& L0－3てl8 \& 069 \& โ0－3t8＇ऽ \& 10－388＇t \& T0－396＇$\frac{1}{}$ <br>
\hline 00＋ \& 00＋ \& 00＋ヨ \& 00＋3Ss＇て \& 00＋36て＇て \& 00＋350＇Z \& 00 \& 00＋ヨZ9＇โ \& 00 \& － 922 \& 00＋360 \& T0－3ムt＇6 \& \& T0－3069 \& โ0－3t8＇ \& 10－3¢8 \& 0－396 $¢$ <br>
\hline 00＋ヨ \& 00＋ヨૅT「と \& 00＋ヨ \& 00＋ヨsc＇ \& 00＋36て＇て \& 00＋3S0＇Z \& 00＋ヨย8 \& 00＋ヨZ9＇T \& 00＋ヨEt \& ＋392 \& ＋360 \& J \& コ \& －306＇9 \& T0－3T8＇ \& $0-3 \varepsilon 8$ \& 96＇$\varepsilon$ <br>

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| ¢ |
| 0 | \& 00＋ヨマ8 \& 00＋ヨss＇z \& 00＋3 \& 00＋ヨs0 \& 00＋ \& 00＋Э ${ }^{\text {co }}$＇ \& 00＋3¢t \& 00＋39 \& 0＋360 \& － 3 \& －Эそ \& 6＇9 \& โ0－эโ8＇ऽ \& $0-38^{\prime \prime}$ \& 0－396 $¢$ <br>

\hline $00+$ \& 00 \& 00＋ \& 00 \& 00 \& 0 \& 00 \& T \& 0 \& 00＋ 39 ＇$\tau$ \& 00＋360 \& T0－3＜t＇6 \& L0－3てt＇8 \& 10－3069 \& T0－3t8＇ऽ \& 0－Эを8 \& ${ }^{\text {® }}$ <br>
\hline 00＋ヨで・ \& $00+3 \tau \tau$ \& $00+\exists$ ¢ ${ }^{\text {2 }}$ \& 00＋3ss＇Z \& 00＋36 \& 00＋3 \& 00＋3 \& 00＋ヨZ9 \& 00＋3 \& 00＋392 \& $00+360$ \& 10－3L \& โ0－Эてt＇8 \& 10－306＇9 \& โ0－3T8＇ \& 10－388 \& โ0－396＇と <br>
\hline 00＋ヨてヤ \& 00＋ヨזr• \& 00＋ヨて8＇て \& 00＋3ss＇て \& 0 \& 0 \& 00＋3 \& ママ \& 00＋ヨEt \& ＋ 392 \& 00＋360 \& －3＜t \& 0－Эてt 8 \& T0－3069 \& โ0－3t8＇ \& －38 \& 96＇$\varepsilon$ <br>
\hline 00＋ヨ \&  \& 00＋ヨて8＇て \& S \& 00＋36て＇て \& 00＋ヨS0＇r \& 00＋ヨ\＆ \& 00＋ЭZ9＇โ \& 00＋ 0 ¢t \& 00＋ 392 \& ＋360 \& －3L \& э \& －3069 \& โ0－3t8＇ऽ \& －3 \& －396 <br>
\hline 00＋ヨで・ \& 00 \& 00＋ヨ \& 00＋ヨss＇ \& 00＋36て \& 00＋3s0＇て \& 00 \& 00＋ヨz9＇โ \& 0 \& 00＋392＇t \& 00＋360 \& 10－3Lb \& 0－3てt＇8 \& 0－3069 \& โ0－3t8＇ऽ \& －э \& 20－796＇દ <br>
\hline 00＋ヨで・ \& 00＋ヨ \& 00＋ヨて8＇て \& 00＋3Ss＇て \& 00＋36て＇ \& 00＋350 \& 00＋3¢8 \& 00＋3Z9＇โ \& 00＋ヨEt \& 00＋392 \& 00＋360＇โ \& $\angle t$ \& 0－Эてt＇8 \& 10－306＇9 \& โ0－3t8＇ \& 10－388 \& 10－396 $¢$ <br>
\hline 00＋ヨてヤ \& $00+\exists \tau \tau \cdot \varepsilon$ \& $00+\exists$ ¢ ${ }^{\text {2 }}$ \& 00＋3ss＇Z \& 00＋36て＇ \& 00＋350＇Z \& 0＋ヨદ8 \& ＋ヨマ9 \&  \& ＋ 392 \& 0＋360 \& F \& ヨ \& T0－306＇9 \& T0－3T8＇ \& －3દ \& 0－396 $¢$ <br>
\hline 00＋ヨで・ \& 00＋コル上＇ \& 00＋ヨて8＇て \& 00＋3ss＇て \& 0 \& 00＋350 \& 00＋ヨع8 \& ＋ヨマ9＇T \& $00+3$ ¢t \& 00＋392 \& 0＋360 \& 3Lt \& －Эで8 \& －306＇9 \& T0－3t8＇ऽ \& 0－38 \& 0－396＇$غ$ <br>
\hline 00＋ヨで・ \& $00+3 \tau \tau$ \& 00＋ヨマ8 \& 00＋3ss＇ \& 00＋362 \& 00＋350＇z \& 00＋Э६8 \& 00＋ヨZ9＇โ \& 00＋ \& 00＋392 \& 00＋ 360 ＇$\tau$ \& T0－3ム \& 0－ \& โ0－3069 \& โ0－3t8＇ऽ \& T0－3を \& $\varepsilon$ <br>
\hline \& \& \& \& \& \& \& \& \& \& \& \& \& \& \& \& <br>
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