# Simulation of Thermo-mechanical Deformation in High Speed Rolling of Long Steel Products 

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#### Abstract

The goal of this thesis is to develop an off-line process model that can be used by engineers to expedite the optimum selection of process parameters in a high-speed mill for hot rolling of long steel products in the United States (U.S.) steel industry. The software tool developed in this work will better enable steel mill manufacturers and operators to predict the geometric properties of the hot rolled material. The properties predicted by the model can be used by the manufacturer to determine if customer requirements for the final rolled product can be met with the specified equipment and rolling conditions. This model can be used to reduce manufacturing costs and shorten production cycle time while assuring product quality.

A coupled thermo-mechanical simulation model was developed using the commercial finite element code ABAQUS. The rolling model is three-dimensional, thermo-mechanical, transient and nonlinear. Two case studies are considered to demonstrate how the finite element model predicts geometric parameters which are necessary to satisfy customer requirements. The finite element model was validated through full-scale testing and verified with existing theoretical/empirical models. The results of the test cases demonstrate that the finite element model is able to predict geometrical properties to ensure that the steel mill satisfies the customer requirements.

A Java pre- and post-processing graphical user-oriented interface has been developed to aid a mill engineer with little or no finite element experience throughout the analysis process of the finishing rolling stands. The Java program uses the finite element analysis results to predict roundness and tolerance customer requirements. Other parameters that are determined include spread, cross-sectional area, percentage reduction in area, incremental plastic strain and total plastic strain and roll force.


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## List of Symbols

| $T(t)$ | Stock Temperature |
| :---: | :---: |
| $h$ | Heat Transfer co-efficient |
| $\sigma_{r}$ | Stefan-Boltzmann Constant |
| $\alpha$ | Thermal Diffusivity |
| $\frac{d T}{d t}$ | Rate of Temperature Change During Rolling |
| $\begin{gathered} d t \\ d \varepsilon_{p} \end{gathered}$ |  |
| $\frac{d \varepsilon_{p}}{d t}$ | Plastic Strain Rate |
| $\mu$ | Co-efficient of Friction |
| $D_{0}$ | Initial Grain Size |
| $t_{0.5}$ | Time to complete 50\% Re-crystallization |
| $T(A 3)$ | Temperature of Alpha Dissolution |
| $T(A 1)$ | Eutectoid Temperature |
| $f_{\alpha}$ | Volume Fraction of Ferrite |
| $f_{\text {carbide }}$ | Volume Fraction of Iron Carbide |
| $f_{\gamma}$ | Volume Fraction of Austenite |
| $T_{\text {heating }}$ | Temperature of Reheating |
| $T_{\text {cooling }}$ | Temperature of Cooling |
| $\left(\frac{d T}{d t}\right)_{\text {cooling }}$ | Rate of Temperature Change During Cooling Process |
| $W_{\text {max }}$ | Maximum Spread of Stock at a Stand |
| $W_{i}$ | Maximum Width of Incoming Stock |
| $\gamma$ | Spread Coefficient |
| $B_{c}$ | Interval of two Cross Points Perpendicular to the Roll Axis direction when the Stock Cross-section and Roll-Groove overlap |
| $A_{h}$ | Area fraction of Stock above Roll-Groove when the Cross-section of the Stock and Roll-Groove are overlapped |
| $A_{s}$ | Area fraction of Stock cut out by $\mathrm{B}_{\mathrm{c}}$ at the inside Roll-Groove when the Cross-section of the Stock and Roll-Groove overlap |
| $A_{0}$ | Cross-sectional Area of Incoming Stock |
| $R_{\text {mean }}$ | Mean Radius of Roll |
| $H_{i}$ | Equivalent Height of Incoming Stock |
| $H_{0}$ | Equivalent Height of Outgoing Stock |
| $h_{i}$ | Maximum Equivalent Height of Incoming Stock |
| $\varepsilon_{p}$ | Mean effective Plastic Strain |


| $H_{i}$ | Equivalent Height of Incoming Stock |
| :---: | :---: |
| $H_{o}$ | Equivalent Height of Outgoing Stock |
| $W_{i}$ | Equivalent Width of Incoming Stock |
| $W_{o}$ | Equivalent Width of Outgoing Stock |
| $\varepsilon_{1}$ | Plastic Strain in Principal Strain Direction 1 |
| $\varepsilon_{2}$ | Plastic Strain in Principal Strain Direction 2 |
| F | Roll Force |
| $P$ | Average Roll Pressure |
| $A_{d}$ | Total Contact Area |
| $C_{x}$ | Distance where the Roll Groove and the Deformed Stock are Separated |
| $L_{\text {max }}$ | Maximum Contact Length |
| $K_{m}$ | Average Resistance |
| $\mu$ | Coulomb Friction Co-efficient |
| $\bar{L}$ | Average Contact Length |
| $h_{m}$ | Effective Mean Height of Stock |
| $\varepsilon$ | Plastic Strain |
| $\dot{\varepsilon}$ | Plastic Strain Rate |
| $T$ | Temperature of the Material ( ${ }^{\circ} \mathrm{K}$ ) |
| $t$ | Non-dimensional Temperature of the Material |
| C | Percentage Carbon Content |
| Mn | Percentage Manganese Content |
| V | Percentage Vanadium Content |
| Mo | Percentage Molybdenum Content |
| Ni | Percentage Nickel Content |
| $k$ | Conductivity of Stock |
| $\dot{q}$ | Heat Generation Rate in Stock |
| $\rho$ | Stock Density |
| $C_{p}$ | Specific Heat of Stock |
| $\chi$ | Fraction of Plastic Deformation Work converted in to Heat in Stock |
| $\beta$ | Mechanical Equivalent of Heat |
| $h^{*}(t)$ | Convective Coefficient between Roll and Stock |
| $r^{*}$ | Radius below which Heat Transfer is neglected |
| $T_{r}$ | Temperature at the surface of the Stock |
| $\varepsilon^{T}$ | Total Plastic Strain at a Stand |
| $\varepsilon^{i}$ | Total Plastic Strain at $\mathrm{i}^{\text {th }}$ Element |
| $V^{i}$ | Volume of the $\mathrm{i}^{\text {th }}$ Element |
| $\Delta \varepsilon^{i}$ | Incremental Plastic Strain at a Stand |
| $\Delta \varepsilon$ | Incremental Plastic Strain ${ }^{\text {th }}$ Element |
| $\Delta \varepsilon_{i j}^{i}$ | Incremental Strain Components |
| $f(y)$ | Groove Surface |

$g(y) \quad$ Side Free Surface

## 1. Introduction

### 1.1. Necessity for Off-line Rolling Simulations in the U.S. Steel Industry

Steel is still a dominant structural material in use today and will be in the foreseeable future. The U.S. steel industry has faced fierce competition from the global market for the past twenty-five years. The steel industry today is vital to both economic competitiveness and national security, employing 170,000 Americans in well-paying jobs ( $50 \%$ above the average for all manufacturing) [1.1]. Asia and Eastern Europe have been taking advantage of their low cost to manufacture inexpensive steel and export it at a low price [1.2]. The tendency towards producing - in a consistent manner - the finished products with specifically controlled microstructural and mechanical properties within narrow limits has distinctly intensified while the quality and dimension range have significantly increased in recent years. Furthermore, mill customers, e.g., automotive manufacturers who use the rod and bar stock to produce fasteners, valve springs and other parts, demand even narrower finished-product tolerances. For the U.S. steel industry to be globally competitive in cost and quality, it must be a leader in innovation and technology.

It is estimated that the rolling process is used in $80-90 \%$ of the steel production worldwide. However, there are currently no off-line tools commercially available in the U.S. to predict a priori the microstructure and hence, the mechanical and geometric properties, of a rolled product after the steel has been subjected to the series of operations necessary for obtaining the desired shape. Consequently, attempts to correlate the rolling characteristics with mechanical properties and microstructure in the finished product have been predominantly empirical in nature. These empirical models may at best be valid under conditions that were used to generate the data, i.e. specific mill conditions and/or type of steel, but do not provide a detailed description of parameters throughout the product. Furthermore, the rolling trials required for empirical studies are very expensive and a process model that can correlate the rolling characteristics with the microstructural parameters could be very beneficial.

During the last five to ten years, there has been a continued effort in the development of software tools by overseas mill builders, steel manufacturers and universities. These tools are increasingly being applied to the development of process improvements - to the point where some of these foreign steel producers have even made products that have a quality or property advantage over US-made products. In the case of the foreign mill builders and steel producers, who are very large companies with extensive resources, the software tools are being used to demonstrate their product's superior performance over the US-built mills, giving them a definite competitive advantage.

This work will focus on developing a off-line software tool intended to significantly improve the process and product development of rolled steel bars and rods. As stated in [1.1], "the prediction accuracy of current deformation models (for rolling,
extrusion, etc.) on quantitative microstructure-property relationships is limited and is a barrier to major advances in rolling process technology." As stated above, the competitiveness of the U.S. steel industry is declining steadily. In order to reverse this trend, it is imperative that new tools be developed to aid U.S. steel makers in a global market.

### 1.2. What is missing in Deformation and Microstructure Rolling Simulations?

Rod and bar customers today are demanding tighter specifications for tolerances on geometric, mechanical and microstructure properties to satisfy the requirements of the products they manufacture. These downstream users are setting requirements on those properties for products to be used in specialized applications, e.g., bridge cable, tire cords, high strength fasteners, etc. This presents a problem for many U.S. rolling mill operators, who are accustomed to meeting stringent requirements on geometric and mechanical properties but not microstructural parameters. In order to determine precise mechanical equipment and processing necessary for optimizing the microstructure, more sophisticated computer models of deformation and microstructure evolution are needed.

The coupling of the rolling process simulation with both deformation and microstructure evolution is a capability that is missing in the U.S. steel industry - as cited by a Steel Roundtable held in 1998 by the American Iron and Steel Institute (AISI) [1.1]. A user-friendly software tool that can be used by process engineers off-line is needed for accurately predicting geometry and such microstructural characteristics as primary and re-crystallized grain size and secondary phase distribution and morphology. Furthermore, mechanical properties such as tensile strength, \% reduction of area and hardness need to be correlated with microstructural parameters.

By having a more complete understanding of the rolling process, the U.S. steel industry will be able to move ahead on improving process and product development of bar and rod products in the world market. A coupled deformation and microstructural rolling simulation tool will allow off-line analyses of "what if" studies of manufacturing options and alternative material microstructures. The tool will accelerate development cycles for new products and reduce the number of costly mill trials - totally eliminating the need for them eventually. The simulations would be used to evaluate roller groove geometries, roll gap settings, stand spacing and other parameters for design comparisons. The intelligent design of groove profiles and other process parameters is a key factor for effective processing (to get proper dimensions, internal deformation and microstructure distribution) and ensuring that the required as-rolled product properties are achieved according to customer specifications.

### 1.3. Significance of this Work

The significance of this work is that product development testing can be carried out off-line via simulations yielding a major reduction in the product development cycle time and expensive on-line testing. Off-line testing can also be carried out even though full-scale facilities do not exist. As basic research, it will provide opportunities for the refinement and validation of current process models of hot rolling steel. The model will facilitate practicing engineers to use advanced technology currently unavailable to U.S.
companies and also provide opportunities for professional development in a field where little is currently offered in the U.S. The results of the work will also have future expansion possibilities, including the extension of the capabilities to on-line models to aid in process setup and control in the rolling mill. This work will have a broad impact on the U.S. steel industry by providing state-of-practice technology to carry out process and product development that will lead to more competitive products in U.S. and overseas markets.

### 1.4. Goal and Objectives

The goal of this project is to develop an off-line finite element model of hot rolling process to simulate coupled thermo-mechanical deformation of rod and bar rolling that can be used by mill engineers in the U.S. steel industry and compare the results with experimental data and various empirical models. A U.S. rolling mill using this process model (when fully verified and validated) will be more capable of manufacturing a product that satisfies customer requirements.

The three research and development objectives consist of the following:

- Thermo-mechanical Deformation Model. Using the commercial finite element code ABAQUS [1.3] a three-dimensional thermo-mechanical deformation model is developed to model the multi-stand finishing rolling process under high temperature and high-speed conditions.
- Verification and Validation. Results of the three-dimensional finite element thermomechanical deformation model are compared to results from the state-of-the-art empirical model and experimental results for a few baseline cases.
- Development of a User Interface. A simple, user friendly Graphical User Interface is developed to preprocess the finite element model for commercial use in a rolling mill. This Graphical User Interface (GUI) is developed using Java ${ }^{\mathrm{TM}}$ technology [1.4] and python script [1.5].


## 2. The Finishing Rolling Process and Model

### 2.1. Processing Stages in a Rolling Mill

Rod and bar steel mills are comprised of equipment for reheating, rolling and cooling as shown in Table 2.1. The primary objectives of the rolling stage are to reduce the cross section of the incoming stock and to produce the customer required section profile, mechanical properties and microstructure in the product.

Table 2.1. Major parameters in the three stages of mill processing [2.1].

| Reheating | ROLLING |  | Cooling |
| :---: | :---: | :---: | :---: |
|  | Roughing | Intermediate |  |
| Reheating Rate | Temperature | Start Temperature <br> Reheating Time <br> Reheating | \% Area Reduction <br> Temperature |
| Interpass Time |  |  |  |
| Strain Rate | Final Temperature |  |  |

When manufacturing long products, it is common to use a series of rolling stands in tandem to obtain high production rates. The stands are grouped into roughing, intermediate and finishing stages (Table 2.1) - usually 26 to 30 stands. Typical temperature, speed, inter-stand time (time between each stand), true strain and strain rate ranges at each stage are shown in Table 2.2. Since cross-sectional area is reduced progressively at each set of rolls, the stock moves at different speeds at each stage of the mill. A rod rolling mill, for example, gradually reduces the cross-sectional area of a starting billet (e.g., 160 mm square, $10-12$ meters long) down to a finished rod (as small as 5.0 mm in diameter, 1.93 km long) at high finishing speeds (up to $120 \mathrm{~m} / \mathrm{s}$ ). Typical rod mills with a four stand finishing block with stands positioned closely together and oriented in a $90^{\circ}$ configuration to allow no-twist rolling is shown in Figure 2.1. A vast majority of the finishing blocks employ an oval-round pass sequence since it produces a good quality surface free of laps and a fairly uniform deformation across the width.

Table 2.2. Typical temperature, speed, interpass time, strain and strain rate ranges at rolling stages.

|  | ROUGHING | INTERMEDIATE | FINISHING |
| :---: | :---: | :---: | :---: |
| Temperature Range | $1000-1100{ }^{\circ} \mathrm{C}$ | $950-1050{ }^{\circ} \mathrm{C}$ | $850-950{ }^{\circ} \mathrm{C}$ |
| Speed Range | $0.1-1 \mathrm{~m} / \mathrm{s}$ | $1-10 \mathrm{~m} / \mathrm{s}$ | $10-120 \mathrm{~m} / \mathrm{s}$ |
| Inter-Stand Time <br> Range | $10300-1600 \mathrm{~ms}$ | $1300-1000 \mathrm{~ms}$ | $60-5 \mathrm{~ms}$ |
| True Strain Range | $0.20-0.40$ | $0.30-0.40$ | $0.15-0.50$ |
| Strain Rate Range | $0.90-10 \mathrm{~s}^{-1}$ | $10-130 \mathrm{~s}^{-1}$ | $190-2000 \mathrm{~s}^{-1}$ |



Figure 2.1. Rod mill with a four stand finishing block.

### 2.2. Importance of the Finishing Rolling Stage

The simulation of the entire process of rolling throughout a rod and bar mill is extremely complex and requires too many resources to carry out even with today's computer power. Therefore, it is necessary to focus on the most important stage of rolling - the finishing end of the mill. This limitation of scope can be justified from both the geometric and material standpoints.

It is well known from experience that the final dimensional quality of the rolled product is determined by the rolling stands within the finishing blocks. The dimensional accuracy in the final product depends on many factors including the initial stock dimensions, roll pass sequence, temperature, microstructure, roll surface quality, roll and stand stiffness and the stock/roll friction condition. Some of the factors that will be considered in this study will be roll spread, side free surface shape, and effective plastic strain.

With regards to the material (steel), the development of the microstructure during rolling is very complex involving static and dynamic re-crystallization of austenite. From a practical point of view, the austenite grain size distribution in the rolled product is of paramount importance in controlling mechanical properties. In the roughing and intermediate stages of the rolling mill, the stock is moving slowly between the stands (Table 2.2), such that the material has a chance to 'normalize' itself as a result of recovery and re-crystallization. During the finishing rolling stage, the stock is traveling at a high speed between closely spaced stands and consequently, will not have adequate time to normalize. This lack of normalization can have a significant effect on the final microstructure and mechanical properties of the rolled product. This work will only consider the finishing rolling and cooling stages as shown in Table 2.1 and only geometric parameters will be considered.

### 2.3. Requirements of an Offline Rolling Model

Since the chemical composition is fixed for specific steel grades, the customer requirements for a particular product that can be controlled in the rolling mill consist of geometry, mechanical properties and microstructure. Theoretical/empirical models can predict these product characteristics, however, they are simplified three-dimensional or two-dimensional models. A finite element analysis can model the process more accurately and can predict the detailed distribution of all these product characteristics throughout the product. The product characteristics are obtained as output in the off-line FEM rolling model are shown in Figure 2.2. The geometric properties consist of roundness (ovality) and tolerance that are determined from the section profile of the finished rod. Mechanical properties include yield and ultimate tensile strengths, \% reduction in area (ductility) and hardness. Microstructure characteristics include grain size, grain distribution, phase composition and phase distribution.

Modeling of the thermo-mechanical rolling process is well established as a valuable off-line tool for optimizing processing conditions. Since rolling involves macroscopic and microscopic phenomena, a coupled thermo-mechanical-microstructural approach should be used. Macroscopic and microscopic phenomena that could be included in this work are shown in Figure 2.3. Since this work is the first stage of a larger project only the shaded components shown in Fig 2.3 will be considered.

The macroscopic phenomena can be broadly classified as heat flow during rolling and deformation under application of rolling load. The macroscopic phenomena will be modeled using the finite element method and will include such factors as:

1. Conduction in the stock and the rolls and convection/radiation to the environment
2. Adiabatic heating due to deformation.
3. Thermal expansion and contraction during the heating and cooling cycles.
4. Large strains and displacements due to elastoviscoplastic flow.
5. The effects of strain, strain rate and temperature.
6. Contact and friction.

Only items 2 through 6 are considered in this work. Item 1 is not considered because 1) Modeling of convection and radiation requires determination of convective heat transfer coefficients and emissivity coefficients which can be done only by experiments.

The modeling of the process at the microscopic level involves many complex physical phenomena associated with nucleation and evolution of the microstructure. The principal microscopic phenomena that could be addressed include the following:

1. Austenite re-crystallization and grain growth.
2. Transformation of austenite into ferrite, pearlite, bainite and martensite (and/or other phases).

A coupling scheme could be established to link the outputs from the macroscopic and microscopic models as shown in Figure 2.3. The microscopic coupling could be carried out primarily through fundamental transport equations and semi-empirical relationships for steels that have been published in the literature. The coupled model would predict in a discretized manner the evolution of microstructure and mechanical
properties at the finite element nodal points. The main assumption is that microstructural features and mechanical properties can be determined and assigned to each macroscopic nodal point. Therefore, a fine mesh will result in predicting the microstructure evolution with greater precision.

The proposed off-line three-dimensional FEM rolling model will be designed for usage as shown in Figure 2.2. In this work only the shaded boxes in Figure 2.2 are considered, however discussion will address all components. Inputs to the off-line FEM rolling model include specifications on the rolling mill finishing stands and incoming stock. The incoming stock is assumed to be at a uniform temperature and uniform austenite grain size. Once the rolling model has solved the coupled thermo-mechanicalmicrostructural problem, the predicted results are output as geometrical, microstructural, and mechanical properties. The numerical results of the FEM rolling model are then validated with full-scale mill testing and verified with current theoretical/empirical models. Theoretical/empirical models for rod and bar round-oval-round pass rolling can predict spread/side free surface [2.1, 2.3], section profile (cross-sectional area) [2.4], mean effective plastic strain and strain rate [2.5, 2.6], and roll force and torque (power) [2.7, 2.8]. If the FEM results are inconsistent with test and theoretical/empirical results, the model is modified. Once the FEM model is validated, the output is compared to customer requirements. If the FEM results do not satisfy customer requirements, the input conditions of the rolling process are modified. This refinement is repeated until the FEM solutions are consistent with the mill testing, theoretical/empirical models and customer requirements. When both these requirements are satisfied, the product would be considered suitable for production on-line.

### 2.4. Challenges in Developing an Off-line Rolling Model

Simulating high speed hot rolling of long products is considered one of the most difficult metal-forming processes and is very complicated from an analyst's perspective. The application of finite element approximations to the rolling process poses modeling challenges on the macroscopic and microscopic levels. Some of the macroscopic challenges include the following:

- Nonlinear Phenomena. The rolling process involves many nonlinear phenomena, e.g., high rates of deformation, contact, friction, rate dependent material behavior, heat transfer and thermo-mechanical coupling. Microscopic issues will not be considered in this work.
- Slender Stock. The large aspect ratio of the stock (length in the rolling direction versus the product cross-sectional dimensions) presents a challenge to adequately discretize the three-dimensional material and conduct the simulations economically.
- Process Interactions between Rolling Stands. Continuous mill operations are complicated further by the interaction of processing between multiple stands that are inherent in the mill design. For example, sensitivity of the deformation in long narrow product to the effects of tension and compression between rolling stands places demands on the accuracy of the boundary conditions and the computational techniques.


Figure 2.2. Proposed off-line finishing rolling process rod and bar simulation model. The shaded part of this proposed model is only considered.


Figure 2.3. Coupling scheme for macroscopic and microscopic models.

### 2.5. Rod and Bar Rolling Simulation Codes used by the Overseas Steel Industry

This section provides a brief state-of-practice review of rolling simulation codes and steel microstructure models encountered in the worldwide steel industry. A literature review on the current state-of-practice reveals very little detailed information regarding the theoretical aspects of any existing thermo-mechanical microstructure rod and bar rolling simulations since they are all proprietary in nature. There are currently no commercial codes in the marketplace that specialize on rolling simulations. ABAQUS [2.9] and MSC.Marc [2.10] have been used extensively to analyze the rolling process whereas ADINA [2.11], ANYSY [2.12], DEFORM-3D [2.13], FORGE3 [2.14], LSDYNA [2.15] and MSC.SuperForge (finite volume) [2.16] are mainly used for sheet metal forming and forging applications. However, there are non-commercial finite element rolling codes that have been developed for the steel industry in Japan, Germany and the United Kingdom as shown in Table 2.3. None of them are available for use in the U.S.

The two Japanese codes include CORMILL and SIMURO. The CORMILL (COmputational Rolling MILL) System [2.17-2.18] was developed at the University of Tokyo, however it can only be used by a Japanese company/university. The CORMILL System is based on mixed Lagrangian-Eulerian formulation assuming elastic-plastic material behavior. CORMILL is capable of simulating three-dimensional deformation characteristics and microstructure evolution in the hot rolling of strip, bar, and wire rod. Development started in 1989 and the developers claim that there have been more than several thousand case studies carried out at University of Tokyo and Japanese industries. The CORMILL System is used today as a tool to design new rolling conditions, roll groove profiles and operation conditions in the research and development departments of several Japanese companies.

Daido Steel, a private steel producer in Japan has independently developed SIMURO (SIMUrator for ROlling) [2.20] to analyze rolling, however, it also is not in the public domain. SIMURO is a three-dimensional, thermo-mechanical finite element based code assuming rigid-plastic material behavior. The major difference between the Japanese programs is that SIMURO can simulate the entire rolling process including the cooling zone that is not considered in CORMILL. Theoretical aspects and capabilities of SIMURO cannot be found in the literature.
SMS Scholoemann-Siemag AG a German manufacturer of rolling mill equipment has developed an in-house computer simulation coupled with MSC.Marc called CRCT
[2.20, 2.21$]$, i.e., Controlled Rolling and Cooling Technology, which has been around since 1991. CRCT is used by SMS to further develop rolling technology and by rod mill operators in Europe to improve final product quality. The software simulates the temperature evolution of a rod through a rolling mill and predicts the microstructure and mechanical properties of the rolled stock. In the literature a very brief description of code capabilities can be found and no information is provided on theoretical aspects.

Corus (part of which was formerly British Steel) is one of the United Kingdom's largest steel producers and $80 \%$ of its products are hot rolled. The Corus research and development group in the U.K. is at Swinden Technology Centre and this center has the ability to predict shape and property development during hot rolling, cooling and downstream processing via simulation [2.22,2.23]. Corus has been applying the finite element technology to solve various processes types, e.g., forming, welding, etc., since 1978. Current software includes finite element components developed in-house and other commercial finite element codes used along side ABAQUS.

Table 2.3. Comparison of overseas rod and bar rolling simulation codes.

| REFERENCE | CORMILL <br> [2.17-2.19] | SIMURO [2.20] | CRCT <br> $[\mathbf{2 . 2 1 , 2 . 2 2 ]}$ | Corus <br> [2.23,2.24] |
| :---: | :---: | :---: | :---: | :---: |
| COUNTRY | Japan | Japan | Germany | United Kingdom |
| COMPUTER <br> CODE | In-House |  <br> MSC.Marc |  <br> MSC.Marc |  <br> ABAQUS |
| USER <br> INTERFACE | Command | Graphical | Graphical | Graphical |
| TECHNIQUE | Finite Element | Finite Element | Finite Element | Finite Element |
| FORMULATION | Arbitrary <br> Lagrangian- <br> Eulerian | Arbitrary <br> Lagrangian- <br> Eulerian | Arbitrary <br> Lagrangian- <br> Eulerian | Arbitrary <br> Lagrangian- <br> Eulerian |
| DIMENSIONALIT <br> Y | 3-D | 1-D, 2-D \& 3-D | 3-D | 3-D |
| TIME <br> DEPENDENCE |  <br> Transient |  <br> Transient |  <br> Transient |  <br> Transient |
| MATERIAL <br> MODEL | Elasto-Plastic | Rigid-Plastic | Elasto-Plastic |  <br> Visco-Plastic |
| MATERIAL <br> FLOW StRESS | Misaka's <br>  <br> General <br> Equation | 12 Types <br>  <br> User Defined | Plastic Strain, <br> Plastic Strain <br>  <br> Temperature | Strain, <br>  <br> Temperature |
| THERMO- <br> MECHANICAL <br> CoUPLING | No | Yes | Yes | Yes |
| COOLING | No | Yes | Yes | Yes |
| ROLL <br> MATERIAL | Rigid \& Elastic | Unavailable | Unavailable | Rigid \& Elastic |


| MULTI-PASS <br> RoLLING | 2-, 3- or 4-Roll | 2-, 3- or 4-Roll | Unavailable | 2-, 3- or 4-Roll |
| :---: | :---: | :---: | :---: | :---: |
| Pass SEQUENCE | 7 Types <br> Including <br> Round-Oval | I Types <br> Including <br> Round-Oval | Unavailable | 4 Types <br> Including <br> Round-Oval |
| No-TWIST <br> RoLLING | Yes | Yes | Unavailable | Yes |
| STAND <br> STIFFNESS | No | No | Unavailable | Yes |
|  <br> TORQUE <br> PREDICTION | Unavailable | Yes | Yes | Yes |
| MICROSTRUCT <br> URE <br> PREDICTION | Yes | Yes | Yes | Yes |
| MECHANICAL <br> PROPERTIES <br> PREDICTION | Unavailable | Unavailable | Yes | Yes |

In regards to the state-of-the-art I am not aware of any in-depth surveys that have only focused on rolling. Surveys on metal processing include a 1982 paper by Kobayashi [2.25] and a follow up in 1985 [2.26]. In 1994 Brannberg and Mackerle [2.27] and in 1998 Mackerle [2.28] compiled extensive bibliographies on the finite element method in materials processing technology. Rowe et al. [2.29] provide a very good bibliography of over 700 books and research papers on metal forming up to 1991. Finite element textbooks on metal forming include Kobayashi, Oh and Altan [2.30], Rowe et al. [2.29] and Wagoner and Chenot [2.31]. There is however one book by Lenard et al. [2.32] that does address rolling applications using the finite element method. There are conferences held regularly focusing on metal forming and include the following: NUMIFORM (International Conference on Numerical Methods in Industrial Forming Processes), International Conference on Technology of Plasticity, International Conference on Metal Forming and Iron \& Steel Society Mechanical Working and Steel Processing Conference.

Extensive research studies have been carried out on flat (plate) rolling. Little research has been done for rod and bar rolling since the stock between the grooved rolls is neither a condition of plane strain or plane stress. Three-dimensional finite element rod and bar studies have included deformation [2.33-2.38], hybrid FEM-slab deformation [2.39-2.42], thermal-mechanical [2.43-2.45] and thermo-mechanical-microstructural [2.19, 2.23, 2.24, 2.46-2.49]. There have also been studies on modeling rod and bar using generalized plane strain [2.50-2.53].

## 3. Theoretical and Empirical Geometric and Deformation Models for Steel Rod and Bar Round-Oval, Oval-Round Pass Rolling

### 3.1. Overview

Theoretical and empirical rolling models are a valuable alternative in validating full-scale mill testing and verifying the finite element-rolling model. Theoretical and empirical models to predict geometric and deformation parameters are well established for strip and plate rolling, however, forming conditions in rod and bar rolling is threedimensional and the former is two-dimensional. In this chapter the state-of-the-art of theoretical and empirical models for rod and bar round-oval-round rolling will be discussed. The major advantage of these models is their simplicity and fast computational time to obtain a solution. Furthermore, these models are fairly accurate in calculating certain parameters of the rod/bar rolling process and the rolled products. However, these models do not provide detailed information about how a parameter varies throughout the rod/bar length and cross section and in that sense can only yield limited global information. The geometric and deformation models that will be discussed include spread and side free surface, section profile (cross-sectional area), mean effective plastic strain and strain rate, and roll force and torque (power).

### 3.2. Spread and Cross-sectional Area

Several empirical analytical models have been proposed to calculate the surface profile and side free surface of a deformed rod and bar stock. Spread is defined as the dimension of the deformed stock after rolling in the direction normal to the direction of rolling (perpendicular to paper) as shown in Figure 3.1. In other words, it measures the increase of width of the stock due to rolling deformation. The side free surface is defined as the region of the stock surface that does not come in to contact with the rolls during the rolling process as signified by the thick line in Figure 3.1.


Figure 3.1. Spread and side free surface.

The spread and side free surfaces are very important in rolling. The surface profile of a deformed stock depends on the spread, free surface profile, and the elongation of the stock. This means that the final shape of the stock is mainly dependent on these parameters. Since the final shape of the stock is very important to the customer, these parameters are very crucial to a roll pass designer when designing a particular rolling pass for specific shape and size requirements. Accuracy in calculating these parameters are critical when satisfying such geometric customer requirements as roundness and tolerance in accordance with ASTM standards [3.1]. Roundness is defined as the difference between maximum diameter and minimum diameter. Tolerance is the allowable difference in maximum/minimum diameter between what a customer orders and what the steel mill delivers.

Table 3.1 provides a comparison of various spread and side free surface models. The main disadvantages of the following models are stated in the table. The three most widely used models in practice will be discussed and have been developed by Saito et al. [3.2], Arnold and Whitton [3.3] and Shinokura and Takai [3.4].

Saito et al. [3.2], in 1977, proposed empirical formulas for calculating spread. The model depends on such parameters as theoretical contact width, actual contact width, mean thickness of the stock, mean height of the pass, mean radius of the roll, mean projected contact length, projected contact area, spread coefficient, elongation coefficient and mean forward slip rate. The major assumption is that the shape of the free surface before and after the rolling is same. The model was experimentally verified by carrying out tests on mild steel S17C ( $0.17 \% \mathrm{C}, 0.19 \% \mathrm{Si}, 0.47 \% \mathrm{Mn}, 015 \% \mathrm{P}, 0.029 \% \mathrm{~S}, 0.008 \% \mathrm{Al})$ at $1050 \pm 100{ }^{\circ} \mathrm{C}$.

Arnold and Whitton [3.3], in 1975, proposed a simple empirical model where spread is calculated based on calculation of a spread coefficient. This model uses an experimental factor and thickness of the rectangle the same cross-sectional area as the rod section before and after rolling. The model was experimentally verified using titanium 120,130 , and 160 , mild steel and titanium alloys $314,315,317$ and 318 . The main disadvantage of this model is that there are too many unknowns and to solve for spread one has to assume a final cross-sectional area. Therefore, this approach can only be used for experimental verification not pass design. Furthermore, it doesn't take into account the finish round stands encountered in Morgan RSM mill.

Shinokura and Takai [3.4], in 1982 developed an empirical-theoretical model that calculates maximum stock spread in round-oval (or oval-round) pass and square-diamond (or diamond-square) pass rolling. The idea behind this model is that the maximum spread of an outgoing stock can be calculated from the roll radius, maximum size of incoming stock and the area fraction between stock and the geometry of the roll groove. The parameters used in this model are initial width $\left(\mathrm{W}_{\mathrm{i}}\right)$, mean radius of the roll $\left(\mathrm{R}_{\text {mean }}\right)$, equivalent height of incoming stock $\left(\mathrm{H}_{\mathrm{i}}\right)$, equivalent height of outgoing stock $\left(\mathrm{H}_{0}\right)$,
maximum height of stock $\left(h_{i}\right)$ and the spread coefficient $(\gamma)$. The spread $\mathrm{W}_{\text {max }}$ is determined from the following relationship,

$$
\begin{equation*}
W_{\max }=W_{i}\left[1+\gamma\left(\frac{A_{h}}{A_{o}}\right) \frac{\sqrt{R_{\text {mean }}\left(H_{i}-H_{o}\right)}}{W_{i}+0.5 h_{i}}\right] \tag{3.1a}
\end{equation*}
$$

with

$$
\begin{align*}
& H_{i}=\left(A_{o}-A_{s}\right) / B_{c}  \tag{3.1b}\\
& H_{o}=\left(A_{o}-A_{s}-A_{h}\right) / B_{c} \tag{3.1c}
\end{align*}
$$

where $B_{c}$ is the interval of two cross points perpendicular to the roll axis direction when the stock cross-section and roll-groove overlap, $\mathrm{A}_{0}$ is the cross-sectional area of incoming stock, $A_{h}$ is the area fraction of stock above roll-groove when the cross-section of the stock and roll-groove are overlapped, and $\mathrm{A}_{\mathrm{s}}$ is the area fraction of stock cut out by $\mathrm{B}_{\mathrm{c}}$ at the inside roll-groove when the cross-section of the stock and roll-groove overlap. The parameters are shown in Figure 3.2. The important assumption is that the spread of the stock depends only on the geometry of the stock and roll-groove. The main disadvantage of the model is the empirical spread coefficient, which are determined by experiment. The value of the spread coefficient in oval-round pass is 0.83 and in round-oval pass is 0.97 .

Lee et al. [3.22], in 2000, proposed an empirical model where free surface radius is calculated based on calculation of spread by Shinokura and Takai [3.4]. This model is valid only for round-oval and oval-round pass sequences. This model linearly interpolates between groove radius and stock radius and uses a weighting fraction based on spread and face width. The model is experimentally validated for low carbon plain steel ( $0.1 \% \mathrm{C}$ ) in a experimental mill setup.

Shinokura and Takai's [3.4] model is used in this work for calculating spread because it is fairly accurate in most conditions. This model is also well accepted in industry. And many research efforts are based on this model. For calculation of surface profile Lee et al. [3.22] used this model.


Figure 3.2. Illustration of equivalent rectangle method in round-oval pass for calculation of equivalent height of incoming stock and roll groove.

Table 3.1. Models for determining spread and side free surface.

| Reference | Theoretical/ Empirical Model | Experimental Verification | Steel Type(s) | Pass <br> Sequence | Transnation al Rolling Speed | Rolling Temperature | Disadvantages | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Arnold and Whitton [3.3] | Empirical | Yes | Pure Titanium <br> (120,130,160), <br> Mild Steel and <br> Titanium Alloys $(314,315,317,318)$ | NA | NA | $\begin{gathered} 700 \& 800{ }^{\circ} \mathrm{C} \text { : } \\ \text { Titanium } \\ 900^{\circ} \mathrm{C}: \\ \text { Mild Steel } \end{gathered}$ | - No Discussion on Spread Equation <br> - Round-oval Pass Sequence Not Considered <br> - Spread is based on calculation of exit area experimentally. |  |
| Saito et al. [3.2] | Empirical | Yes | Mild Steel S17C | NA | NA | $1050 \pm 100^{\circ} \mathrm{C}$ | - Assumes shapes of free surface before and after rolling are same. | + 2-3 \% Error |
| Schlegel and Hensel [3.7] | NA | NA | NA | NA | NA | NA | NA |  |
| Shinokura and Takai [3.4] | Empirical- <br> Theoretical | Yes | Mild | NA | NA | 950-1050 ${ }^{\circ} \mathrm{C}$ | - Spread formula uses a coefficient that needs more verification. |  |
| Vater and Schütza [3.6] | Empirical | Yes | NA | NA | NA |  | - Not General <br> - Not Simple <br> - Not Accurate |  |
| $\begin{gathered} \text { Yanagimoto } \\ {[3.5]} \\ \hline \end{gathered}$ | Empirical | Yes | CR | NA | NA | $1100{ }^{\circ} \mathrm{C}$ | CR |  |
| Lee et al. [3.22] | Empirical | Yes | Low carbon Steel (0.1\%C) | Single Stand Experimental Mill | NA | $1400{ }^{\circ} \mathrm{C}$ | - Calculation of Surface Profile <br> - Valid for Round-oval and Oval-round Pass |  |

NA=Not Available
CR=Cannot Read Since written in Languages other than English

### 3.3. Mean Effective Plastic Strain

The mean effective plastic strain at a rolling stand is defined as the maximum average effective (equivalent) plastic strain of the stock at a given stand during the rod/bar rolling process. Calculation of mean effective plastic strain is extremely important for predicting and controlling the mechanical properties of the rod/bar after rolling because all mathematical models of microstructure evolution requires thermomechanical variables such as mean effective plastic strain, mean effective plastic strain rate and temperature at each rolling stands. Temperature evolution due the mechanical energy converted to heat during the deformation process is also dependent on mean effective plastic strain and mean effective plastic strain rate. Furthermore, mean effective plastic strain rate is in turn a function of mean effective strain and the process time. All of this suggests that the capability of predicting mean plastic strain is essential for controlling the mechanical properties and microstructure of the output rod/bar.

Mean effective plastic strain can be defined in two ways:

1. Incremental mean effective plastic strain. Here it is assumed that the geometry of the stock before it enters a particular stand is the initial geometry of the stock. The final geometry of the stock is the geometry after a particular stand.
2. Total mean effective plastic strain. Here it is assumed that the geometry of the stock before it enters the $1^{\text {st }}$ stand is the initial geometry of the stock. The final geometry of the stock is the geometry after a particular stand.

Table 3.2 provides a comparison of various mean effective strain models. The main advantages and disadvantages of each model are stated in this table. The three most widely used models in practice will be discussed and have been developed by Macagno et al. [3.8], Saito and Kawai [3.9,10] and Lee et al. [3.11].

Macagno et al. [3.8], in 1996 proposed an empirical model of calculating mean effective strain as simple area strains multiplied by an empirical factor. This model is validated against the numerical simulation of deformation due to rod rolling developed at BHP steel [3.13] to calculate the redundant strains associated with specific groove geometries. The main disadvantage of this model is the significant variation of the empirical factor, which ranges from 1.5 to 2 in the roughing stands and 2 to 3 in the subsequent finishing stands.

Saito et al. [3.9], in 1983 proposed a model for mean strain based on equivalent rectangle approximation method discussed before for calculation of spread by Shinokura and Takai [3.4] method. According to Saito et al. [3.9] mean effective plastic strain is expressed simply as natural logarithmic of change of equivalent height on the basis of cross point of incoming stock and groove shape of rolls i.e.,

$$
\begin{equation*}
\varepsilon_{p}=\ln \left(\frac{H_{i}}{H_{o}}\right) \tag{3.2a}
\end{equation*}
$$

where $H_{i}$ is height of the initial equivalent rectangle and $H_{o}$ is height of the final equivalent rectangle.

Kawai [3.10], in 1985, adopted Saito et al.'s [3.10] equation but included a constant in Equation (3.2a). He introduced this constant by applying the plane strain condition in the case of rolling process. His equation is given as,

$$
\begin{equation*}
\varepsilon_{p}=\frac{2}{\sqrt{3}} \ln \left(\frac{H_{i}}{H_{o}}\right) \tag{3.2b}
\end{equation*}
$$

Lee et al. [3.11], in 1999, proposed a model based on equivalent rectangle approximation method and hypothesis of parallelepiped deformation. In this model the round or oval Stock is replaced by a equivalent rectangular prism (Figure 3.3). Then principal plastic strain components are calculated using the volume constancy criteria. The parameters used in this model are equivalent height of initial geometry of the stock $\left(\mathrm{H}_{\mathrm{i}}\right)$, equivalent height of final geometry of the stock $\left(\mathrm{H}_{\mathrm{o}}\right)$, equivalent width of initial geometry of the stock $\left(\mathrm{W}_{\mathrm{i}}\right)$, equivalent width of final geometry of the stock $\left(\mathrm{W}_{\mathrm{o}}\right)$.

The strain is given by

$$
\begin{align*}
& \varepsilon_{p}=\frac{2}{\sqrt{3}}\left(\varepsilon_{1}^{2}+\varepsilon_{2}^{2}+\varepsilon_{1} \varepsilon_{2}\right)  \tag{3.3a}\\
& \varepsilon_{1}=\ln \left(\frac{H_{i}}{H_{o}}\right)  \tag{3.3b}\\
& \varepsilon_{2}=\ln \left(\frac{W_{i}}{W_{o}}\right) \tag{3.3c}
\end{align*}
$$

Three methods of maximum height, method of maximum width, method of widthheight ratio can be used for calculating the parameters $\mathrm{H}_{\mathrm{i}}, \mathrm{H}_{0}, \mathrm{~W}_{\mathrm{i}}, \mathrm{W}_{\mathrm{o}}$.

In maximum height method the maximum height of the stock both initial and final is chosen as $\mathrm{H}_{\mathrm{i}}$ and $\mathrm{H}_{0}$. The widths, $\mathrm{W}_{\mathrm{i}}$ and $\mathrm{W}_{\mathrm{o}}$ is calculated the following relationships

$$
\begin{align*}
W_{i} & =\frac{A_{i}}{H_{i}}  \tag{3.3d}\\
W_{o} & =\frac{A_{o}}{H_{o}} \tag{3.3e}
\end{align*}
$$

where $A_{i}$ and $A_{o}$ are initial and final areas of the stock.
In maximum width method the maximum width of the stock both initial and final is chosen as $\mathrm{W}_{\mathrm{i}}$ and $\mathrm{W}_{\mathrm{o}}$. The heights, $\mathrm{H}_{\mathrm{i}}$ and $\mathrm{H}_{\mathrm{o}}$ is calculated the following relationships

$$
\begin{align*}
& H_{i}=\frac{A_{i}}{W_{i}}  \tag{3.3f}\\
& H_{o}=\frac{A_{o}}{W_{o}} \tag{3.3~g}
\end{align*}
$$

where $A_{i}$ and $A_{o}$ are initial and final areas of the stock.

In width-height ratio method an arbitrary ratio for both $\mathrm{W}_{\mathrm{i}} / \mathrm{H}_{\mathrm{i}}$ and $\mathrm{W}_{\mathrm{o}} / \mathrm{H}_{\mathrm{o}}$ is assumed. Then $\mathrm{W}_{\mathrm{i}}, \mathrm{W}_{\mathrm{o}}, \mathrm{H}_{\mathrm{i}}$ and $\mathrm{H}_{\mathrm{o}}$ is calculated the following relationships

$$
\begin{align*}
& A_{i}=H_{i} W_{i}  \tag{3.3h}\\
& A_{o}=H_{o} W_{o} \tag{3.3i}
\end{align*}
$$

where $\mathrm{A}_{\mathrm{i}}$ and $\mathrm{A}_{0}$ are initial and final areas of the stock. These methods of calculation are shown in Figure 3.4.

The major disadvantage of this model is that it assumes that the strain components in $\mathrm{x}, \mathrm{y}, \mathrm{z}$ directions are actually the principal strain directions. Also, the error of this model also increases with the amount of distortion. However it is the most recent and most improved model for calculating strain. This model is used in conjunction with maximum width method for calculating theoretical effective plastic strain (both incremental and total) in this work. This is because maximum width method is shown to be most accurate with finite element solution by Lee et al. [3.11]. In case of both incremental and total mean effective plastic strain the initial parameters $\left(W_{i}, H_{i}\right.$ and $\left.A_{i}\right)$ are chosen according to their definition given above.


Figure 3.3. Schematic representation of parallelepiped deformation of equivalent rectangle section (reprinted from Lee et al. [3.11]).


Figure 3.4. Three methods of computing an equivalent cross sectional area for the oval round stand. (a) Method of width-height ratio (b) Method of maximum height (c) Method of maximum width (reprinted from Lee et al. [3.11]).

Table 3.2. Models for determining mean effective plastic strain.

| Reference | Theoretical/ <br> Empirical Model | Experimental Verification | Steel Type(s) | Pass <br> Sequence | Transnational Rolling Speed | Rolling Temperature | Disadvantages | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Macagno et al. [3.8] | Empirical- <br> Theoretical | No | Plain Carbon | NA | NA | $1000{ }^{\circ} \mathrm{C}$ | No Mathematical Rationale for Constant Factor | Strains found by multiplying area strains by constant factor |
| Kemp [3.13] | Empirical- <br> Theoretical | Yes | Mild | NA | NA | $1100{ }^{\circ} \mathrm{C}$ | No Mathematical Rationale for Constant Factor | Strains found by multiplying area strains by constant factor |
| Lehnert and Cuong [3.12] | Theoretical | No | High Strength Carbon (St 355) Stainless Steel (X8CrNiTi18.10) | NA | NA | $1000{ }^{\circ} \mathrm{C}$ | - Based on Plane Strain <br> - No Method to Find Exit Cross-section | Might be applicable once the exit cross-sectional shape at a stand can be correctly predicted. |
| Saito et al. [3.9] | Empirical | Yes | Mild Steel S17C | NA | NA | $1050 \pm 100$ | - Used Mean Plastic Strain in Compression <br> - Lateral Spread due to Draught Neglected | 1-D Model |
| Kawai [3.10] | Empirical | No | Medium Carbon (EN80-0.4\%C) | NA | NA | $1000-1200{ }^{\circ} \mathrm{C}$ | Based on [3.] with Plane Strain | 2-D Model |
| Lee et al. [3.11] | Theoretical | $\begin{gathered} \text { No } \\ \text { (Verified with } \\ \text { FEM) } \end{gathered}$ | Low Carbon $(0.1 \% \mathrm{C})$ | NA | NA | $1000{ }^{\circ} \mathrm{C}$ | No Distribution of Variables Over Crosssection | - 3-D Model - Only Geometry Needed |

NA $=$ Not Applicable

### 3.4. Roll Force

Calculation of roll force is important because calculation of torque and power in a rolling mill is based on calculation of roll force. Accurate prediction of roll force for grooved rolling is considerably more difficult than predicting the geometry of the stock. There are essentially three problems, present during flat rolling as well but somewhat easy to handle. They are 1) material's resistance to deformation, as a function of strain, strain rate and temperature 2) the ability to calculate the distributions of the strains, strain rates, stress and temperature in the deformation zone and; 3) the conditions at the roll metal interface, i.e., the coefficients of friction and heat transfers.

Table 3.3 provides a comparison of various roll force and torque models. The main disadvantages of each model are stated in this table. The five most widely used models in practice will be discussed and have been developed by Arnold and Whitton [3.14], Orowan and Pascoe [3.15], Shinokura and Takai [3.16], Khaikin et al. [3.17] and Lee et al. [3.18]

Arnold and Whitton [3.14], in 1975 proposed a formula for roll-separating force based on Sim's [3.19] hot flat rolling theory, which included modifications for projected area of contact and empirical factors.

Orowan and Pascoe [3.15], in 1948 modified their simplified theory of flat rolling to be convenient for bar rolling. They assumed sticking friction for their model.

Shinokura and Takai [3.16], in 1986 introduced a method for calculating effective roll radius, the projected contact area, the non-dimensional roll force and the torque arm coefficients, which were expressed as simple functions of the geometry of the deformation zone. These variables are given for square-to-oval, round-to-oval, square-to-diamond, diamond-to-diamond and oval-to-oval stands.

Khaikin et al. [3.17], in 1971 developed a relation for the projected area of contact for square-diamond-square pass sequence.

Most recently Lee et al. [3.18], in 2001 developed a relation based on projected contact area and average contact stress (roll pressure). In this model it is assumed that deformation occurs under a weak plane strain condition. According to his model roll force at a given stand is calculated by the means of following equations

$$
\begin{align*}
& F=P A_{d}  \tag{3.4a}\\
& A_{d}=2 \int_{0}^{C_{x}} L_{\max }\left(1-\frac{x}{C_{x}}\right)^{m} d x  \tag{3.4b}\\
& P=\left(1-\varepsilon_{1}\right) K_{m} \exp \left[\frac{\mu \bar{L}}{h_{m}}\right] \tag{3.4c}
\end{align*}
$$

where, F is roll force, P is roll pressure, L is average contact length, $\mathrm{L}_{\max }$ is maximum contact length $A_{d}$ is total contact area, $h_{m}$ is effective mean height of stock, $K_{m}$ is average resistance
and $\mu$ is Coulomb friction co-efficient. In this study Lee et al. [3.18] model has been used for calculating roll force.

Table 3.3. Models for determining roll force.

| Reference | Theoretical/ <br> Empirical Model | Experimental Verification | Steel Type(s) | Pass <br> Sequence | Transnational Rolling Speed | Rolling Temperature | Disadvantages | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bayoumi [3.21] | Theoretical | Yes | Low Carbon (AISI 1018) | NA | NA | $1090{ }^{\circ} \mathrm{C}$ |  | - Flowline Field Solution |
| Arnold and Whitton [3.14] | Empirical | Yes | Pure Titanium (120,130,160), Mild Steel and Titanium Alloys (314,315,317,3 18) | NA | NA | $\begin{gathered} 700 \& 800{ }^{\circ} \mathrm{C}: \\ \text { Titanium } \\ 900^{\circ} \mathrm{C} \text { : Mild } \\ \text { Steel } \end{gathered}$ | Not Consistent | Based on Flatrolling |
| Orowan and Pascoe [3.15] | EmpiricalTheoretical | NA | NA | NA | NA | NA | Not Consistent | Based on Flatrolling |
| Shinokura and Takai [3.16] | Empirical- <br> Theoretical | NA | NA | NA | NA | NA | - Included Six <br> Types of Rolling <br> Pass Sequences <br> - Based on Area <br> Strain Model | - Consistently Underperdicts Force/Torque |
| Khaikin et al. [3.17] | Empirical- <br> Theoretical | Yes | NA | NA | NA | NA | - No Experimental <br> Details <br> - Actual Data Not Given | - Over 300 <br> Experiments <br> - Consistently <br> Underperdicts <br> Force/Torque |
| Said, et al. [3.20] | Empirical- <br> Theoretical | Yes | Low Carbon (AISI 1018) | NA | NA | $900-1100{ }^{\circ} \mathrm{C}$ |  | $\begin{gathered} \hline \text { - Compared } \\ \text { Models in }[3.14, \\ 3.15,3.16,3.17] . \\ -[3.15] \text { and }[3.16] \\ \text { superior in } \\ \text { prediction } \\ \text { consistency. } \\ \hline \end{gathered}$ |
| Lee and Kim [3.18] | Theoretical | Yes | Low Carbon $(0.1 \% \mathrm{C})$ | NA | NA | $750-1100{ }^{\circ} \mathrm{C}$ |  | - Based on Weak Plane Strain <br> - Overestimates Slightly |

NA = Not Applicable

## 4. Predicting Flow Stress Behavior of Steel at High Temperature and Strain Rates

### 4.1. Overview

One of the important parameters in modeling the simulation of high-speed high temperature rolling is the flow-stress behavior of the particular steel grade. Flow stress is defined, as the instantaneous yield stress or true stress of a metal defined when a metal starts to undergo continuous plastic deformation. The two principal methods for accurately obtaining the flow stress of a particular grade of steel is direct experimental results and empirical constitutive equations. Empirical constitutive equations are often derived from the regression analysis of experimental data. Typically these equations define the flow strength of a material as a function of the variable considered important by the authors. Table 4.1 lists well-known experimental studies, independently, carried out by different researchers around the world. Table 4.2 shows the most commonly used and widely acceptable constitutive equations for steel, their applicability for different strain ranges, strain rate and temperature and their advantages and disadvantages.

### 4.2. Experimental Studies

Various researchers have carried out experimental studies regarding the flow stress of common steel grades at various strain rates. The most widely used experimental studies are by Cook [4.1], Suzuki [4.2] and Stewart [4.3]. Flow stress data is generally presented as smooth plots of flow stress versus natural strain for various strain rates and temperature ranges.

Cook et al. [4.1] in 1957 carried out experiments for measuring flow stress data for low carbon, medium carbon and high carbon steel. Flow stress versus natural strain curves was presented for various steel grades between a temperature range of $900^{\circ} \mathrm{C}$ to $1200^{\circ} \mathrm{C}$ and strain rate range of $1.5 \mathrm{~s}^{-1}$ to $100 \mathrm{~s}^{-1}$.

Suzuki et al. [4.2] in 1968 carried out experiments for measuring flow stress data for metals and alloys using cam-plastometer apparatus. This article presented flow stress versus natural strain curves for various steel grades between a temperature range of $800^{\circ} \mathrm{C}$ to $1200^{\circ} \mathrm{C}$ for three strain rates $0.3 \mathrm{~s}^{-1}, 2 \mathrm{~s}^{-1}, 10 \mathrm{~s}^{-1}$.

Stewart et al. [4.3] carried out experiments for measuring flow stress data for metals and alloys. This article presented flow stress versus natural strain curves for various steel grades between a temperature range of $700^{\circ} \mathrm{C}$ to $1200^{\circ} \mathrm{C}$ and a strain rate range of $0.4 \mathrm{~s}^{-1}$ to $140 \mathrm{~s}^{-1}$.

Table 4.1. Experimental studies for determining flow stress of steel for different temperature, strain and strain rate ranges.

| Experimental <br> Data | Temperature <br> Range | Strain Range | Strain Rate Range | Experimental <br> Procedure | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Cook [4.1] | $900^{\circ} \mathrm{C}$ to $1200^{\circ} \mathrm{C}$ | NA | $1.5 \mathrm{~s}^{-1}$ to $100 \mathrm{~s}^{-1}$ | NA | - Closely matched by Tomchick equation [4.4]. <br> - Not matched well by Misaka equation [4.6]. |
| Suzuki [4.2] | $800^{\circ} \mathrm{C}$ to $1200^{\circ} \mathrm{C}$ | $0-70 \%$ | $0.3 \mathrm{~s}^{-1}, 2 \mathrm{~s}^{-1}, 10 \mathrm{~s}^{-1}$ | Cam-plastometer | - Closely matched by Tomchick equation [4.4]. <br> - Not matched well by Misaka equation [4.6] for <br> low and high carbon steels. <br> - Matched well by Shida equation [4.5] for low <br> carbon steel. |
| Stewart [4.3] | $700^{\circ} \mathrm{C}$ to $1200^{\circ} \mathrm{C}$ | NA | $0.4 \mathrm{~s}^{-1}$ to $140 \mathrm{~s}^{-1}$ | NA | - Closely matched by Shida equation [4.5]. <br> - Not matched well by Misaka [4.6] and Tomchick <br> [4.4] equations. |

NA=Not Available

### 4.3. Empirical Constitutive Equations

Most of the empirical constitutive equations are based on the thermodynamical concept that flow stress of a material depends on present values and past history of observable variables such as strain, strain rate and temperature. The general relationship is of the following form

$$
\begin{equation*}
\sigma=f(\varepsilon, \dot{\varepsilon}, T) \tag{4.1}
\end{equation*}
$$

where $\sigma$ is the flow stress, $\varepsilon$ is the strain, $\dot{\varepsilon}$ is the strain rate, T is the temperature and the exact relationship between the variables are determined by the regression analysis of available experimental data. The most widely used empirical equations have been developed by Tomchick [4.4], Shida [4.5] and Misaka [4.6]. Lee et al. [4.8] has recently proposed a modification of the Shida equation.

Tomchick [4.4], in 1982 proposed a empirical constitutive equation by studying Cook experimental data [4.1]. The experimental data was analyzed to determine strain hardening behavior, strain rate hardening behavior and temperature dependence by considering flow stress $(\sigma)$ as a simultaneous function of strain $(\varepsilon)$, strain rate $(\dot{\varepsilon})$, and temperature (T). The equation is given by,

$$
\begin{equation*}
\sigma=(A+B \varepsilon) \varepsilon^{n} \dot{\varepsilon}^{m} \exp (-\lambda T) \tag{4.2}
\end{equation*}
$$

where $\mathrm{A}, \mathrm{B}, \mathrm{n}, \mathrm{m}$ and $\lambda$ are material constants determined by regression analysis of the Cook experimental data [4.1].

Shida [4.5], in 1969 developed a constitutive equation, which is most comprehensive and widely used constitutive equations of steel. The relationship defines flow strength $(\sigma)$ as a function of strain $(\varepsilon)$, temperature (T) and carbon content. The mathematical formulations of Shida's empirical relations are as follows

$$
\begin{equation*}
\sigma=\sigma_{f} f\left(\frac{\dot{\varepsilon}}{10}\right)^{m}\left(\text { in } \mathrm{Kg} / \mathrm{mm}^{2}\right) \tag{4.3a}
\end{equation*}
$$

where
with,

$$
\left.\begin{array}{l}
\sigma_{f}=0.28 \exp \left[\frac{5}{t}-\frac{0.01}{C+0.05}\right] \\
m=(-0.019 C+0.126) t+(0.075 C-0.05) \\
\sigma_{f}=0.28 q(C, t) \exp \left[\frac{5}{t_{d}}-\frac{0.01}{C+0.05}\right] \\
q(C, t)=30(C+0.9)\left[t-\frac{0.95(C+0.49)}{C+0.42}\right]^{2}+\frac{C+0.06}{C+0.09}  \tag{4.3e}\\
m=(0.081 C-0.154) t+(-0.019 C+0.207)+\frac{0.027}{C+0.320}
\end{array}\right\} t \geq t_{d} \quad\left\{\begin{array}{l}
\end{array}\right\}
$$

$$
\begin{equation*}
t_{d}=\frac{0.95(C+0.41)}{C+0.32} \tag{4.3~g}
\end{equation*}
$$

$$
\begin{align*}
& f=1.3\left(\frac{\varepsilon}{0.2}\right)^{n}-0.3\left(\frac{\varepsilon}{0.2}\right)  \tag{4.3h}\\
& n=0.41-0.07 C  \tag{4.3i}\\
& t=T\left({ }^{o} K\right) / 1000 \tag{4.3j}
\end{align*}
$$

furthermore, C is the carbon content of the steel grade in percent and t is a dimensionless temperature.

Lee et al. [4.8] in 2002 modified Equation (4.3a) of Shida's Model to make it more generalized and applicable to a much larger range of strain rates. The relationship in Equation (4.3a) is replaced by the following relationship

$$
\begin{equation*}
\sigma=\sigma_{f} f\left(\frac{\dot{\varepsilon}}{10}\right)^{m}\left(\frac{\dot{\varepsilon}}{100}\right)^{m / 2.4}\left(\frac{\dot{\varepsilon}}{1000}\right)^{m / 15} \tag{4.4}
\end{equation*}
$$

with all other parameters remaining the same as in [4.5]. Equation (4.4) is valid for the strain rate up to $3000 \mathrm{~s}^{-1}$ and has been validated by Split Hopkinson pressure bar test for 4340-alloy steel.

Misaka et al. [4.6] in 1971 developed a constitutive equation, which defines flow strength as a function of strain $(\varepsilon)$, strain rate $(\dot{\varepsilon})$, temperature (T), and material composition. The flow stress is given by the following relationship

$$
\begin{align*}
\sigma & =f\left\{\exp \left(0.126-1.75 C+0.594 C^{2}+\frac{2851+2968 C-1120 C^{2}}{T}\right)\right\} \varepsilon^{0.21} \dot{\varepsilon}^{0.13}  \tag{4.5a}\\
f & =0.916+0.18 M n+0.389 V+0.191 M o+0.004 N i \tag{4.5b}
\end{align*}
$$

where $\sigma$ is mean resistance to deformation $\left(\mathrm{Kg} / \mathrm{mm}^{2}\right), \mathrm{C}$ is Carbon Content $(\%), \mathrm{Mn}$ is Manganese Content (\%), V is Vanadium Content (\%), Mo is Molybdenum Content (\%), Ni is Nickel Content (\%), and T is temperature ( ${ }^{\circ} \mathrm{K}$ ).

Table 4.1. Constitutive equations for determining flow stress of steel for different strain rates and temperatures.

| Constitutive Equation | Temperature Range | Strain Range | Strain Rate Range | Material Composition | Advantages | Disadvantages |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Tomchick [4.4] | $900^{\circ} \mathrm{C}$ to $1200^{\circ} \mathrm{C}$ | NA | $1.5 \mathrm{~s}^{-1}$ to $100 \mathrm{~s}^{-1}$ | Low Carbon, Medium Carbon and High Carbon Steel | - Matches excellently with Cook [4.1] data. - Applicable over a wide variety of strain rates. | - Applicability of strain range is unclear. <br> - Effect of material composition is unclear. |
| Shida [4.5] | $700^{\circ} \mathrm{C}$ to $1200^{\circ} \mathrm{C}$ | 0-70\% | $1 \mathrm{~s}^{-1}$ to $100 \mathrm{~s}^{-1}$ | Up to $1.2 \%$ Carbon Content | - Matches relatively well with Cook [4.1] and Suzuki [4.2] data. <br> - Effect of material composition on flow stress is well defined |  |
| Misaka [4.6] | NA | NA | NA | NA | - Effect of material composition on flow stress is well defined. | - Matches poorly with Suzuki [4.2] data form low and High Carbon Steel. |
| $\begin{gathered} \text { Lee } \\ \text { (Modified Shida) } \\ {[4.8]} \end{gathered}$ | $25^{\circ} \mathrm{C}$ to $1100^{\circ} \mathrm{C}$ | 0-70\% | $1 \mathrm{~s}^{-1}$ to $3000 \mathrm{~s}^{-1}$ | Up to $1.2 \%$ Carbon Content | - Matches excellently with SHPB test conducted by Lee et al. [4.8] <br> - Applicable for a large range of strain rate. | - Experimental verification has been done only for AISI 4340 steel. |

NA= Not Available

## 5. Case Studies and Discussion

### 5.1. Overview

In this work the commercial finite element code ABAQUS/Explicit [5.1] is used to simulate the rolling process. Two case studies are considered as benchmarks to validate the finite element model against full-scale mill testing and theoretical models. The following two case studies are considered:

- Republic Engineered Products Rod Outlet. Republic Engineered Products, Lorain, OH , Rod Outlet is a single strand mill designed and installed by Morgan Construction Company and it began operating in 1994. It is a 14 -stand outlet with 10 -stand No-Twist Mill and 4 -stand Reducing/Sizing mill. The mill now produces carbon and alloy steel rods from 5.5 mm to 22 mm diameter.
- POSCO No. 3 Mill. POSCO, No. 3 mill, Pohang, Korea is a two-strand mill, designed and installed by Morgan Construction Company and it began operating in 1988. Morgan upgraded the mill, in 2001. The initial 13 stands of this mill is double strands. The mill separates after stand 13 into two independent strands with 6 -stand pre-finishing mills, 10 -stand No-Twist mills and 4 -stand Reducing/sizing mills. The mill now produces carbon and alloy steel bars from 5.0 mm to 22 mm diameter at temperatures as low as $750{ }^{\circ} \mathrm{C}$, and at speeds of up to 110 meters per second. As a result of the upgrade, the output for the two strands will increase from 700,000 to 820,000 metric tons per year.
Details of these two case studies are given in Table 5.1.
Table 5.1. Details of Republic Engineered Products Rod Outlet and POSCO No. 3 mill.

| Organization | REP <br> (Republic Engineered Products) | POSCO |
| :---: | :---: | :---: |
| Location | Lorain, Ohio, USA | Pohang, Republic of Korea |
| Built | 1960 s - Rod Outlet Added in 1994 | 1987-Modernization with RSM's in <br> 2001 |
| Mill | Rod Outlet - Single Strand, 14 Stand <br> Rod Outlet | Two strand, with 13 Stands Rolling <br> Double Strand, Separating after <br> Stand 13 into Two Independent <br> Strands with Pre-finishing Mills, <br> No-Twist Mills and Reducing/Sizing <br> Mills |
| Mill | Rod Outlet - 10 Stand No-Twist Mill <br> and 4 Stand Reducing/Sizing Mill | 5-stand Roughing Mill, 8-stand <br> Intermediate Mill, 6-stand Pre- <br> Finishing Mills, 10-stand No-Twist <br> Mills and 4-stand Reducing/Sizing <br> Mills |
| Products | Rod Outlet - Carbon and Alloy Steel <br> Rods from 5.5 mm to 22 mm <br> Diameter | Carbon and Alloy Steel Bars from <br> 5.0 mm to 22 mm Diameter |
| Billet | 152 mm Square, Continuous Cast | 162 mm Square, Continuous Cast |

The Republic mill will consider the finishing stands (4-stand Reducing/Sizing mill) while POSCO No. 3 will consider the roughing stands (Initial four stands of the roughing mill). Since available finite element and theoretical results for POSCO No. 3 mill can be found in Lee et al. [5.1, 5.3], the roughing stands are considered.

This chapter contains a brief description of these two case studies, the different techniques used to model the case studies, results of the finite element solution and a comparison of these results with available full-scale mill testing data and theoretical results. The two case studies will be presented based on the flow chart in Figure 2.2.

### 5.2. Case Study \#1- Republic Engineered Products, Finishing Stands

### 5.2.1. Product Manufactured in the Mill

The Republic Engineered Products, Lorain, OH consists of Morgan RSM [5.11] that is used to produce a finished rod of 12.75 mm diameter. The customer (rod user) is a U.S. automotive supplier who manufactures M12 x $1.25,4 \mathrm{~g}$ (high accuracy, fine fits) steel bolt of SAE class 4.6 from the finished rod. The material considered is AISI 1045 medium carbon steel that is commonly used in the U.S. automotive industry for gears, shafts, axles, studs and bolts.

### 5.2.2. Configuration of the Rolling Stands

The details of the Republic Engineered Products, Lorain, OH for the finishing rolling stands and the incoming stock are defined in Table 5.2. The geometric details regarding the finishing rolling stands were obtained from Morgan Construction Company [5.11]. Detailed pictures of the Republic Engineered Products RSM mill are shown in Figure 5.1. Republic Engineered Products RSM mill consists of four finishing stands with a pass sequence of oval-round-round-round. Stand \#1 consists of two oval grooved rolls and input stock is of circular cross-section (Figure 5.1c). Stand \#2 consists of two round grooved rolls oriented at $90^{\circ}$ to Stand \#1 and the output of the Stand \#1 is used as input stock for this stand. Stand \#3 consists of two round grooved rolls oriented at $90^{\circ}$ to Stand \#2 and the output of the Stand \#2 is used as input stock for this stand. Stand \#4 consists of two round grooved rolls oriented at $90^{\circ}$ to Stand \#3 and the output of the Stand \#3 is used as input stock for this stand.

Table 5.2. Details of Republic Engineered Products, Finishing rolling stands and incoming stock.

| Finishing Rolling Stands |  | Incoming Stock |  |
| :---: | :---: | :---: | :---: |
| Stand Sequence | Oval-round-round-round | Translational Speed | $19 \mathrm{~m} / \mathrm{s}$ |
|  | Stands 1-2: 820 mm ; | Cross Section Profile | 16.395 mm Diameter ${ }^{1}$ |
| (On-center) | Stands 2-3: 966 mm ; Stands 3-4: 150 mm | Section Length | The stock is continuously fed into the stands |
| Roll Diameters | Stand \#1: 211.09 mm ; <br> Stand \#2: 211.09 mm ; <br> Stand \#3: 145.13 mm ; <br> Stand \#4: 145.14 mm | Material | AISI 1045 <br> Medium Carbon Steel |
| Roll Gaps | Stand \#1: 1.2 mm ; Stand \#2: 1.36 mm ; Stand \#3: 1.32 mm ; Stand \#4: 1.4 mm | Chemical Composition | $\begin{gathered} \text { C-0.45, Mn-0.75, } \\ \text { P-0.04, S-0.05 (wt. \%) } \end{gathered}$ |
| Roll Groove Geometries | Defined by Morgan RSM [5.11] | Austenite Grain Size | Not Applicable |
| Roll Material | Tungsten Carbide |  |  |
| No-twist Rolling | Stands are Alternatively Oriented $90^{\circ}$ from Each Other | Temperature | Uniform at $910{ }^{\circ} \mathrm{C}$ |
| Roll Temperatures | Not Applicable | Strain Rate Range | $350-500 \mathrm{~s}^{-1}$ |
| Rotational Speed of Rolls | Stand \#1: 2138.5 rpm ; <br> Stand \#2: 2591.2 rpm ; <br> Stand \#3: 4005.9 rpm; <br> Stand \#4: 4164.6 rpm | Specific Heat | $475 \mathrm{~J} / \mathrm{Kg} / \mathrm{K}$ [5.7] |
| Roll/Stock Friction | Friction due to Contact between Wat | ungsten Carbide Roll and Present between as Coola | I 1045 Stock Surface with |

${ }^{1}$ Diameter obtained by full-scale mill testing at room temperature is corrected by $+1 \%$ due to thermal expansion from room temperature to $910^{\circ} \mathrm{C}$ (Commonly used by Morgan Construction Company [5.11]).


Figure 5.1. Finishing stands of Republic Engineered Products, RSM Mill

### 5.2.3. How is the Problem Modeled using FEM?

The commercial finite element code ABAQUS/Explicit [5.10] was used in this work. Table 5.3 states the assumptions, solution techniques and other modeling parameters used in the finite element simulation of the four finishing stands in the Republic Engineered Products RSM mill. Each item shown in Table 5.4 is discussed indepth in Appendix E. For this study, the RSM was analyzed as a complete assembly, i.e.,
all four stands as shown by the finite element model in Figure 5.2. A finite element preand post-processor program is written using Python script and Java (Appendix A) to analyze the results of the finite element solution and verify with full-scale mill testing data and validate with theoretical results.

Table 5.3. Details of ABAQUS/Explicit finite element model for the Republic Engineered Products, Finishing rolling stands and incoming stock.

| Formulation | Mesh Domain | Lagrangian |
| :---: | :---: | :---: |
|  | Time Dependence | Transient |
|  | Time Integration | Explicit, Dynamics, Adiabatic. <br> Optimal time step is decided automatically by ABAQUS |
|  | Dimensionality | Three-Dimensional |
|  | Mass Scaling | None |
|  | Adaptive Meshing | Lagrangian Analysis: No |
|  | Hourglass | Artificial Stiffness |
| Stock | Element Type | Linear Hexahedral Brick (C3D8R), Deformable, Reduced Integration |
|  | Mesh Characteristics | \#of Nodes: 49,994 \#of Elements: 48,820 \#of DOF: 147,030 (including Lagrange Multipliers) |
|  | Material | Homogeneous and Isotropic |
|  | Length | $1.0 \mathrm{~m}^{1}$ |
|  | Rate Dependence | Yes |
|  | Spring Back Calculation | No |
|  | Plasticity Law | Lee (Modified Shida) ${ }^{2}$ [5.4] |
|  | Hardening Rate | Isotropic |
|  | \% Plastic Deformation Energy Converted to Heat | 0.90 [5.9] |
|  | Initial Conditions | Initial Velocity of the Stock; Initial Temperature of the Stock |
| Roll | Material | Rigid |
|  | Finite Element Characterization | Analytic Rigid Surface |
|  | Boundary Conditions | Rotational Speed of Rolls (Table 5.2) |
| Stock / Roll Interface | Contact Condition | Tangential: Penalty; Normal: Hard |
|  | Friction Model | Coulomb ( $\mu=0.3$ ) |
|  | Heat Transfer Effects | Not Applicable |
| Stand | Material | Rigid Pin support at Roll |
|  | Model Spacing (On-Center) ${ }^{1}$ | Stands 1-2: 250 mm ; Stands 2-3: 200 mm ; Stands 3-4: 200 mm |
|  | Orientation ${ }^{3}$ | Stand \#1: Vertical; Stand \#2: Horizontal; Stand \#3: Vertical; Stand \#4: Horizontal |

${ }^{1}$ The section length of the stock is 1.0 m in the finite element model to reduce the number of degrees of freedom in the model. Inter-stand distances are also minimized for the same reason.
${ }^{2}$ Appropriate models are used based on expected strain rate range in Table 5.2.
${ }^{3}$ Stand orientation for the finite element model was assumed oriented vertically and horizontally for simplicity in model creation


Figure 5.2. Arrangement of ABAQUS/Explicit rolling stands in Republic Engineered Products RSM mill.

In this work a full three-dimensional finite element model is considered. The pure Lagrangian formulation was only considered due to Python scripting limitations in ABAQUS. Only this formulation could be integrated in the Java Pre-processor (Appendix A). The Arbitrary Lagrangian-Eulerian (ALE) formulation was also considered in this work. However, ALE cannot be used via Python script and the results are similar to the Lagrangian formulation (Appendix F). Since this work is limited to geometric customer requirements, the finite element model only accounted for deformation and not heat transfer. The process, being a very high speed one, is considered as adiabatic. Therefore explicit, dynamic and adiabatic is used to solve this transient problem. Since the deformation of the rolls and stands are within the elastic limit and are very small compared to the large plastic deformation of the stock, the rolls and stands are considered as rigid. The stand Spacing used in this simulation (Table 5.3) are less than the separations that would be used on actual equipment (Table 5.2) in order to reduce computational time without adversely affecting solution accuracy ${ }^{1}$. Stock material is assumed as homogeneous and isotropic material with no porosities. Three-dimensional, deformable, reduced integration, linear hexahedral (brick) element (C3D8R) is used to model the stock. Contact between roll and stock is defined, as a contact pair that consists of penalty contact enforcement method. Mass scaling is not used since, though, a large amount of Mass Scaling can predict the correct deformed shape, however, it may

[^0]adversely affect other parameters that are influenced by inertia, e.g., stress, velocity, etc. An adiabatic analysis is performed with the assumption that the fraction of the energy of plastic deformation that is converted into heat as 0.9 [5.9]. The rolls are constrained to rotate only in one direction and the magnitude of rotation is based on the years of design experience at Morgan Construction Company. This data is used as a boundary condition in the finite element model. The velocity and temperature of the stock at the entry to the first stand is used as initial conditions in the model. An in-depth discussion of the items in Table 5.3 is given in Appendix E.

### 5.2.4. Comparison of Finite Element Results with Full-scale Testing and Theoretical Calculation

A simplified version of the proposed rolling model was used to produce a finished rod of 12.75 mm diameter. As shown in the lower half of Figure 5.2. Once the finite element analysis is completed, the model is validated with full-scale mill testing and verified with theoretical models. Table 5.4 summarizes the finite element, theoretical and full-scale mill testing results for spread, cross-sectional area, percentage reduction in area, incremental plastic strain, total plastic strain and roll force at all four finishing stands. Figures 5.3 through 5.6 compares the finite element, theoretical, and full-scale mill testing results for the cross-sectional profile, incremental plastic strain, total plastic strain and roll force at Stands \#1 through \#4. Finite element plots of the cross-sectional plastic strain distribution at Stands \#1 through \#4 are shown in Figure 5.7.

Table 5.4. Comparison of full-scale mill testing, FEM and theoretical geometric results at each finishing stand for Republic Engineered Products RSM mill.

| Characteristics of Finite Element Model | Formulation Type |  |  | Lagrangian |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | Shida [F.2] |
|  | Number of Nodes |  |  | 42,820 |
|  | Number of Elements |  |  | 49,994 |
|  | Number of Degrees of Freedom (Including Lagrange multipliers) |  |  | 147,030 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 19.11 \\ (-2.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 13.58 \\ (-0.9 \% \mathrm{~T}) \\ (-1.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 14.45 \\ (3.1 \% \mathrm{~T}) \\ (3.0 \% \mathrm{FST}) \end{gathered}$ | $\begin{gathered} 12.81 \\ (-0.2 \% \mathrm{~T}) \\ (-0.1 \% \mathrm{FST}) \end{gathered}$ |
| Theoretical Lee [5.3] | 19.57 | 13.70 | 13.98 | 12.84 |
| Full-scale Mill Testing | - | 14.01 | 14.02 | 12.82 |
| Cross-sectional Area (mm ${ }^{2}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 167.68 \\ (-2.8 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 145.72 \\ (0.1 \% \mathrm{~T}) \\ (-0.6 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 134.92 \\ (-0.7 \% \mathrm{~T}) \\ (0.2 \% \mathrm{FST}) \end{gathered}$ | $\begin{gathered} 128.84 \\ (-1.3 \% \mathrm{~T}) \\ (0.5 \% \mathrm{FST}) \end{gathered}$ |
| Theoretical Lee [5.3] | 172.50 | 146.60 | 135.94 | 130.59 |
| Full-scale Mill Testing | - | 145.66 | 134.66 | 128.15 |


| Percentage Reduction in Area (\%) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 18.67 \\ (2.1 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 13.10 \\ (-12.8 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 7.40 \\ (1.9 \% \mathrm{~T}) \\ (-2.0 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 4.51 \\ (14.5 \% \mathrm{~T}) \\ (-6.6 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 18.28 | 15.02 | 7.27 | 3.94 |
| Full-scale Mill Testing | - | - | 7.55 | 4.83 |
| Incremental Plastic Strain ${ }^{1}(\mathrm{~mm} / \mathrm{mm})$ |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.399 \\ (5.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.380 \\ (+15.2 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.107 \\ (0.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.081 \\ (1.25 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] | 0.380 | 0.331 | 0.107 | 0.08 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.399 \\ (5.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.764 \\ (7.6 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.904 \\ (11.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.983 \\ (13.1 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.380 | 0.710 | 0.814 | 0.869 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 110.2 \\ (-42.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 80.7 \\ (-48.3 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 49.1 \\ (7.7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 30.7 \\ (20.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 191.9 | 156 | 46 | 26 |

T-\% Difference with theoretical method.
$\mathrm{FST}^{2}$ - \% Difference with full-scale mill testing data.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

Overall there is very good correlation between the finite element solution, theoretical solution and full-scale mill testing for spread and cross-sectional area of the stock. The percentage difference between finite element solution, theoretical solution and full-scale mill testing for spread and cross-sectional area is a maximum of $3 \%$ and in most cases within $2 \%$. It can be concluded that for the last three stands with round grooves, the finite element solution for cross-sectional area is greater than full-scale mill testing cross-sectional area and less than theoretical cross-sectional.

There is no full-scale mill testing data available for incremental plastic strain and total plastic strain, therefore, only the theoretical and finite element solutions are compared. The theoretical and finite element solutions for incremental plastic strain and total plastic strain are consistent for the initial stands. However, the difference between them increases with successive stands due to error accumulation ${ }^{3}$ from the previous

[^1]stands. Both the incremental plastic strain and total plastic strain finite element solution is generally greater than the theoretical solution and the maximum percentage difference is $15 \%$. The finite element solution however is more useful since it determines the strain distribution that can be used to find mechanical properties and microstructure.

There is no full-scale mill testing data available for the roll force, therefore, only the theoretical and finite element solutions are compared. The finite element solution for roll force is less $\approx 40-50 \%$ of the theoretical solution for the first two stands where $\%$ reduction is large. This appears very large and is probably due to the fact that the actual model for calculating roll force by Lee [5.2] uses two parameters that are experimentally determined. In absence of experimental data these two parameters were determined theoretically ${ }^{4}$. For the last two stands, where $\%$ reduction is small, the finite element solution for roll force is $\approx 10-20 \%$ greater than the theoretical solution. It was observed that the roll force obtained by the finite element solution is consistent within $10 \%$ of a proprietary Morgan [5.11] technique for calculating roll force. The proprietary model employs a combination of empirical techniques and experimental validation.

The results from Stand \#4 (last stand) are very important, because geometric roundness and tolerances at the stand exit determines product quality. The results indicate a strong correlation between full-scale mill testing, finite element solution and theoretical solution for spread and cross-sectional area.

[^2]

a. Cross-sectional profile and area after Stand \#1.
b. Plastic Strains after Stand \#1.

c. Roll Force at Stand \#1.

Figure 5.3. Comparison of finite element and theoretical solutions for Stand \#1.

Table 5.5. Results after Stand \#1 of the Republic Engineered Products RSM.

| Finishing Stand \#1 |  |  |  |
| :---: | :---: | :---: | :---: |
| Parameter | Method | Value | \% Difference <br> with Theoretical |
| Spread | FEM | 19.11 mm | $-2.3 \%$ |
|  | Theoretical Lee <br> $[5.3]^{1}$ | 19.57 mm |  |
| Cross-sectional Area | FEM | $167.68 \mathrm{~mm}^{2}$ | $+2.1 \%$ |
|  | Theoretical Lee [5.3] | $172.50 \mathrm{~mm}^{2}$ |  |
| Percentage Reduction <br> in Cross-sectional <br> Area | FEM | Theoretical Lee [5.3] | $18.28 \%$ |

${ }^{1}$ Spread factor $\beta=0.97$
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.9].
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

a. Cross-sectional profile and area after Stand \#2.

c. Plastic Strains after Stand \#2.

b. Cross-sectional profile and area after Stand \#1.

d. Roll Force at Stand \#2.

Figure 5.4. Comparison of finite element and theoretical solutions for Stand \#2.

Table 5.6. Results after Stand \#2 of the Republic Engineered Products RSM.

| Finishing Stand \#2 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Parameter | Method | Value | \% Difference with |  |
|  |  |  | Theoretic al | Full-scale Mill Testing |
| Spread | FEM | 13.58 mm | -0.88 | -3.0 |
|  | Theoretical Lee [5.3] ${ }^{1}$ | 13.70 mm |  |  |
|  | Full-scale Mill <br> Testing | 14.01 mm |  |  |
| Cross-sectional Area | FEM | $\begin{gathered} 145.72 \\ \mathrm{~mm}^{2} \end{gathered}$ | -0.6 | +0.1 |
|  | Theoretical Lee [5.3] | $146.60$ |  |  |
|  | Full-scale Mill Testing | $\begin{gathered} 145.66 \\ \mathrm{~mm}^{2} \end{gathered}$ |  |  |
| Percentage Reduction in Cross-sectional Area | FEM | 13.10 \% | -12.8 \% |  |
|  | Theoretical Lee [5.3] | 15.01 \% |  |  |  |
| Incremental Plastic Strain | FEM | $\begin{gathered} 0.38 \\ \mathrm{~mm} / \mathrm{mm} \\ \hline \end{gathered}$ | -15.3 |  |
|  | Theoretical Lee $[5.1]^{2}$ | $\begin{gathered} 0.33 \\ \mathrm{~mm} / \mathrm{mm} \\ \hline \end{gathered}$ |  |  |  |
| Total <br> Plastic Strain | FEM | $\begin{gathered} \hline 0.764 \\ \mathrm{~mm} / \mathrm{mm} \\ \hline \end{gathered}$ | +7.6 |  |
|  | Theoretical Lee $[5.1]^{2}$ | $\begin{gathered} 0.710 \\ \mathrm{~mm} / \mathrm{mm} \\ \hline \end{gathered}$ |  |  |  |
| Roll Force | FEM | 80.7 kN | -48.3 |  |
|  | Theoretical Lee $[5.2]^{3}$ | 156 kN |  |  |  |

[^3]
a. Cross-sectional profile and area after Stand \#3.

c. Plastic Strains after Stand \#3.

b. Cross-sectional profile and area after Stand \#3.


Figure 5.5. Comparison of finite element and theoretical solutions for Stand \#3.

Table 5.7. Results after Stand \#3 of the Republic Engineered Products RSM.

| Finishing Stand \#3 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Parameter | Method | Value | \% Difference with |  |
|  |  |  | Theoretic al | Full-scale Mill Testing |
| Spread | FEM | 14.45 mm | +3.1 | +3.0 |
|  | Theoretical Lee $[5.3]^{1}$ | 14.02 mm |  |  |
|  | Full-scale Mill Testing | 13.98 mm |  |  |
| Cross-sectional Area | FEM | $134.92 \mathrm{~mm}^{2}$ | -0.7 | +0.2 |
|  | Theoretical Lee [5.3] | $135.96 \mathrm{~mm}^{2}$ |  |  |
|  | Full-scale Mill Testing | $134.66 \mathrm{~mm}^{2}$ |  |  |
| Percentage <br> Reduction in Crosssectional Area | FEM | 7.40 \% | +1.8 | -2.0 |
|  | Theoretical Lee [5.3] | 7.27 \% |  |  |
|  | Full-scale Mill Testing | 7.55 \% |  |  |
| Incremental Plastic Strain | FEM | $\begin{gathered} 0.107 \\ \mathrm{~mm} / \mathrm{mm} \end{gathered}$ | +0.5 |  |
|  | Theoretical Lee $[5.1]^{2}$ | $\begin{gathered} 0.107 \\ \mathrm{~mm} / \mathrm{mm} \end{gathered}$ |  |  |  |
| Total Plastic Strain | FEM | $\begin{gathered} 0.904 \\ \mathrm{~mm} / \mathrm{mm} \end{gathered}$ | +11.2 |  |
|  | Theoretical Lee [5.1] ${ }^{2}$ | $\begin{gathered} 0.813 \\ \mathrm{~mm} / \mathrm{mm} \\ \hline \end{gathered}$ |  |  |  |
| Roll Force | FEM | 49 kN | +7.7\% |  |
|  | Theoretical Lee $[5.2]^{3}$ | 46 kN |  |  |  |

[^4]
a. Cross-sectional profile and area after Stand \#4.

c. Plastic Strains after Stand \#4.

b. Cross-sectional profile and area after Stand \#4.

d. Roll Force at Stand \#4.

Figure 5.6. Comparison of finite element and theoretical solutions for Stand \#4.

Table 5.8. Results after Stand \#4 of the Republic Engineered Products RSM.

| Finishing Stand \#4 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Parameter | Method | Value | \% Difference with |  |
|  |  |  | Theoretica I | Full-scale Mill Testing |
| Spread | FEM | 12.81 mm | -0.2 | -0.1 |
|  | Theoretical Lee [5.3] ${ }^{1}$ | 12.84 mm |  |  |
|  | Full-scale Mill Testing | 12.82 mm |  |  |
| Cross-sectional Area | FEM | $128.84 \mathrm{~mm}^{2}$ | -1.3 | +1.9 |
|  | Theoretical Lee [5.3] | $130.59 \mathrm{~mm}^{2}$ |  |  |
|  | Full-scale Mill Testing | $128.15 \mathrm{~mm}^{2}$ |  |  |
| Percentage Reduction | FEM | 4.51 \% | +14.5 | -6.6 |
|  | Theoretical Lee [5.3] | 3.95\% |  |  |
|  | Full-scale Mill Testing | 4.83 \% |  |  |
| Incremental Plastic Strain | FEM | $\begin{gathered} 0.081 \\ \mathrm{~mm} / \mathrm{mm} \\ \hline \end{gathered}$ | +1.25 |  |
|  | Theoretical Lee $[5.1]^{2}$ | $0.08 \mathrm{~mm} / \mathrm{mm}$ |  |  |  |
| Total Plastic Strain | FEM | $\begin{gathered} 0.982 \\ \mathrm{~mm} / \mathrm{mm} \\ \hline \end{gathered}$ | +13 |  |
|  | Theoretical Lee $[5.1]^{2}$ | $\begin{gathered} 0.869 \\ \mathrm{~mm} / \mathrm{mm} \end{gathered}$ |  |  |  |
| Roll Force | FEM | 30.7 kN | +20.5 |  |
|  | Theoretical Lee $[5.2]^{3}$ | 26 kN |  |  |  |

[^5]

Figure 5.7. Finite element solution of total plastic strain variation in stock at each stand.

### 5.2.5. Are Customer Requirements Satisfied?

The geometric requirements of the finished rod are stated in Table 5.10 and were provided by the U.S. automotive supplier and are based on ASTM standards [5.8]. Tables 5.8 and 5.9 demonstrate good correlation of the finite element model with the design objective to produce rod with a circular cross section in the mill on-line. Note that the theoretical model does give a very good geometric prediction in this case. However, the theoretical model cannot consider steel grade and coupling effects. Furthermore, this type of model cannot predict the distribution of microstructural and mechanical properties throughout the rod. This is very important where a steel mill must satisfy customer requirements for a uniform distribution of mechanical and microstructural properties through out the rod. Although the finite results do not satisfy customer requirements fully in this case, it is expected that the predictions will improve as the finite element model includes all the coupling effects shown in Figure 2.3. This work demonstrates the potential for development of the proposed coupled thermo-deformationmicrostructural simulation model shown in Figure 2.2.

Table 5.9. Comparison of full-scale mill testing, FEM and theoretical geometric results at exit of fourth finishing stand in Republic Engineered Products, Lorain, OH.

| PARAMETER | FULL-SCALE <br> MILL TESTING $^{2}$ | FEM $^{\mathbf{3}}$ | THEORETICAL <br> [5.1-5.3] |
| :---: | :---: | :---: | :---: |
| Maximum Diameter ${ }^{1}$ | 12.82 mm | 12.81 mm <br> $(-0.1 \%)$ | 12.84 mm <br> $(+0.30 \%)$ |
| Minimum Diameter | 12.75 mm | 12.71 mm <br> $(-0.34 \%)$ | 12.79 mm <br> $(+0.31 \%)$ |
| Cross-sectional Area | $128.15 \mathrm{~mm}^{2}$ | $127.97 \mathrm{~mm}^{2}$ <br> $(-0.15 \%)$ | $128.75 \mathrm{~mm}^{2}$ <br> $(+0.47 \%)$ |

${ }^{1}$ Provided by Republic Engineered Products Ohio industrial partner.
${ }^{2}$ The quantity in parentheses represent the percentage difference between the parameter shown in the column and full-scale mill testing.
${ }^{3}$ The quantity in parentheses represents the percentage difference between the parameter shown in the column and the full-scale mill testing

Table 5.10. Geometry customer requirements and a comparison with full-scale mill testing, FEM and theoretical model.

| ASTM REQUIREMENTS |  | FULL-SCALE <br> MILL TESTING $^{3}$ | FEM | THEORETICAL <br> [5.1-5.3] |
| :---: | :---: | :---: | :---: | :---: |
| Roundness $^{\mathbf{1}}$ | 0.08 mm | 0.06 mm | 0.1 mm | $0.12 \mathrm{~mm}[4-6]$ |
| Tolerance $^{\mathbf{2}}$ | $\pm 0.08 \mathrm{~mm}$ | +0.07 mm | +0.06 mm | $+0.04 \mathrm{~mm}[4-6]$ |

${ }^{1}$ Roundness is the difference between maximum diameter and minimum diameter.
${ }^{2}$ Tolerance is the allowable difference in diameter between what a customer orders and what the steel mill delivers.
${ }^{3}$ Provided by Republic Engineered Products Ohio industrial partner.

### 5.3. Case Study \#2 - POSCO No. 3 Mill Roughing Stands

### 5.3.1. Product Manufactured in the Mill

The POSCO No. 3 mill consists of a total 29 stands from roughing to the finishing stage. The first four stands in the roughing stage are considered and finite element and theoretical solutions can be found in Lee et al. [5.1-5.3]. The material considered is AISI 1010 mild carbon steel.

### 5.3.2. Configuration of the Stands

The details of the POSCO No. 3 mill, Pohang, Korea for the first four roughing rolling stands and the incoming stock is defined in Table 5.11. The geometric details regarding the roughing rolling stands were obtained from Morgan [5.11]. Photos of the POSCO No. 3 mill are shown in Figure 5.8. Initial four stands of POSCO No. 3 mill consists of four roughing stands with a pass sequence of box-oval-round-oval. Stand \#1 consists of two box grooved rolls and input stock is of square cross-section (Figure 5.1c). Stand \#2 consists of two oval grooved rolls with same orientation as Stand \#1 and the output of the Stand \#1 is used as input stock for this stand but is twisted $90^{\circ}$. Stand \#3 consists of two round grooved rolls with same orientation as Stand \#2 and the output of the Stand \#2 is used as input stock for this stand with a $90^{\circ}$ twist. Stand \#4 consists of two oval grooved rolls with same orientation to Stand \#3 and the output of the Stand \#3 is used as input stock for this stand with a $90^{\circ}$ twist.

Table 5.11. Details of initial four roughing stands of POSCO No. 3 mill.

| Roughing Rolling Stands |  | Incoming Stock |  |
| :---: | :---: | :---: | :---: |
| Stand Sequence | Box-oval-round-oval | Translational Speed | $0.06275 \mathrm{~m} / \mathrm{s}$ |
|  | Stands 1-2: 3300 mm ; | Cross Section Profile | 162 mm Square Billet |
| (On-center) | Stands 2-3: 5500 mm ; Stands 3-4: 3500 mm | Section Length | The stock is continuously fed into the stands. |
| Roll Diameters | Stand \#1: 700 mm ; <br> Stand \#2: 700 mm ; <br> Stand \#3: 650 mm ; <br> Stand \#4: 650 mm | Material | AISI 1010 <br> Low Carbon |
| Roll Gaps | Stand \#1: 15 mm ; Stand \#2: 15 mm ; Stand \#3: 10 mm ; Stand \#4: 10 mm | Chemical Composition | $\begin{gathered} \text { C-0.10, Mn-0.34, } \\ \text { P-0.025, S-0.02 (wt. \%) } \end{gathered}$ |
| Roll Groove Geometries | Defined by Morgan [5.11] | Austenite Grain Size | Not Applicable |
| Roll Material | High Strength Steel |  |  |
| Twist Rolling | All Horizontal Stands <br> Twist Guides are used to twist the Stock $90^{\circ}$ between stands | Temperature | Uniform at $1000{ }^{\circ} \mathrm{C}$ |
| Roll Temperatures | Not Applicable | Strain Rate Range | $0-0.2 \mathrm{~s}^{-1}$ |


|  | Stand \#1: $2.8 \mathrm{rpm} ;$ <br> Rotational Speed <br> of Rolls | Stand \#2: 3.5 rpm; <br> Stand \#3: $5.7 \mathrm{rpm} ;$ <br> Stand \#4: 7.1 rpm | Specific Heat |
| :---: | :---: | :---: | :---: |

${ }^{1}$ Linear dimensions at room temperature is corrected by $+1 \%$ due to thermal expansion from room temperature to $1000{ }^{\circ} \mathrm{C}$ (Commonly used by Morgan Construction Company [5.11])

a. Mill Overall View

b. Stand Configuration

Figure 5.8. Roughing stands POSCO No. 3 mill.

### 5.3.3. How is the Problem Modeled using FEM?

The commercial finite element code ABAQUS/Explicit [5.10] was used in this work. Table 5.12 states the assumptions, solution techniques and other modeling parameters used in the finite element simulation of the POSCO No. 3 mill. Each item
shown in Table 5.12 is discussed in-depth in Appendix E. For this study, the POSCO No. 3 mill was analyzed as a complete assembly i.e., four stands. A finite element pre and post-processor program is written using Python script and Java (Appendix A \& B) to analyze the results of the finite element solution and verify it with theoretical results.

Table 5.12. Details of ABAQUS/Explicit finite element model for the POSCO No. 3 mill roughing stands.

| Formulation | Mesh Domain | Lagrangian |
| :---: | :---: | :---: |
|  | Time Dependence | Transient |
|  | Time Integration | Explicit, Dynamics, Adiabatic. <br> Optimal time step is decided automatically by ABAQUS |
|  | Dimensionality | Three-Dimensional |
|  | Mass Scaling | None |
|  | Adaptive Meshing | Lagrangian Analysis: No |
|  | Hourglass | Artificial Stiffness |
| Stock | Element Type | Linear Hexahedral Brick (C3D8R), Deformable, Reduced Integration |
|  | Mesh Characteristics | \#of Nodes: 4753 \#of Elements: 3456 \#of DOF: 14307 (including Lagrange Multipliers) |
|  | Material | Homogeneous and Isotropic |
|  | Length | $2.5 \mathrm{~m}^{1}$ |
|  | Rate Dependence | Yes |
|  | Spring Back Calculation | No |
|  | Plasticity Law | Shida ${ }^{2}$ [5.4] |
|  | Hardening Rate | Isotropic |
|  | \% Plastic Deformation Energy Converted to Heat | 0.90 [5.9] |
|  | Initial Conditions | Initial Velocity of the Stock; Initial Temperature of the Stock |
| Roll | Material | Rigid |
|  | Finite Element Characterization | Analytic Rigid Surface |
|  | Boundary Conditions | Rotational Speed of Rolls in Table 5.11 |
| Stock / Roll Interface | Contact Condition | Tangential: Penalty; Normal: Hard |
|  | Friction Model | Coulomb ( $\mu=0.3$ ) |
|  | Heat Transfer Effects | Not Applicable |
| Stand | Material | Rigid Pin support at Roll |
|  | Model Spacing (On-center) ${ }^{1}$ | Stands 1-2: 850 mm ; Stands 2-3: 900 mm ; Stands 3-4: 900 mm |
|  | Orientation ${ }^{3}$ | Stand \#1: Vertical; Stand \#2: Horizontal; Stand \#3: Vertical; Stand \#4: Horizontal |

[^6]The solution procedure used here is similar to that described in Section 5.1.3. An in-depth discussion of the items in Table 5.12 is given in Appendix E.


Figure 5.9. Arrangement of ABAQUS/Explicit rolling stands in POSCO No. 3 mill.

### 5.3.4. Comparison of Finite Element Results with Theoretical Calculation

A simplified version of the proposed rolling model was analyzed. Once the finite element analysis is completed, the model is validated against theoretical models. Table 5.13 summarizes the finite element and theoretical results for spread, cross-sectional area, percentage reduction in area, incremental plastic strain, total plastic strain and roll force at all four roughing stands. Figures 5.10 to 5.14 compares the finite-element and theoretical, results for the cross-sectional profile, incremental plastic strain, total plastic strain and roll force at stands \#1 through \#4. Finite element plots of the cross-sectional plastic strain distribution at stands \#1 through \#4 are shown in Figure 5.13.

Table 5.13. Comparison of full-scale mill testing, FEM and theoretical geometric results at each roughing stand for POSCO No. 3 mill.

| Characteristics of Finite Element Model | Formulation Type |  |  | Lagrangian |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | Shida [F.3] |
|  | Number of Nodes |  |  | 3456 |
|  | Number of Elements Freedom in the problem |  |  | 4753 |
|  | Number of Degrees of Freedom (Including Lagrange multipliers) |  |  | 14307 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 182.58 \\ (-2.7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 196.36 \\ (4.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 114.68 \\ (-3.8 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 146.84 \\ (-3.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 187.65 | 187.97 | 119.27 | 152.18 |
| Cross-sectional Area (mm ${ }^{2}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{aligned} & 20352.26 \\ & (-2.3 \% \mathrm{~T}) \\ & \hline \end{aligned}$ | $\begin{aligned} & 14546.11 \\ & (-0.4 \% \mathrm{~T}) \\ & \hline \end{aligned}$ | $\begin{aligned} & 10825.26 \\ & (-2.8 \% \mathrm{~T}) \end{aligned}$ | $\begin{gathered} 8119.19 \\ (-2.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 20828.64 | 14501.47 | 11142.66 | 8328.73 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 22.45 \\ (8.8 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 29.05 \\ (-4.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 25.04 \\ (8.1 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 24.99 \\ (-1.0 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 20.63 | 30.38 | 23.16 | 25.25 |
| Incremental Plastic Strain ${ }^{1}$ (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.414 \\ (8.7 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.777 \\ (-5.4 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 0.507 \\ (-3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.487 \\ (-10.8 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] | 0.381 | 0.821 | 0.523 | 0.540 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.414 \\ (8.7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 1.293 \\ (8.0 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 1.795 \\ (4.34 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 2.124 \\ (-6.3 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.381 | 1.197 | 1.720 | 2.266 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 2406.03 \\ (-29.1 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 2673.21 \\ (-34.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 2003.48 \\ (-37.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 1692.73 \\ (-46.8 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 3394 | 4069 | 3196 | 3182 |

T - \% Difference with theoretical method.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

Overall there is very good correlation between the finite element solution and theoretical solution for spread and cross-sectional area of the stock. The percentage difference between finite element solution and theoretical solution for spread and cross-sectional area is a maximum of $5 \%$ and in most cases within $2 \%$. It can be concluded that for all four stands, the finite element solution for cross-sectional area is less than theoretical cross-sectional area.

There is no full-scale mill testing data available for incremental plastic strain and total plastic strain, therefore, only the theoretical and finite element solutions are compared. The theoretical and finite element solutions for incremental plastic strain and total plastic strain are consistent for initial stands. However, the difference between them increases with successive stands due to error accumulation ${ }^{5}$ from the previous stands. The incremental plastic strain finite element solution is generally less than the theoretical solution. The total plastic strain finite element solution is generally greater than the theoretical solution. The maximum percentage difference is $10 \%$. The finite element solution however is more useful since it can calculate strain distribution, which is helpful for calculating mechanical properties and microstructure.

There is no full-scale mill testing data available for the roll force, therefore, only the theoretical and finite element solutions are compared. The finite element solution for roll force is $\approx 30-50 \%$ less than the theoretical solution for all stands. This appears very large and is probably due to the fact that the actual model for calculating roll force by Lee [5.2] uses two parameters that are experimentally determined. In absence of experimental data these two parameters were determined theoretically ${ }^{6}$. It was observed that the roll force obtained by the finite element solution is consistent within $10 \%$ of a proprietary Morgan [5.11] technique for calculating roll force. The proprietary model employs a combination of empirical techniques and experimental validation.

[^7]

c. Roll Force at Stand \#1.

Figure 5.10. Comparison of finite element and theoretical solutions for Roughing Stand \#1.

Table 5.14. Results after roughing Stand \#1 of the POSCO No. 3 mill.

| Roughing Stand \#1 |  |  |  |
| :---: | :---: | :---: | :---: |
| Parameter | Method | Value | \% Difference <br> with Theoretical |
| Spread | FEM | 182.58 mm | -2.7 |
|  | Theoretical Lee <br> [5.3] | 187.65 mm |  |
| Cross-sectional Area | FEM | $20352.26 \mathrm{~mm}^{2}$ | +8.8 |
| Percentage Reduction <br> in Cross-sectional <br> Area | FEM | $22.45 \%$ |  |
| Theoretical Lee [5.3] | $20828.64 \mathrm{~mm}^{2}$ | Theoretical Lee [5.3] | $20.63 \%$ |

${ }^{1}$ Spread factor $\beta=0.83$
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.9].
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

a. Cross-sectional profile and area after Stand \#2.

b. Plastic Strains after Stand \#2.


Figure 5.11. Comparison of finite element and theoretical solutions for Roughing Stand \#2.

Table 5.15. Results after roughing Stand \#2 of the POSCO No. 3 mill.

| Roughing Stand \#2 |  |  |  |
| :---: | :---: | :---: | :---: |
| Parameter | Method | Value | \% Difference with Theoretical |
| Spread | FEM | 196.36 mm | 4.5 |
|  | Theoretical Lee [5.3] ${ }^{1}$ | 187.97 mm |  |
| Cross-sectional Area | FEM | $14440.42 \mathrm{~mm}^{2}$ | -0.4 |
|  | Theoretical Lee [5.3] | $14501.47 \mathrm{~mm}^{2}$ |  |
| Percentage Reduction in Cross-sectional Area | FEM | 29.04 \% | -4.4 |
|  | Theoretical Lee [5.3] | 30.38 \% |  |
| Incremental Plastic Strain | FEM | $0.777 \mathrm{~mm} / \mathrm{mm}$ | -5.4 |
|  | Theoretical Lee [5.1] ${ }^{2}$ | $0.821 \mathrm{~mm} / \mathrm{mm}$ |  |
| Total Plastic Strain | FEM | $1.293 \mathrm{~mm} / \mathrm{mm}$ | 8.0 |
|  | Theoretical Lee [5.1] ${ }^{2}$ | $1.197 \mathrm{~mm} / \mathrm{mm}$ |  |
| Roll Force | FEM | 2673.21 | -34.3 |
|  | Theoretical Lee [5.2] ${ }^{3}$ | 4069 |  |

${ }^{1}$ Spread factor $\beta=1.00$
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.9].
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.



Figure 5.12. Comparison of finite element and theoretical solutions for Roughing Stand \#3.

Table 5.16. Results after roughing Stand \#3 of the POSCO No. 3 mill.

| Roughing Stand \#3 |  |  |  |
| :---: | :---: | :---: | :---: |
| Parameter | Method | Value | \% Difference with Theoretical |
| Spread | FEM | 114.68 mm | -3.8 |
|  | Theoretical Lee [5.3] ${ }^{1}$ | 119.27 mm |  |
| Cross-sectional Area | FEM | $10825.26 \mathrm{~mm}^{2}$ | -2.9 |
|  | Theoretical Lee [5.3] | $11142.66 \mathrm{~mm}^{2}$ |  |
| Percentage Reduction in Crosssectional Area | FEM | 25.03 \% | 8.1 |
|  | Theoretical Lee [5.3] | 23.96 \% |  |
| Incremental Plastic Strain | FEM | $0.507 \mathrm{~mm} / \mathrm{mm}$ | -3.1 |
|  | Theoretical Lee [5.1] ${ }^{2}$ | $0.523 \mathrm{~mm} / \mathrm{mm}$ |  |
| Total Plastic Strain | FEM | $1.795 \mathrm{~mm} / \mathrm{mm}$ | +4.3 |
|  | Theoretical Lee [5.1] ${ }^{2}$ | $1.720 \mathrm{~mm} / \mathrm{mm}$ |  |
| Roll Force | FEM | 2003.48 | -37.3 |
|  | Theoretical Lee [5.2] ${ }^{3}$ | 3196 |  |

${ }^{1}$ Spread factor $\beta=0.83$
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.9].
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

a. Cross-sectional profile and area after Stand \#4.

b. Plastic Strains after Stand \#4.

c. Roll Force at Stand \#4.

Figure 5.13. Comparison of finite element and theoretical solutions for Roughing Stand \#4.

Table 5.17. Results after roughing Stand \#4 of the POSCO No. 3 mill.

| Roughing Stand \#4 |  |  |  |
| :---: | :---: | :---: | :---: |
| Parameter | Method | Value | $\begin{gathered} \hline \text { \% Difference } \\ \text { with } \\ \text { Theoretical } \end{gathered}$ |
| Spread | FEM | 146.84 mm | -3.5 |
|  | Theoretical Lee [5.3] ${ }^{1}$ | 152.18 mm |  |
| Cross-sectional Area | FEM | $8119.19 \mathrm{~mm}^{2}$ | -2.5 |
|  | Theoretical Lee [5.3] | $8328.73 \mathrm{~mm}^{2}$ |  |
| Percentage Reduction | FEM | 24.99 \% | -1.0 |
|  | Theoretical Lee [5.3] | 25.25 \% |  |
| Incremental Plastic Strain | FEM | $0.487 \mathrm{~mm} / \mathrm{mm}$ | -10.8 |
|  | Theoretical Lee [5.1] ${ }^{2}$ | $0.540 \mathrm{~mm} / \mathrm{mm}$ |  |
| Total <br> Plastic Strain | FEM | $2.124 \mathrm{~mm} / \mathrm{mm}$ | -6.3 |
|  | Theoretical Lee [5.1] ${ }^{2}$ | $2.266 \mathrm{~mm} / \mathrm{mm}$ |  |
| Roll Force | FEM | 1692.73 | -46.8 |
|  | Theoretical Lee [5.2] ${ }^{3}$ | 3182 |  |

[^8]
a. Arrangement of rolling stand in multi-stand rolling (Repeated from Figure 5.9).


Figure 5.14. Finite element solution of total plastic strain ( $\mathrm{mm} / \mathrm{mm} \mathrm{)} \mathrm{in} \mathrm{stock}$.

## 6. Conclusion

A Java pre- and post-processing graphical user-oriented interface has been developed to aid a mill engineer with little or no finite element experience throughout the analysis process of the finishing rolling stands. This work validated the application of ABAQUS/Explicit Lagrangian solution modeling technique to simulate both high speed finishing stand (Republic Engineered Products RSM mill) and slow speed roughing stand (First four stands of POSCO No. 3 mill) rolling. It has been demonstrated that the finite element modeling techniques used in this work successfully predict geometrical shape (spread, cross-sectional area and shape of the stock), incremental plastic effective strain and total plastic effective strain for a wide range of rolling speed $(0.05-0.2 \mathrm{~m} / \mathrm{s}$ and 19$30 \mathrm{~m} / \mathrm{s}$ ), strain rate ( $0.1-0.2 \mathrm{~s}^{-1}$ and $350-500 \mathrm{~s}^{-1}$ ) and different stock materials (AISI 1010 and AISI 1045 steel). In this work various strain rate and temperature dependent plasticity models were used. It has been found that parameters like geometrical shape (spread, cross-sectional area and shape of the stock) vary negligibly with the employment of these models instead of using a simple plastic strain model considered in previous work [6.1]. However the roll force varies significantly with different plasticity model. Though it has been demonstrated that roll force data doesn't compare well with the available theoretical model it has been found that the roll force data obtained from the finite element analysis is consistent to results obtained by a proprietary Morgan technique. The Morgan roll force model employs a combination of empirical techniques that have been experimentally validated. In this work a thermo-mechanically coupled finite element model has been employed. It has been found that parameters like geometrical shape vary negligibly with the employment of the thermo-mechanically coupled finite element model instead of using a thermally uncoupled model used in previous work [6.1].

The ability to accurately predict formed geometrical shape (spread, cross-sectional area and shape of the stock), incremental plastic effective strain and total plastic effective strain, based on process parameters, is very encouraging. The simulation approach described herein can still be used to evaluate roller groove-shapes, root diameters, and tolerances of the roll shape and positions within a stand. The finite element solution for the last stand of Republic Engineered Products RSM mill lies within the ASTM [6.2] roundness and tolerance requirements. This capability is presently valuable for the purpose of design comparisons.

## 7. Future Work

Initial work done on the finite element modeling and theoretical solution of Republic Engineered Products finishing stands and POSCO No. 3 mill roughing stands has yielded important information and insight on how to carry out future work for fullscale rolling mill simulation and the best way of achieving it. The major thrust of any future work should be in evaluating the complete range of parameters important to designers and manufacturers of rolling mills, both theoretically and by the finite element method. Furthermore, improving both theoretical and finite element solutions to meet the customer requirements of tolerance in various parameters of the output rolled product. The complete research and developmental work required to be done is listed briefly in Figure 2.2. In this chapter we will discuss some aspects of future work.

### 7.1. Theoretical Thermo-Mechanical Model

### 7.1.1. Theoretical Calculation of Stock Temperature during the Rolling Process

Temperature of stock during the rolling process varies from stand to stand due to following mechanisms:

- Heat Generation Due to Plastic Deformation. Heat is generated in the stock when plastic deformation of the stock takes place as a part of the energy expended to deform the stock is converted into heat.
- Friction Between Stock and Rolls. Some part of the work due to friction is converted into heat and then some part of this heat is transferred to the stock.
- Heat Transfer. Heat transfer mechanisms include conduction (between roll and stock), convection (between stock and environment), and radiation (between stock and environment).

Several researchers have attempted to calculate stock temperature distribution in multi stand rolling using different assumptions. They include Lee et al. [7.1] and Serajzadeh et al. [7.2].

Lee et al. [7.1] in 2002 applied the equivalent circle approximation to the temperature distribution problem in the multi-stand rolling problem and developed a onedimensional axisymmetric differential equation of the temperature distribution, which was then solved by finite difference method using the boundary condition of BraunAngott et al. [7.3] and Carnahan [7.4]. The heat transfer equation is given by the following

$$
\begin{align*}
& \frac{\partial}{\partial r}\left(k \frac{\partial T}{\partial r}\right)+\dot{q}=\rho C_{p} \frac{\partial T}{\partial t},  \tag{7.1a}\\
& \dot{q}=\chi \frac{\sigma \dot{\varepsilon}}{\rho \beta C_{p}} \tag{7.1b}
\end{align*}
$$

where, T is the stock temperature, t is time, k is conductivity, $\rho$ is stock density, $\chi$ is fraction of plastic deformation work converted in to heat in stock, $\beta$ is mechanical equivalent of heat, $\mathrm{C}_{\mathrm{p}}$ is specific heat of stock, $\sigma$ is stock flow stress, $\dot{\varepsilon}$ is stock strain rate and $\dot{q}$ is heat generation rate of stock. This model only accounts for conduction in the stock.

Serajzadeh et al. [7.2] in 2002 considered a more general case where the heat transfer in the peripheral direction is negligible. The governing partial differential equation is given as follows

$$
\begin{equation*}
\frac{1}{r} \frac{\partial}{\partial r}\left(k \frac{\partial T}{\partial r}\right)+\frac{\partial}{\partial z}\left(k \frac{\partial T}{\partial z}\right)=\rho C_{p} \frac{\partial T}{\partial t} \tag{7.2a}
\end{equation*}
$$

with the following initial and boundary conditions

$$
\begin{align*}
& T(r, z, t=0)=T_{0}  \tag{7.2b}\\
& \left(-k \frac{\partial T}{\partial r}\right)_{r=R}=h^{*}(t)\left(T_{r}-T\right)  \tag{7.2c}\\
& \left(-k \frac{\partial T}{\partial r}\right)_{r=r^{*}}=0 \tag{7.2d}
\end{align*}
$$

where $\mathrm{T}, \mathrm{t}, \mathrm{r}, \rho, \mathrm{k}$ and $\mathrm{C}_{\mathrm{p}}$ are temperature, time, distance from roll axis, density, heat conductivity and specific heat of the stock, respectively. Also, $\mathrm{T}_{\mathrm{r}}$ is roll surface temperature, $\mathrm{h}^{*}$ is convective coefficient between roll and stock and $\mathrm{r}^{*}$ is the radius below which heat transfer can be neglected.

### 7.1.2. Microstructure Evolution of Stock During the Rolling Process

An important customer requirement that has to be determined is microstructure evolution of the stock during rolling since mechanical properties of the output products depend on microstructure. According to mainstream literature microstructure depends on the following parameters:

- Temperature Distribution in the Stock
- Strain and Strain Rate in the Stock
- Inter-Stand time
- Cooling Mechanism of the Stock

Several researchers have proposed different models to calculate the microstructure evolution of the stock during multi-stand rolling. Prominent among them are Sellars [7.5], Yanagimoto et al. [7.6] and Farrugia et al. [7.7].

### 7.2. Finite Element Modeling

### 7.2.1. Calculation of Output Parameters for Rolling Mill by post processing FEM Output Results

The commercial finite element software ABAQUS is used to solve the rolling mill simulation problem where output is determined in terms of general mechanical variables that include displacement, strain, stress energy, etc. These results have to be post processed using an in-house code for calculating parameters important to designers and manufacturers of rolling mills. Although some parameters such as spread, plastic strain, cross sectional area of the stock after each stand have been calculated in this work by post-processing the finite element results the complete range of parameters including roll torque and the power requirements have to be calculated in this way.

### 7.2.2 Improvements to the Finite Element Model

The finite element model currently used in this work is based on Lagrangian and transient Arbitrary Eulerian-Lagrangian (ALE) formulations. Though these models yield results that are generally in agreement with the experimental geometrical data, these methods are computationally expensive. Another way of modeling the problem is the steady-state ALE formulation. This method requires an initial guess of the threedimensional stock geometry at each stand as well as between stands. The closer the initial geometry is, to the actual geometry, the faster the solution time. A theoretical threedimensional geometrical solution for the stock, in multi-stand rolling has been developed by Bayoumi et al. [7.8]. If used as an initial geometric guess in the steady-state ALE formulation, this approximate three-dimensional geometrical solution can be used to reduce solution time. If this approach is successful the flowchart of the model in Figure 2.3 would become Figure 7.1 the step (box) second from the top has been added.

### 7.3. Improvement of Theoretical-Empirical Model Based on Numerical Experiments

While it is known that solution to the multi-stand rolling problem is influenced by numerous factors such as stock velocity and stand spacing most theoretical-empirical models neglect most factors for simplicity. For example, the most recent theoreticalempirical model by Lee et al. [7.9] to calculate spread assumes that spread depends only on stock and roll geometry. This is because almost all past models depend on various experimentally determined coefficients, which are expensive enough to study all the parameters affecting the ultimate result. A well-established and validated finite element model in contrast can be used in place of experiments. Numerical experiments cost only a fraction of actual experimentation and can be used to study effect of the above-discussed parameters. Results of these experiments can then be included to generalize theoreticalempirical models. This approach is very feasible due to rapidly decreasing computing costs.


Figure 7.1. Proposed flowchart if steady-state finite element modeling is successful.

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# Appendix A: Pre-processing Finish Rolling Stage GUI for ABAQUS 

## A.1. Introduction

A Java pre-processing graphical user interface (GUI) has been developed so that a mill engineer can define a finite element model of the mill setup. Using the analysis results the engineer can determine whether or not the mill setup satisfies customer requirements. The major reason why the java language was selected is that it is platform independent; therefore code does not have to be recompiled. The GUI was developed using the Java ${ }^{\text {TM }}$ Platform Standard Edition [A.2]. the mill engineer can input groove geometry data, stock geometry data, stock material property data, element and mesh information, boundary and initial conditions, stock/roll friction, temperature related data, etc. Once the stands and stocks are defined, the pre-processor creates a Python script file. Through the ABAQUS/CAE interface the Python script is used to automatically generate an input file (pre-processing stage) of the finite element model. to create the input file for ABAQUS to carry out a rolling simulation at the finishing stage for steel rods/bars. The interface allows the user to input groove geometry data, stock geometry data, stock Material property data, element and mesh information, boundary and initial conditions, and temperature related data. Using this input information the Java program creates a Python script file [A.1]. Through the ABAQUS/CAE interface the Python script file is used to generate a finite element input file (pre-processing stage) of the actual physical phenomena. The finite element model is then solved using the ABAQUS solver (processing stage). The output file can be opened and results viewed in ABAQUS/Viewer or Visualization Module of ABAQUS/CAE. Analysis results can also be calculated in terms of Rolling Parameters using the Java Post-processing program (Appendix B).

## A.2. Programming Environment

The GUI was written using the Java programming language. Java is both a program environment and a language developed by Sun Microsystems, Inc. [A.2]. Any program that is written in Java can run on any computer as long as the "Java Virtual Machine (JVM)" is installed. The JVM is real standard for an imaginary machine. The standard reflects the basic capability of all computer platforms (all CPUs as well as all operating systems). With Java, a programmer no longer writes code for a particular real platform but instead for this imaginary computer. Each real computer can run this platform independent code by becoming (through software) this Java Virtual Machine. The major reason why Java was selected for this project is due to its portability of being used on different computer without rewriting the code. The GUI was developed using the Java Development Kit (JDK) version 1.4.1 [A.3]

## A.3. Steps of Rolling Simulation Analysis

The first stage requires the user provides input in the Pre-processor GUI to define the finite element model that will be solved using in ABAQUS. The input values are validated and then the Python Script (.py) file is created. This file contains all the preprocessing information to define the problem. The user then enters ABAQUS/CAE with the Python script file in RUN-SCRIPT mode. From the ABAQUS/CAE GUI the analysis (processing) job is submitted. After the analysis is over the results are stored in a output database (.odb) file. The output file can be opened and results viewed in ABAQUS/Viewer or Visualization Module of ABAQUS/CAE. Analysis results can also be calculated in terms of Rolling Parameters using the Java Post-processing program (Appendix B). Architecture used in the rolling process is shown in Figure A.1.


Figure A.1. Flowchart for GUI software.

## A.4. Pre-processor GUI Screen Layout

## A.4.1. GUI Layout

The GUI is divided in three frames, i.e., upper-left, upper-right and lower frames. The upper left-hand frame shows different roll configuration options (Roll geometry, Roll properties etc.) and the screen layout is similar to MS Windows Explorer. The upper right-hand frame is where the user defines input parameters for the rolling simulation (see next section). The lower frame displays the input information defined by the user in the upper-right hand frame, e.g., the user can visualize the geometry of the roll grove geometry to ensure that the data has been entered correctly. The user cannot interact with the lower frame.

## A.4.2. Input Modules

The GUI is divided into three main modules that are displayed in the upper righthand frame of Figure A. 1 as follows:

1. Rolling Stands: This module is divided into following sub-modules:
1.1. Roll and Groove geometry: The user defines Roll and Groove Geometry of the roll in this module.
1.2. Roll Properties: The user defines Roll Material Properties in this module.
1.3. Roll Boundary Conditions: The user defines Roll Boundary Conditions in this module.
2. Input Stock: This module is divided into following sub-modules:
2.1. Feed Section Geometry: The user defines Feed Section Stock Geometry in this module.
2.2. Stock properties: The user defines Stock Material Properties in this module.
2.3. Stock Initial Conditions: The user defines Stock Initial Conditions in this module.
2.4. Stock Meshing: The user defines Stock Mesh Information in this module.
3. Contact Information: The user defines Roll/Stock Contact Information in this module.

## A.4.2.1. Roll \& Groove Geometry Module

The user enters the input parameters related to the groove and roll geometry in this module. The screen layout of the groove geometry module is shown in Figure A.4. The input data required is shown in the upper right-hand side frame in Figure A.4. The geometry module is accessed through the Groove Geometry menu. The geometry of the groove and roll geometry is displayed in the lower frame.

The user can select the Stand No. in the upper left-hand frame. They can be either Finish round or Oval round. The finish round requires two radii to define the groove geometry and they are Open Radius and Relief Radius. Oval round is relatively simple as it involves only Open radius. Detailed geometric specifications of these two types of groove Geometry is shown below.


Figure A.2. Finish groove.


Figure A.3. Oval groove.
There are three buttons in the lower part of the frame namely "OK", "Change" and "Accept". Initially only "OK" button is enabled, the other two buttons are disabled.

A list of possible user interactions with these buttons and their results are given below in a Table A.1.

Table A.1. Possible User Interactions

| User Action | Result |
| :---: | :---: |
| User clicks the "OK" button | If all the geometric parameters are entered properly in the input text fields, then, <br> - The groove geometry is drawn in the lower frame. <br> - The input text-fields are disabled. <br> - Change button remains enabled. <br> If all the required data for the model (Roll \& Stock) is already filled out <br> - "Accept" button becomes enabled. <br> - "OK" button itself is disabled. <br> If no data is entered in the input text fields, then <br> - An error message is shown to the user and he is prompted to enter data in the input text-fields. <br> If data entered in the input text fields are invalid, then <br> - An error message is shown to the user and he is prompted to enter proper data in the input text-fields. |
| User clicks on the "Change" button | - The input text-fields are enabled so that the user can change them. <br> - "OK" button becomes enabled. <br> - "Change" button remains enabled. <br> - "Accept" button is disabled. |
| User clicks on the "Accept" button | The python script (.py) file for defining the FEA model is generated |



Figure A.4. Screen layout of the groove geometry Module.

## A.4.2.2. Roll Properties

The screen layout for this module is shown in Figure A.5. The user inputs the data related to Roll Material properties in this module. These include Roll Type (RIGID / DEFORMABLE) and Roll density. In this work only rigid rolls are considered.
"OK", "Change", "Accept" button functions in the same way as described in the Roll \& Groove Geometry Module.


Figure A.5. Screen Layout of the Roll Properties Module.

## A.4.2.3. Roll Boundary Conditions

The screen layout for this module is shown in Figure A.6. The user inputs the Rotational Speed of Rolls of successive rolling stands as boundary conditions in this module.
"OK", "Change", "Accept" button functions in the same way as described in the Roll \& Groove Geometry Module.


Figure A.6. Screen Layout of the Roll Boundary Conditions Module.

## A.4.2.4. Feed Section Geometry

The user enters the input data related to the Feed Section (input stock at the 1st Stand) geometry in this module. The stock geometry module is shown in Figure A.7. The stock can be specified in two ways as shown by the radio buttons in Figure A.7. If the stock is a perfect circle then a radius is only required as shown in Figure A.7. In general a stock is not a perfect circle and can be defined though a file that specifies the ( $\mathrm{X}, \mathrm{Y}$ ) coordinates of surface points on the stock section. The file containing the geometric location of surface points is input though the input window as shown in Figure A.8. The software assumes that the origin $(0,0)$ is located at the geometric center of the stock cross section.
"OK", "Change", "Accept" button functions in the same way as described in the Roll \& Groove Geometry Module.


Figure A.7. Screen layout for entering stock geometry data


Figure A.8. Screen layout for specifying the file, which contains stock geometry data for stock geometry Module.

## A.4.2.5. Stock Properties

The screen layout for this module is shown in Figure A.9. The user inputs the data related to the Material properties of the stock (rod/bar) that include Density, Young's modulus, Poisson's ratio, Yield point, Specific Heat and Heat Conversion Fraction in this module. The number of points for defining the plastic region can be specified in the last input text-field. After this input text-field is specified the user can click on the "Get data for stress strain curve" button to get actual Flow Stress Data corresponding to Plastic Strain and Temperature. On clicking this button a new window opens up (Figure A.10). User can enter the Plastic Strain data in table shown in this window. On clicking "OK" button in this window the data is stored and the window closes itself.
"OK", "Change", "Accept" button functions in the same way as described in the Roll \& Groove Geometry Module.


Figure A.9. Screen Layout of the Material data Module.


Figure A.10. Screen layout for entering plastic strain curve.

## A.4.2.6. Stock Initial Conditions

The user specifies input data related to initial conditions of the stock in this module. The stock initial conditions module is shown in Figures A.11. Initial velocity in the Rolling direction and Temperature is required as input in this module.


Figure A.11. Screen layout stock initial conditions Module.
"OK", "Change", "Accept" button functions in the same way as described in the Roll \& Groove Geometry Module.

## A.4.2.7. Stock Meshing Module

The screen layout for this module is shown in Figure A.12. The user inputs the Element Shape, Element library, Element Geometric Order, Kinematic Split Options and Hourglassing Options in this module.
"OK", "Change", "Accept" button functions in the same way as described in the Roll \& Groove Geometry module.


Figure A.12. Screen layout stock meshing Module.

## A.4.2.8. Contact Information

The screen layout for this module is shown in Figure A.13. The user inputs the Roll/Stock contact behavior including normal contact behavior, tangential contact behavior and coulomb friction co-efficient between Roll and Stock in this module.
"OK", "Change", "Accept" button functions in the same way as described in the Roll \& Groove Geometry module.


Figure A.12. Screen layout Roll/Stock Contact Information Module.

## Appendix B: Post-processing Finite Element Simulation Results

## B.1. Introduction

A program has been developed using the Python scripting language and Java $2^{\mathrm{TM}}$ platform to post-process the results from finite element simulation in ABAQUS/Explicit. The purpose of this post-processor is to calculate parameters like spread, cross-sectional area of the stock, incremental plastic strain, total plastic strain and roll force from the solution data written by ABAQUS during the analysis.

## B.2. Steps of Rolling Post-Processing

Initially the data generated by ABAQUS analysis is contained in a output database (.odb) file. A Python script program uses this file as an input and generates ASCII results files. The Java post-processing program uses these ASCII results files as input. The Java program processes the ASCII data to calculate spread, cross sectional area of the stock, incremental plastic strain, total plastic strain and roll force.


Figure B.1. Flowchart for Java post-processing software.

## B.2.1. Python Script Program

This program reads the output database file and writes the following information into ASCII files as shown in Table B.1.

Table B.1. Information written by the python script program in the ASCII files.

| General Data | Total Number of Nodes |
| :---: | :---: |
|  | Total Number of Elements |
| Nodal Data | Node Number |
|  | Element Data |
|  | Nodal Coordinates |
|  | Element Number |
|  | Total Plastic Strain components at Element Integration Points |
| Contact Data | Element Connectivity |
|  | Normal Force at each Contact Nodes |

## B.2.2 Java Post-processing Program

The Java post-processing program reads the ASCII data from the data files generated by the Python script. Nodal and element data from the python script is separated into deformed zones based on the position of the nodes and elements relative to the position of the rolls. Spread and cross-sectional area of the stock are determined from the nodal data. It calculates the total and incremental strain from the element data. The roll force is calculated from the contact data.

## B.2.2.1. Spread Calculation

The boundary nodes and their nodal position within each deformed zone are calculated using the Graham Scan Algorithm [B.1]. The Graham Scan Algorithm [B.1] is used to determine the convex hull (boundary nodes) from a set of nodal data points. Then the program calculates spread at a given stand by calculating the average spread in the deformed zone after the given stand and before the next stand.

## B.2.2.2. Cross Sectional Area Calculation

The boundary nodes and their nodal position within each deformed zone is calculated using the Graham Scan Algorithm [B.1] for convex polygons. The program calculates the cross-sectional area at a given stand by calculating the average crosssectional area in the deformed zone after the given stand and before the next stand.

## B.2.2.3. Total Plastic Strain Calculation

The program calculates the total plastic strain at a given stand by calculating the volume averaged total plastic strain in the deformed zone after the given stand and before the next stand as follows (Lee et al. [B.3]):

$$
\begin{equation*}
\varepsilon^{T}=\frac{\sum_{i=1}^{N_{e}} V^{i} \varepsilon^{i}}{\sum_{i=1}^{N_{e}} V^{i}} \tag{B.1a}
\end{equation*}
$$

where $\varepsilon^{i}$ is the total plastic strain at the $\mathrm{i}^{\text {th }}$ element, $V^{i}$ is the volume of the $\mathrm{i}^{\text {th }}$ element and $\mathrm{N}_{\mathrm{e}}$ is the number of elements in the deformed zone.

## B.2.2.4. Incremental Plastic Strain Calculation

To calculate the incremental strain at a given stand the following method is used. First the deformed zone after the given stand and before the next stand is selected. After that individual elements in this deformed zone is identified. Increments in strain components of these elements are calculated by subtracting the total strain component data before deformation at the given stand (this data is available in the time dependent history output) from the final total strain component data. Then the following relation [B.2] calculates incremental plastic strain at $\mathrm{i}^{\text {th }}$ element

$$
\begin{equation*}
\Delta \varepsilon^{i}=\sqrt{\frac{2}{3}\left\{\left(\Delta \varepsilon_{x x}^{i}\right)^{2}+\left(\Delta \varepsilon_{y y}^{i}\right)^{2}+\left(\Delta \varepsilon_{z z}^{i}\right)^{2}+2\left(\Delta \varepsilon_{x y}^{i}\right)^{2}+2\left(\Delta \varepsilon_{y z}^{i}\right)^{2}+2\left(\Delta \varepsilon_{z x}^{i}\right)^{2}\right\}} \tag{B.2a}
\end{equation*}
$$

where $\Delta \varepsilon_{i j}^{i}$ is the incremental strain components at the $i^{\text {th }}$ element and $\Delta \varepsilon^{i}$ is the incremental plastic strain at the $i^{\text {th }}$ element.

The incremental effective plastic strain is calculated by volume averaging the incremental plastic strain at each element as follows (Lee et al. [B.3]):

$$
\begin{equation*}
\Delta \varepsilon=\frac{\sum_{i=1}^{N_{e}} V^{i} \varepsilon^{i}}{\sum_{i=1}^{N_{e}} V^{i}} \tag{B.2b}
\end{equation*}
$$

where $\Delta \varepsilon$ is the incremental plastic strain at the $\mathrm{i}^{\text {th }}$ element, $V^{i}$ is the volume of the $\mathrm{i}^{\text {th }}$ element and $\mathrm{N}_{\mathrm{e}}$ is the number of elements in the deformed zone.

## B.2.2.5. Roll Force Calculation

The program calculates the role force at a particular stand by adding up all the normal and tangential nodal forces at the nodes where the roll and stock is in contact at that stand in the direction perpendicular to both the direction of rolling and roll axes.

## B.3. Java Post-processor GUI Screen Layout

## B.3.1. GUI Layout

The GUI is divided in three frames, i.e., upper-left, upper-right and lower frames. The upper left-hand frame shows the link to the Post-processor screen and the screen layout is similar to MS Windows Explorer. The upper right-hand frame is where the user defines various post-processing options (see next section). The user cannot interact with the lower frame.

## B.3.2. Post-processor Module

The screen layout for this module is shown in Figure B.2. The user selects various post-processing options and also selects the General, Node, Element and Force data files (Table B.1). On pressing the "OK" button the post-processing is performed and output data is written in a file. The user also has the option of calculating the rolling parameters theoretically. To calculate the rolling parameters theoretically the user needs to specify one more file that contains the groove geometry, stock geometry and rotational roll speed data.


Figure B.2. Screen layout Post-processor Module

## Appendix C: Initial Finite Element Mesh

## C.1. Overview

To ensure solution quality throughout a rolling simulation the initial finite element mesh is very important. This section discusses the initial bar/rod geometry, creating a symmetrical mesh, element distortion metrics and element size.

## C.2. Rod and Bar Geometry

In the finishing stages of bar and rod rolling the input geometry is a prismatic solid cylinder or a polyhedral. The solid in reality is not prismatic, however, is assumed prismatic. The cross-sectional geometry of the stock is either round or oval. In this work the geometric bar/rod model will be approximated as completely round. In each case the cross-section of the stock is symmetrical along the plane going through the center of the stock and parallel to roll axes and symmetrical along the plane perpendicular to this plane as shown in Figure C.1. Cartesian coordinate system is used to define the axes and Z-axis is always taken as the rolling direction axis. Since the roll geometries are also symmetric, and if misalignment is neglected between the rolls and the stock, the problem can be considered to have two perpendicular planes of symmetry in the cross-section. Misalignment between the rolls and the stock can be neglected since it is very small. Therefore, to improve solution quality and to almost ensure a symmetric solution, a symmetric initial mesh will be constructed in this work.


Figure C.1. Planes of symmetry in a typical rod/bar.

## C.3. Constructing a Symmetrical Mesh in ABAQUS

The mesh is constructed using the internal mesh generator of ABAQUS. For three-dimensional (3-D) deformable solids, ABAQUS has three types of elements and they include the Hex (hexahedral), Hex-dominated (it is a mixed mesh of hexahedral and tetrahedral elements where the majority of the elements are hexahedral but there are also some tetrahedral elements for enabling the mesh to follow the exact geometry of the part more closely) and Tets (tetrahedral). If the free meshing option is used in ABAQUS/CAE then a symmetric mesh in general will not be generated for the symmetric geometry. To generate a symmetric mesh in the cross-section of the rod/bar, the ABAQUS/CAE option for defining lines/planes of symmetry is used. For generating symmetrical mesh, two perpendicular lines of symmetry on one of the cross-sectional faces must be defined. One should note that if the two symmetry planes were used, then throughout the rolling simulation the bar/rod mesh would remain symmetric along the entire length of the rod/bar cross section. A typical symmetrical mesh for the rod/bar is shown in Figure C.2.


Figure C.2. Symmetrical mesh in rod/bar.

## C.4. Element Distortion Metric Guidelines

After the mesh is generated then each element in the mesh is examined to ensure it falls within the acceptable element distortion metric guidelines. In short, the shape of an element can affect the element solution accuracy. An ideal shape provides the greatest accuracy, e.g., an ideal hexahedral is a square cube, and the more distorted the element leads to a decrease in solution accuracy. The extent of loss of accuracy due to distortion, varies with element type, mesh arrangement and physical problem. Furthermore, distortion usually degrades stresses more than displacements and temperature fields. A very good discussion on element distortion metrics can be found in Fagan [C.1].

ABAQUS/CAE provides the option for checking element quality after the mesh has been generated. The element distortion metrics in ABAQUS/CAE include aspect ratio, shape factor, maximum face corner angle and minimum face corner angle. Table C. 1 shows acceptable limits for each element distortion index recommended by ABAQUS.

Table C.1. ABAQUS guidelines for three-dimensional element distortion metrics.

| Distortion Metrics | Hexahedral | Tetrahedral | Wedge |
| :---: | :---: | :---: | :---: |
| Aspect Ratio | 3.0 | 3.0 | 3.0 |
| Shape Factor | $\mathrm{N} / \mathrm{A}$ | 0.2 | N/A |
| Minimum Face Corner Angle | $30^{\circ}$ | $20^{\circ}$ | $30^{\circ}$ |
| Maximum Face Corner Angle | $140^{\circ}$ | $120^{\circ}$ | $120^{\circ}$ |

## C.5. Element Size

The mesh size is another factor in determining the solution quality throughout the rolling simulation. Theoretically speaking, the larger is the mesh, i.e., the smaller is the individual elements, the more accurate is the solution. However, a larger size mesh requires more computational time to solve the problem. This is simply because the greater the number of nodes yields a greater number of degrees of freedom leading to more unknowns. To solve an $n \mathrm{x} n$ system of linear algebraic equations requires approximately $n$ number of divisions, $n^{3} / 3+n^{2}$ number of multiplication's and $n^{3} / 3+n$ additions [B.3] if the solution is obtained using the Gauss elimination method. Other methods for solving a matrix also need more computation for a larger matrix. Therefore, there must be a balance between accuracy and computational time.

Case studies were carried out to determine an appropriate element size that would yield very good accuracy and solve the equations in reasonable amount of time.

## Appendix D: Full Scale Mill Testing

A series of tests were conducted on one of Morgan's [D.1] RSM units installed in a rod production line in order to gather detailed dimensional data on the rolling stock for comparison with the finite element model and theoretical model in the next section. A standard size rod product of AISI 1045 carbon steel was rolled in a series of tests in which the entry temperature to the RSM, the rolling rate and the entry dimensions were all held constant. The tests consisted of rolling a billet through four stands of the RSM to obtain rod samples.

Samples of the rolled product were obtained after the rod had passed through water cooling boxes, formed into continuous loops by the laying head and cooled on the aircooling conveyor. Short samples were cut from the coils produced from each test. For dimensional measurement, the samples were placed in a custom-made system for detailed off-line dimensional measurements of rod and bar products using a laser gauge and specialized analysis software. Diameter measurements were obtained for sixty diametrical locations, giving a detailed representation of the stock geometry profile. The measurements are carried out for RSM feed section, exit of stand \#2, exit of stand \#3 and exit of stand \#4. The obtained data is shown in Table D. 1

Table D.1. Dimension measurements of stock samples from RSM Full-scale mill Testing

| Measurements at RSM feed section |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Angle | Diameter | Angle | Diameter | Angle | Diameter |
| 0 | 16.4699 | 63 | 16.3525 | 126 | 16.4428 |
| 3 | 16.4741 | 66 | 16.3782 | 129 | 16.4494 |
| 6 | 16.4707 | 69 | 16.3880 | 132 | 16.4627 |
| 9 | 16.4551 | 72 | 16.3979 | 135 | 16.4844 |
| 12 | 16.4387 | 75 | 16.4043 | 138 | 16.5055 |
| 15 | 16.4346 | 78 | 16.4117 | 141 | 16.5026 |
| 18 | 16.4246 | 81 | 16.4327 | 144 | 16.4848 |
| 21 | 16.4130 | 84 | 16.4396 | 147 | 16.4796 |
| 24 | 16.4012 | 87 | 16.4438 | 150 | 16.4785 |
| 27 | 16.3955 | 90 | 16.4689 | 153 | 16.4793 |
| 30 | 16.3764 | 93 | 16.4737 | 156 | 16.4780 |
| 33 | 16.3692 | 96 | 16.4789 | 159 | 16.4769 |
| 36 | 16.3685 | 99 | 16.4499 | 162 | 16.4737 |
| 39 | 16.3598 | 102 | 16.3899 | 165 | 16.4702 |
| 42 | 16.3527 | 105 | 16.3830 | 168 | 16.4605 |
| 45 | 16.3367 | 108 | 16.4032 | 171 | 16.4585 |
| 48 | 16.3026 | 111 | 16.4175 | 174 | 16.4611 |
| 51 | 16.2773 | 114 | 16.4277 | 177 | 16.4595 |
| 54 | 16.2495 | 117 | 16.4372 | 180 | 16.4557 |
| 57 | 16.2733 | 120 | 16.4413 |  |  |
| 60 | 16.3213 | 123 | 16.4411 |  |  |


| Measurements at Exit of Stand \#2 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Angle | Diameter | Angle | Diameter | Angle | Diameter |
| 0 | 13.4975 | 63 | 13.7204 | 126 | 13.6503 |
| 3 | 13.4806 | 66 | 13.7925 | 129 | 13.6421 |
| 6 | 13.4689 | 69 | 13.8360 | 132 | 13.6359 |
| 9 | 13.4572 | 72 | 13.8711 | 135 | 13.6283 |
| 12 | 13.4424 | 75 | 13.9057 | 138 | 13.6190 |
| 15 | 13.4295 | 78 | 13.9306 | 141 | 13.6115 |
| 18 | 13.4189 | 81 | 13.9643 | 144 | 13.6057 |
| 21 | 13.4102 | 84 | 13.9887 | 147 | 13.6017 |
| 24 | 13.4048 | 87 | 13.9971 | 150 | 13.5919 |
| 27 | 13.3941 | 90 | 14.0065 | 153 | 13.5820 |
| 30 | 13.3912 | 93 | 14.0092 | 156 | 13.5738 |
| 33 | 13.3825 | 96 | 13.9977 | 159 | 13.5584 |
| 36 | 13.3769 | 99 | 13.9677 | 162 | 13.5440 |
| 39 | 13.3702 | 102 | 13.9089 | 165 | 13.5490 |
| 42 | 13.3641 | 105 | 13.8216 | 168 | 13.5433 |
| 45 | 13.3601 | 108 | 13.7561 | 171 | 13.5225 |
| 48 | 13.3564 | 111 | 13.6966 | 174 | 13.5108 |
| 51 | 13.3726 | 114 | 13.6700 | 177 | 13.5092 |
| 54 | 13.4261 | 117 | 13.6646 | 180 | 13.4951 |
| 57 | 13.5079 | 120 | 13.6569 |  |  |
| 60 | 13.6159 | 123 | 13.6550 |  |  |
| Measurements at Exit of Stand \#3 |  |  |  |  |  |
| Angle | Diameter | Angle | Diameter | Angle | Diameter |
| 0 | 12.5497 | 63 | 12.8083 | 126 | 13.7836 |
| 3 | 12.5420 | 66 | 12.8695 | 129 | 13.7120 |
| 6 | 12.5395 | 69 | 12.9954 | 132 | 13.6209 |
| 9 | 12.5406 | 72 | 13.1725 | 135 | 13.4982 |
| 12 | 12.5368 | 75 | 13.3578 | 138 | 13.3434 |
| 15 | 12.5210 | 78 | 13.5101 | 141 | 13.1699 |
| 18 | 12.5102 | 81 | 13.6266 | 144 | 12.9973 |
| 21 | 12.5081 | 84 | 13.7107 | 147 | 12.8736 |
| 24 | 12.5175 | 87 | 13.7640 | 150 | 12.8170 |
| 27 | 12.5323 | 90 | 13.8109 | 153 | 12.7816 |
| 30 | 12.5443 | 93 | 13.8648 | 156 | 12.7468 |
| 33 | 12.5571 | 96 | 13.9132 | 159 | 12.7194 |
| 36 | 12.5731 | 99 | 13.9484 | 162 | 12.6905 |
| 39 | 12.5920 | 102 | 13.9711 | 165 | 12.6618 |
| 42 | 12.6122 | 105 | 13.9864 | 168 | 12.6313 |
| 45 | 12.6387 | 108 | 13.9882 | 171 | 12.6066 |
| 48 | 12.6623 | 111 | 13.9809 | 174 | 12.5860 |
| 51 | 12.6848 | 114 | 13.9649 | 177 | 12.5679 |
| 54 | 12.7122 | 117 | 13.9372 | 180 | 12.5526 |
| 57 | 12.7427 | 120 | 13.8956 |  |  |
| 60 | 12.7754 | 123 | 13.8426 |  |  |


| Measurements at Exit of Stand \#4 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Angle | Diameter | Angle | Diameter | Angle | Diameter |
| 0 | 12.7711 | 63 | 12.7614 | 126 | 12.8015 |
| 3 | 12.7692 | 66 | 12.7599 | 129 | 12.8048 |
| 6 | 12.7677 | 69 | 12.7570 | 132 | 12.8085 |
| 9 | 12.7685 | 72 | 12.7524 | 135 | 12.8103 |
| 12 | 12.7680 | 75 | 12.7528 | 138 | 12.8143 |
| 15 | 12.7695 | 78 | 12.7545 | 141 | 12.8151 |
| 18 | 12.7658 | 81 | 12.7578 | 144 | 12.8162 |
| 21 | 12.7628 | 84 | 12.7557 | 147 | 12.8137 |
| 24 | 12.7604 | 87 | 12.7547 | 150 | 12.8064 |
| 27 | 12.7562 | 90 | 12.7560 | 153 | 12.7938 |
| 30 | 12.7554 | 93 | 12.7711 | 156 | 12.7855 |
| 33 | 12.7564 | 96 | 12.7900 | 159 | 12.7819 |
| 36 | 12.7567 | 99 | 12.7958 | 162 | 12.7789 |
| 39 | 12.7597 | 102 | 12.7974 | 165 | 12.7776 |
| 42 | 12.7606 | 105 | 12.7963 | 168 | 12.7754 |
| 45 | 12.7592 | 108 | 12.7983 | 171 | 12.7723 |
| 48 | 12.7604 | 111 | 12.7966 | 174 | 12.7688 |
| 51 | 12.7594 | 114 | 12.7980 | 177 | 12.7709 |
| 54 | 12.7612 | 117 | 12.7943 | 180 | 12.7720 |
| 57 | 12.7616 | 120 | 12.7954 |  |  |
| 60 | 12.7634 | 123 | 12.7984 |  |  |

## Appendix E: Important Aspects of the Finite Element Model

The table below provides some details regarding the finite elements models used in Tables 5.3 and 5.12.

|  |  | Two types of solution techniques are used in solving this <br> problem. The first kind of formulation involves traditional pure <br> Lagrangian formulation where the mesh is constrained to the <br> material. The second kind of formulation combines features of <br> both pure Eulerian formulation (in which the mesh is fixed <br> spatially and the material flows through the mesh) and pure <br> Lagrangian formulation. In this case Adaptive meshing is used <br> and is referred to as the Arbitrary Lagrangian-Eulerian (ALE) <br> formulation. This approach often eliminates excessive mesh <br> distortions that are associated with a Lagrangian analysis <br> involving large deformation. Using this approach, the inlet of <br> the stock was defined with Eulerian constraints in order to <br> permit material flow; the mesh on this face was spatially <br> constrained in all directions. The material on the radial surface <br> of the stock was constrained to the mesh in the direction normal <br> to the free surface but was permitted to flow relative to the <br> mesh in the tangential direction. |
| :---: | :--- | :--- |
| Mesh Domain |  |  |


| Adaptive <br> Meshing | Adaptive meshing is often used to control excessive mesh <br> distortion, which often occurs in non-linear problems. In <br> adaptive mass scaling after a certain number of time steps the <br> entire geometry of the body is remeshed. We this method for <br> the ALE formulation only. |
| :---: | :--- | :--- |
|  | One disadvantage of using reduced integration procedure is that <br> it can admit deformation modes, which cause no straining at the <br> integration points. These zero energy modes make the element <br> rank deficient and cause a phenomenon called hourglassing <br> where, the zero energy modes starts propagating through the <br> mesh leading to inaccurate solutions. This problem is <br> particularly severe in hexahedral elements. To counter this a <br> small artificial stiffness is attached with the zero energy and is <br> associated with the zero energy deformation modes. This <br> procedure is called hourglass control. In this work, we select <br> the hourglass control as "Stiffness" was used. |


| Stock | Element Type | Three-dimensional, Deformable, Reduced Integration, Linear Hexahedral (Brick) element (C3D8R) is used in this work. There are two advantages of using Reduced integration elements. First, stresses and strains are calculated in the socalled Barlow Points [] providing optimal accuracy. Second, the computational time is less due to reduced number of integration points. |
| :---: | :---: | :---: |
|  | Material | Stock material is assumed as homogeneous and isotropic material with no porosities. |
|  | Rate <br> Dependence | The stock material is assumed to be strain rate dependent. |
|  | Plasticity Law | Three main plasticity laws are used in this work. They are Shida [E.2], Modified Shida [E.3] and Lee [E.4]. |
|  | Hardening Rate | Isotropic |
|  | \% Plastic <br> Deformation <br> Energy <br> Converted to <br> Heat | In an adiabatic analysis a portion of the energy of plastic deformation converts into heat. In this work we consider this ratio to be 0.90 . |
|  | Initial Conditions | Two initial conditions are mainly used in this work. They are 1) Initial velocity of the stock i.e. the velocity of the stock when it enters the first stand and 2) Initial temperature of the stock i.e. the temperature of the stock when it enters the first stand. |
| Roll | Material | Tungsten carbide |
|  | Finite Element Characterizati on | The rolls are considered as analytic rigid surface in this work. |
|  | Boundary Conditions | Angular velocity of rolls are used as the boundary conditions for this work |
| Stock / <br> Roll <br> Interface | Contact Condition | Contact between roll and stock is defined as a contact pair that consist of penalty contact enforcement method, balanced contact surface weighting and finite sliding formulation is used. |
|  | Friction Model | Coulomb friction model is used for this work with $\mu=0.3$ |
|  | Heat Transfer Effects | Heat transfer effects are not considered |
| Stand | Material | Stand is considered as a rigid pin support |

## Appendix F: Additional Finite Element Analyses

## F.1. Results of Finite Element Solution for the RSM Case (Section 5.2)

In this section detailed results of the finite element model solved by different formulation types, constitutive models for plastic behavior and different mesh sizes are presented. Tables F. 1 through F. 7 summarizes the finite element, theoretical and fullscale mill testing results for spread, cross-sectional area, percentage reduction in area, incremental plastic strain, total plastic strain and roll force at all four finishing stands. Overall it can be observed from finite element solutions obtained using Lagrangian formulation yields marginally better results than finite element solutions obtained using Arbitrary Lagrangian-Eulerian (ALE) formulation. It is also observed that effect of using different constitutive models on geometric and deformation parameters is practically nonexistent. Therefore it can be concluded that stock deformation in finishing rolling stage doesn't depend on constitutive laws. But it is observed that the It is also observed that effect of using different constitutive models on roll force is significant and cannot be neglected. It was observed that the roll force obtained by the finite element solution using Modified Shida [F.1] constitutive law is most consistent with a proprietary Morgan [F.5] technique for calculating roll force. The proprietary model employs a combination of empirical techniques and experimental validation.

Table F.1. Results for Republic Engineered Products RSM mill using Lagrangian formulation, Modified Shida [F.1] constitutive law and coarse mesh.

| Characteristics of Finite Element Model | Formulation Type |  |  | Lagrangian |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | Modified Shida [F.1] |
|  | Number of Nodes |  |  | 1300 |
|  | Number of Elements |  |  | 1782 |
|  | Number of Degrees of Freedom (Including Lagrange multipliers) |  |  | 5394 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 18.90 \\ (-3.4 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 13.29 \\ (-5.1 \% \mathrm{~T}) \\ (-2.2 \% \mathrm{FST}) \\ \hline \end{gathered}$ | 14.78 $(5.7 \% \mathrm{~T})$ $(5.4 \% \mathrm{FST})$ | 12.99 $(1.2 \% \mathrm{~T})$ $(1.3 \% \mathrm{FST})$ |
| Theoretical Lee [5.3] | 19.57 | 13.70 | 13.98 | 12.84 |
| Full-scale Mill Testing | - | 14.01 | 14.02 | 12.82 |
| Cross-sectional Area (mm ${ }^{\text {2 }}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 158.68 \\ (-8.0 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 139.47 \\ (-4.9 \% \mathrm{~T}) \\ (-4.2 \% \mathrm{FST}) \end{gathered}$ | $\begin{gathered} 132.08 \\ (-2.83 \% \mathrm{~T}) \\ (-1.9 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 124.98 \\ (-4.3 \% \mathrm{~T}) \\ (-2.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 172.50 | 146.60 | 135.94 | 130.59 |
| Full-scale Mill Testing | - | 145.66 | 134.66 | 128.15 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 24.36 \\ (33.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 13.77 \\ (-8.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 5.60 \\ (-23.0 \% \mathrm{~T}) \\ (-28.4 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 5.67 \\ (44.2 \% \mathrm{~T}) \\ (-11.6 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 18.28 | 15.02 | 7.27 | 3.94 |
| Full-scale Mill Testing | - | - | 8.39 | 4.83 |
| Incremental Plastic Strain ${ }^{1}$ (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.382 \\ (0.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.280 \\ (-15.2 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.077 \\ (-27.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.09 \\ (12.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] | 0.380 | 0.33 | 0.107 | 0.08 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.382 \\ (0.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.677 \\ (-4.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.826 \\ (1.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.901 \\ (3.7 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.380 | 0.710 | 0.814 | 0.869 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 120.9 \\ (-37 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 76.4 \\ (-51 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 37.5 \\ (-17 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 50.4 \\ (97 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 191.9 | 156 | 46 | 26 |

T-\% Difference with theoretical method.
FST - \% Difference with full-scale mill testing data.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

Table F.2. Results for Republic Engineered Products RSM mill using Lagrangian formulation, Modified Shida [F.1] constitutive law and medium mesh.

| Characteristics of Finite Element Model | Formulation Type |  |  | Lagrangian |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | Modified Shida [F.1] |
|  | Number of Nodes |  |  | 7800 |
|  | Number of Elements |  |  | 9563 |
|  | Number of Degrees of Freedom (Including Lagrange multipliers) |  |  | 27737 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 19.13 \\ (-2.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 13.76 \\ (0.5 \% \mathrm{~T}) \\ (-1.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 14.71 \\ (4.9 \% \mathrm{~T}) \\ (5.3 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 12.94 \\ (0.8 \% \mathrm{~T}) \\ (0.9 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 19.57 | 13.70 | 13.98 | 12.84 |
| Full-scale Mill Testing | - | 14.01 | 14.02 | 12.82 |
| Cross-sectional Area (mm ${ }^{\text {2 }}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 166.84 \\ (-3.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 145.74 \\ (-0.6 \% \mathrm{~T}) \\ (1.8 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 134.88 \\ (-0.8 \% \mathrm{~T}) \\ (2.0 \% \mathrm{FST}) \\ \hline 1020 \end{gathered}$ | $\begin{gathered} 128.53 \\ (-1.6 \% \mathrm{~T}) \\ (0.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 172.50 | 146.60 | 135.94 | 130.59 |
| Full-scale Mill Testing | - | 145.66 | 134.66 | 128.15 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 22.6 \\ (23.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 14.47 \\ (-3.6 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 8.05 \\ (10.7 \% \mathrm{~T}) \\ (-4.05 \% \mathrm{FST}) \end{gathered}$ | $\begin{gathered} 4.94 \\ (25.6 \% \mathrm{~T}) \\ (-2.2 \% \mathrm{FST}) \end{gathered}$ |
| Theoretical Lee [5.3] | 18.28 | 15.02 | 7.27 | 3.94 |
| Full-scale Mill Testing | - | - | 8.39 | 4.83 |
| Incremental Plastic Strain ${ }^{1}$ (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.388 \\ (2.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.320 \\ (-3.0 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.112 \\ (5.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.0875 \\ (9.3 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] | 0.380 | 0.33 | 0.107 | 0.08 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.388 \\ (2.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.740 \\ (4.25 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.903 \\ (11.0 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.974 \\ (12.1 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.380 | 0.710 | 0.814 | 0.869 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 112.3 \\ (-41.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 80.3 \\ (-48.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 50.4 \\ (11.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 36.6 \\ (44 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 191.9 | 156 | 46 | 26 |

T-\% Difference with theoretical method.
FST - \% Difference with full-scale mill testing data.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

Table F.3. Results for Republic Engineered Products RSM mill using Lagrangian formulation, Shida [F.2] constitutive law and coarse mesh.

| Characteristics of Finite Element Model | Formulation Type |  |  | Lagrangian |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | Shida [F.2] |
|  | Number of Nodes |  |  | 1300 |
|  | Number of Elements Freedom in the problem |  |  | 1782 |
|  | Number of Degrees of Freedom (Including Lagrange multipliers) |  |  | 5394 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 18.88 \\ (-3.4 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 13.29 \\ (-5.1 \% \mathrm{~T}) \\ (-2.2 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 14.75 \\ (5.7 \% \mathrm{~T}) \\ (5.4 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 12.99 \\ (1.2 \% \mathrm{~T}) \\ (1.3 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 19.57 | 13.70 | 13.98 | 12.84 |
| Full-scale Mill Testing | - | 14.01 | 14.02 | 12.82 |
| Cross-sectional Area (mm ${ }^{\text {2 }}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 158.6 \\ (-8.1 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 139.47 \\ (-4.9 \% \mathrm{~T}) \\ (-4.2 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 131.9 \\ (-2.9 \% \mathrm{~T}) \\ (-2.0 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 124.91 \\ (-4.3 \% \mathrm{~T}) \\ (-2.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 172.50 | 146.60 | 135.94 | 130.59 |
| Full-scale Mill Testing | - | 145.66 | 134.66 | 128.15 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 24.41 \\ (33.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 13.79 \\ (-8.1 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 5.66 \\ (-22.2 \% \mathrm{~T}) \\ (-28.4 \% \mathrm{FST}) \end{gathered}$ | $\begin{gathered} 5.59 \\ (42 \% \mathrm{~T}) \\ (-11.6 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 18.28 | 15.02 | 7.27 | 3.94 |
| Full-scale Mill Testing | - | - | 8.39 | 4.83 |
| Incremental Plastic Strain ${ }^{1}$ (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.381 \\ (0.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.277 \\ (-18.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.126 \\ (16.7 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.118 \\ (47 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] | 0.380 | 0.33 | 0.107 | 0.08 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.381 \\ (0.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.677 \\ (-4.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 0.826 \\ (1.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.898 \\ (3.7 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.380 | 0.710 | 0.814 | 0.869 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 113 \\ (-40.9 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 70.9 \\ (-54.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 37.2 \\ (-18.8 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 40.4 \\ (58.8 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 191.9 | 156 | 46 | 26 |

T-\% Difference with theoretical method.
FST - \% Difference with full-scale mill testing data.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

Table F.4. Results for Republic Engineered Products RSM mill using Lagrangian formulation, Shida [F.2] constitutive law and medium mesh.

| Characteristics of Finite Element Model | Formulation Type |  |  | Lagrangian |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | Shida [F.2] |
|  | Number of Nodes |  |  | 7800 |
|  | Number of Elements |  |  | 9563 |
|  | Number of Degrees of Freedom (Including Lagrange multipliers) |  |  | 27737 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 19.09 \\ (-2.4 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 13.77 \\ (0.5 \% \mathrm{~T}) \\ (-1.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 14.69 \\ (4.8 \% \mathrm{~T}) \\ (5.3 \% \mathrm{FST}) \end{gathered}$ | $\begin{gathered} \hline 12.96 \\ (0.9 \% \mathrm{~T}) \\ (1.1 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 19.57 | 13.70 | 13.98 | 12.84 |
| Full-scale Mill Testing | - | 14.01 | 14.02 | 12.82 |
| Cross-sectional Area (mm ${ }^{\text {2 }}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 166.82 \\ (-3.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 145.73 \\ (-0.6 \% \mathrm{~T}) \\ (1.8 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 134.77 \\ (-0.9 \% \mathrm{~T}) \\ (0.9 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 128.50 \\ (-1.6 \% \mathrm{~T}) \\ (0.3 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 172.50 | 146.60 | 135.94 | 130.59 |
| Full-scale Mill Testing | - | 145.66 | 134.66 | 128.15 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 22.6 \\ (23.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 14.46 \\ (-3.6 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 8.12 \\ (11.8 \% \mathrm{~T}) \\ (-4 \% \mathrm{FST}) \end{gathered}$ | 4.88 $(26.3 \% \mathrm{~T})$ $(-1 \% \mathrm{FST})$ |
| Theoretical Lee [5.3] | 18.28 | 15.02 | 7.27 | 3.94 |
| Full-scale Mill Testing | - | - | 8.39 | 4.83 |
| Incremental Plastic Strain ${ }^{1}$ (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.388 \\ (2.4 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.320 \\ (-3.0 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.112 \\ (5.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{aligned} & \hline 0.0871 \\ & (9 \% \mathrm{~T}) \end{aligned}$ |
| Theoretical Lee [5.1] | 0.380 | 0.33 | 0.107 | 0.08 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.388 \\ (2.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.738 \\ (4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.898 \\ (10.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.971 \\ (11.7 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.380 | 0.710 | 0.814 | 0.869 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 108.4 \\ (-43 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 74.8 \\ (-52 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 50.9 \\ (11.6 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 32.1 \\ (26.3 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 191.9 | 156 | 46 | 26 |

T-\% Difference with theoretical method.
FST - \% Difference with full-scale mill testing data.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

Table F.5. Results for Republic Engineered Products RSM mill using Lagrangian formulation, Shida [F.2] constitutive law and fine mesh.

| Characteristics of Finite Element Model | Formulation Type |  |  | Lagrangian |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | Shida [F.2] |
|  | Number of Nodes |  |  | 42820 |
|  | Number of Elements Freedom in the problem |  |  | 49994 |
|  | Number of Degrees of Freedom (Including Lagrange multipliers) |  |  | 147030 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 19.10 \\ (-2.4 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 13.57 \\ (-0.9 \% \mathrm{~T}) \\ (-1.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 14.43 \\ (2.98 \% \mathrm{~T}) \\ (2.8 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 12.83 \\ (-0.1 \% \mathrm{~T}) \\ (0.1 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 19.57 | 13.70 | 13.98 | 12.84 |
| Full-scale Mill Testing | - | 14.01 | 14.02 | 12.82 |
| Cross-sectional Area (mm ${ }^{\text {2 }}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 167.65 \\ (-2.8 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 145.67 \\ (0.01 \% \mathrm{~T}) \\ (-0.6 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 134.83 \\ (-0.8 \% \mathrm{~T}) \\ (0.1 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 128.83 \\ (-1.3 \% \mathrm{~T}) \\ (0.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 172.50 | 146.60 | 135.94 | 130.59 |
| Full-scale Mill Testing | - | 145.66 | 134.66 | 128.15 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 22.95 \\ (25.6 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 15.09 \\ (0.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 8.03 \\ (10.4 \% \mathrm{~T}) \\ (-4.3 \% \mathrm{FST}) \\ \hline \end{gathered}$ | 4.66 $(18.4 \% \mathrm{~T})$ $(-3.5 \% \mathrm{FST})$ |
| Theoretical Lee [5.3] | 18.28 | 15.02 | 7.27 | 3.94 |
| Full-scale Mill Testing | - | - | 8.39 | 4.83 |
| Incremental Plastic Strain ${ }^{1}$ (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.399 \\ (5.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.379 \\ (+15.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 0.107 \\ (0.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.08 \\ (0.2 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] | 0.380 | 0.33 | 0.107 | 0.08 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.399 \\ (5.2 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.763 \\ (7.51 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.902 \\ (10.9 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.981 \\ (13 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.380 | 0.710 | 0.814 | 0.869 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 108.9 \\ (-43.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 79.7 \\ (-48.9 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 47.2 \\ (3.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 29.7 \\ (16.8 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 191.9 | 156 | 46 | 26 |

T-\% Difference with theoretical method.
FST - \% Difference with full-scale mill testing data.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

Table F.6. Results for Republic Engineered Products RSM mill using ALE formulation, Modified Shida [F.1] constitutive law and fine mesh.


T-\% Difference with theoretical method.
FST - \% Difference with full-scale mill testing data.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

Table F.7. Results for Republic Engineered Products RSM mill using ALE formulation, Shida [F.2] constitutive law and fine mesh.

| Characteristics of Finite Element Model | Formulation Type |  |  | ALE |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | hida [F.2] |
|  | Number of Nodes |  |  | 42820 |
|  | Number of Elements Freedom in the problem |  |  | 49994 |
|  | Number of Degrees of Freedom (Including Lagrange multipliers) |  |  | 147030 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 19.10 \\ (-2.4 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 13.57 \\ (-0.9 \% \mathrm{~T}) \\ (-1.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 14.43 \\ (2.98 \% \mathrm{~T}) \\ (2.8 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 12.83 \\ (-0.1 \% \mathrm{~T}) \\ (0.1 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 19.57 | 13.70 | 13.98 | 12.84 |
| Full-scale Mill Testing | - | 14.01 | 14.02 | 12.82 |
| Cross-sectional Area (mm ${ }^{2}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 167.65 \\ (-2.8 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 145.67 \\ (0.01 \% \mathrm{~T}) \\ (-0.6 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 134.83 \\ (-0.8 \% \mathrm{~T}) \\ (0.1 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 128.83 \\ (-1.3 \% \mathrm{~T}) \\ (0.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 172.50 | 146.60 | 135.94 | 130.59 |
| Full-scale Mill Testing | - | 145.66 | 134.66 | 128.15 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 22.95 \\ (25.6 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 15.09 \\ (0.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 8.03 \\ (10.4 \% \mathrm{~T}) \\ (-4.3 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 4.66 \\ (18.4 \% \mathrm{~T}) \\ (-3.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 18.28 | 15.02 | 7.27 | 3.94 |
| Full-scale Mill Testing | - | - | 8.39 | 4.83 |
| Incremental Plastic Strain1 (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.399 \\ (5.2 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.279 \\ (-15.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.107 \\ (0.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.08 \\ (0.2 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] | 0.380 | 0.33 | 0.107 | 0.08 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.399 \\ (5.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.763 \\ (7.51 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.902 \\ (10.9 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.981 \\ (13 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.380 | 0.710 | 0.814 | 0.869 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 108.9 \\ (-43.2 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 79.7 \\ (-48.9 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 47.2 \\ (3.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 29.7 \\ (16.8 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 191.9 | 156 | 46 | 26 |

T-\% Difference with theoretical method.
FST - \% Difference with full-scale mill testing data.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

## F.2. Results of Finite Element solution for the POSCO case (Section 5.3)

In this section detailed results of the finite element model solved by different formulation types, different constitutive model for plastic behavior and different mesh sizes are presented tables F. 8 to F.10. Tables F. 8 to F. 10 summarizes the finite element and theoretical for spread, cross-sectional area, percentage reduction in area, incremental plastic strain, total plastic strain and roll force at all four finishing stands. Overall it can be observed from finite element solutions obtained using Lagrangian formulation yields marginally better results than finite element solutions obtained using Arbitrary Lagrangian-Eulerian (ALE) formulation. It is also observed that effect of using different constitutive models on geometric and deformation parameters is practically non-existent. Therefore it can be concluded that stock deformation in finishing rolling stage doesn't depend on constitutive laws. But it is observed that the It is also observed that effect of using different constitutive models on roll force is significant and cannot be neglected. It was observed that the roll force obtained by the finite element solution using Modified Shida [F.1] constitutive law is most consistent with a proprietary Morgan [F.5] technique for calculating roll force. The proprietary model employs a combination of empirical techniques and experimental validation.

Table F.8. Results for POSCO No. 3 mill using Lagrangian formulation, Suzuki [F.3] constitutive law and medium mesh.

| Characteristics of Finite Element Model | Formulation Type |  |  | Lagrangian |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | Suzuki [F.3] |
|  | Number of Nodes |  |  | 3456 |
|  | Number of Elements Freedom in the problem |  |  | 4753 |
|  | Number of Degrees of Freedom <br> (Including Lagrange multipliers) |  |  | 14307 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 183.40 \\ (-2.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 196.47 \\ (7.7 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 114.69 \\ (-2.8 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 142.62 \\ (-6.1 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.3] | 187.65 | 182.46 | 118.01 | 151.80 |
| Cross-sectional Area (mm ${ }^{\text {2 }}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{aligned} & 20451.25 \\ & (-1.8 \% \mathrm{~T}) \end{aligned}$ | $\begin{gathered} 14547.11 \\ (2.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{aligned} & 10825.74 \\ & (-2.4 \% \mathrm{~T}) \end{aligned}$ | $\begin{gathered} \hline 8119.21 \\ (-2.4 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.3] | 20828.64 | 14237.84 | 11092.66 | 8320.964 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 27.42 \\ (32.9 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 40.60 \\ (28.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 34.37 \\ (55.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 33.33 \\ (33.3 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.3] | 20.63 | 31.64 | 22.09 | 24.99 |
| Incremental Plastic Strain1 (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.41 \\ (7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.74 \\ (-9 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 0.51 \\ (1.7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.47 \\ (-13.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] | 0.381 | 0.808 | 0.499 | 0.540 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.41 \\ (7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 1.25 \\ (5.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 1.80 \\ (6.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 2.12 \\ (-4.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.381 | 1.186 | 1.685 | 2.22 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 2403.12 \\ (-29.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 2670.69 \\ (-34.4 \% \mathrm{~T}) \end{gathered}$ | $\begin{array}{r} 1998.42 \\ (-37.4 \% \mathrm{~T} \end{array}$ | $\begin{gathered} 1684.73 \\ (-47.1 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 3394 | 4069 | 3196 | 3182 |

T-\% Difference with theoretical method.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

Table F.9. Results for POSCO No. 3 mill using Lagrangian formulation, Shida [F.2] constitutive law and medium mesh.

| Characteristics of Finite Element Model | Formulation Type |  |  | ALE |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | uzuki [F.2] |
|  | Number of Nodes |  |  | 3456 |
|  | Number of Elements Freedom in the problem |  |  | 4753 |
|  | Number of Degrees of Freedom (Including Lagrange multipliers) |  |  | 14307 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 183.40 \\ (-2.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 196.47 \\ (7.7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 114.69 \\ (-2.8 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 142.62 \\ (-6.1 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.3] | 187.65 | 182.46 | 118.01 | 151.80 |
| Cross-sectional Area (mm ${ }^{\text {2 }}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{aligned} & 20451.25 \\ & (-1.8 \% \mathrm{~T}) \end{aligned}$ | $\begin{gathered} 14547.11 \\ (2.2 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{aligned} & 10825.74 \\ & (-2.4 \% \mathrm{~T}) \end{aligned}$ | $\begin{gathered} \hline 8119.21 \\ (-2.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 20828.64 | 14237.84 | 11092.66 | 8320.964 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 27.42 \\ (32.9 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 40.60 \\ (28.3 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 34.37 \\ (55.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 33.33 \\ (33.3 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 20.63 | 31.64 | 22.09 | 24.99 |
| Incremental Plastic Strain1 (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.41 \\ (7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.74 \\ (-9 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.51 \\ (1.7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.47 \\ (-13.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] | 0.381 | 0.808 | 0.499 | 0.540 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.41 \\ (7 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 1.25 \\ (5.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 1.80 \\ (6.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 2.12 \\ (-4.5 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.381 | 1.186 | 1.685 | 2.22 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 2398.33 \\ (-29.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 2664.69 \\ (-34.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 1995.42 \\ (-37.5 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 1678.73 \\ (-47.3 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 3394 | 4069 | 3196 | 3182 |

T-\% Difference with theoretical method.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

Table F.10. Results for POSCO No. 3 mill using ALE formulation, Suzuki [F.3] constitutive law and medium mesh.

| Characteristics of Finite Element Model | Formulation Type |  |  | ALE |
| :---: | :---: | :---: | :---: | :---: |
|  | Constitutive Law |  |  | uzuki [F.3] |
|  | Number of Nodes |  |  | 3456 |
|  | Number of Elements Freedom in the problem |  |  | 4753 |
|  | Number of Degrees of Freedom (Including Lagrange multipliers) |  |  | 14307 |
| Spread (mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 183.40 \\ (-2.3 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} \hline 196.47 \\ (7.7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 114.69 \\ (-2.8 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 142.62 \\ (-6.1 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 187.65 | 182.46 | 118.01 | 151.80 |
| Cross-sectional Area (mm ${ }^{\text {2 }}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{aligned} & 20451.25 \\ & (-1.8 \% \mathrm{~T}) \end{aligned}$ | $\begin{gathered} 14547.11 \\ (2.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{aligned} & 10825.74 \\ & (-2.4 \% \mathrm{~T}) \end{aligned}$ | $\begin{gathered} \hline 8119.21 \\ (-2.4 \% \mathrm{~T}) \\ \hline \end{gathered}$ |
| Theoretical Lee [5.3] | 20828.64 | 14237.84 | 11092.66 | 8320.964 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 27.42 \\ (32.9 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 40.60 \\ (28.3 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 34.37 \\ (55.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 33.33 \\ (33.3 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.3] | 20.63 | 31.64 | 22.09 | 24.99 |
| Incremental Plastic Strain1 (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} \hline 0.41 \\ (7 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 0.74 \\ (-9 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.51 \\ (1.7 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.47 \\ (-13.5 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] | 0.381 | 0.808 | 0.499 | 0.540 |
| Total Plastic Strain (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.41 \\ (7 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} \hline 1.25 \\ (5.4 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 1.80 \\ (6.6 \% \mathrm{~T}) \\ \hline \end{gathered}$ | $\begin{gathered} 2.12 \\ (-4.5 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{2}$ | 0.381 | 1.186 | 1.685 | 2.22 |
| Roll Force (kN) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 2406.03 \\ (-29.1 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 2673.21 \\ (-34.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 2003.48 \\ (-37.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 1692.73 \\ (-46.8 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [5.1] ${ }^{3}$ | 3394 | 4069 | 3196 | 3182 |

T - \% Difference with theoretical method.
${ }^{1}$ All Strains are measured at exit of each Stand.
${ }^{2}$ The theoretical strains are calculated by maximum width method [5.1]
${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

## Appendix G: Mesh Convergence Study

## G.1. Convergence Study for Spread and Area for Last Pass of Republic Engineering Products, Lorain, OH RSM Mill

A convergence study is carried out for the last stand of Republic Engineered Products, Lorain, OH RSM Mill for spread and cross-sectional area. Figure G. 1 shows the $\%$ error between finite element and full-scale mill testing results for three different meshes. The $\%$ error data is plotted with number of degrees of freedom for each mesh. From figure G.1a it can be concluded that $\%$ error for spread decreases with increase in number of degrees of freedom for both Modified Shida [G.3] and Shida [G.4] constitutive laws. From figure G.1b it can be concluded that \% error for cross-sectional area decreases with increase in number of degrees of freedom for both Modified Shida [G.3] and Shida [G.4] constitutive laws. It can also be concluded that for the finest finite element mesh considered in this study all errors are well below $1 \%$. Figure G. 2 shows the ASTM [] tolerance and roundness of Finite Element result for each mesh. From figure G.2a it can be concluded that finite element solution for roundness improves with increase in number of degrees of freedom for both Modified Shida [G.3] and Shida [G.4] constitutive laws. From figure G. 2 b it can be concluded that finite element solution for tolerance improves with increase in number of degrees of freedom for both Modified Shida [G.3] and Shida [G.4] constitutive laws. It can also be concluded that for the finest finite element mesh considered in this study the finite element solution actually satisfies ASTM [] standard for roundness and tolerance for 12.75 mm bar.


Figure G.1. \% Error of Finite Element Results with Full-scale Mill Testing at Last Stand of Republic Engineered Products, RSM Mill for 3 different meshes.


Figure G.2. Tolerance and Roundness of Finite Element Results at Last Stand of Republic Engineered Products, RSM Mill for three different meshes.

## Appendix H: A New Approach for Theoretical Calculation of Stock Surface Profile in Multi-Stand Rolling

## H.1. Overview

Theoretical calculation of surface profile is extremely important for accurately calculating of cross-sectional area, plastic strain and percentage reduction of stock in a multi-stand rolling process. Lee et al. [G.1] in 2000 proposed a model to calculate surface profile that is only valid for round-oval and oval-round passes. However, the model cannot be applied to two cases considered in this study. In these situations a commonly followed practice in industry is to assume the free surface as a straight line. In a large number of cases this assumption is also not accurate. In this chapter a more general approach to calculate stock surface profile is proposed.

## H.2. Proposed Approach



Figure H.1. Roll Groove surface and Stock Side Free Surface
In proposed approach the spread (w) is first calculated based on the method by Shinokura and Takai [G.2]. Then it is assumed that the rigid roll groove surface is represented by a curve $x=f(y)$ that is known. The side free surface is represented by the function $x=g(y)$. The problem is assumed symmetric around X - and Y -axis and is therefore solved only for the first quadrant. Let $\mathrm{Q}\left(\mathrm{x}_{1}, \mathrm{y}_{1}\right)$ be the point where the roll groove surface $(x=f(y))$ intersects the stock side free surface $(x=g(y))$ and $\mathrm{P}(\mathrm{w} / 2,0)$ is the point of maximum width. The following assumptions are made regarding the free surface: -

1. The tangent to the free surface at point P is vertical, i.e., $\left.\frac{d g}{d y}\right|_{P\left(\frac{w}{2}, 0\right)}=0$
2. The tangent to the free surface at point Q is collinear to tangent of the roll groove surface at point Q i.e. $\left.\frac{d f}{d y}\right|_{Q\left(x_{1}, y_{1}\right)}=\left.\frac{d g}{d y}\right|_{Q\left(x_{1}, y_{1}\right)}$
3. The free surface is approximated as a complete quadratic polynomial as follows $x=g(y)=A y^{2}+B y+C$, where $\mathrm{A}, \mathrm{B}$ and C are constants to be determined

Since point P is on the side free surface, it satisfies the equation $x=g(y)=A y^{2}+B y+C$
$\frac{w}{2}=0+0+C$
yield, $C=\frac{w}{2}$
From assumptions 1 and 3,
$2 A y+B=\left.0\right|_{P(w / 2,0)}$
yield, $B=0$
From assumptions 2 and 3, Equation G.1a and G.1b,
$2 A y_{1}=f^{\prime}\left(y_{1}\right)$
Since Q satisfies both $f(y)$ and $g(y)$,
$A y_{1}{ }^{2}+\frac{w}{2}=f\left(y_{1}\right)$

Since $f(y)$ is a known function, unknowns $A$ and $y_{1}$ can be solved from Equations G.1c $\&$ G.1d. Then the free surface curve can be written as $x=g(y)=A y^{2}+\frac{w}{2}$, where $A$ is a known constant.

## H.3. Advantages and Disadvantages

The advantage of above-mentioned method is that theoretically it can be applied for any roll groove surface type. But the main drawback of this approach is it gives erroneous results for flat grooves since because in practice Assumption 2 is invalid for flat grooves. Further investigation is needed before this method can be applied universally for all stand sequence. Meanwhile this approach yields gives very accurate results for curved roll groove types that are commonly found.

## Appendix I: Conference Paper

This Paper Appear in the Following Conference:

1. Biswas, S., Rencis, J.J., Gutierrez, H. and Kiefer, B.V., User-oriented Threedimensional Finite Element Modeling of High Speed Bar and Rod Rolling,To appear in the $45^{\text {th }}$ Iron \& Steel Society Mechanical Working and Steel Processing Conference, Chicago, IL, November 9-12, 2003.

# User-Oriented Three-Dimensional Finite Element Modeling of High Speed Bar and Rod Rolling 

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Keywords: Bar and Rod Rolling, Finite Element Analysis, Free Surface, High Speed Rolling, Hot Rolling, Product Geometry, Rolling Simulation


#### Abstract

A Java pre- and post-processing graphical user-oriented interface has been developed by the authors to aid a mill engineer with little or no finite element experience throughout the analysis process of the finishing rolling stands. A case study is presented that uses the commercial finite element code ABAQUS/Explicit to predict roundness and tolerance customer requirements. Other parameters that are determined include spread, crosssectional area, percentage reduction in area, incremental plastic strain, total plastic strain and roll force. All parameters are compared to theoretical models and some are compared to full-scale mill testing.


## Introduction to Case Study

In this study a finite element model of the finishing rolling stands at a Morgan rolling mill is considered to produce a finished rod of AISI 1045 medium carbon steel with a 12.75 mm diameter. The customer (rod user) is a U.S. automotive supplier who will manufacturer M12 x $1.25,4 \mathrm{~g}$ (high accuracy, fine fits) steel bolt of SAE class 4.6 from the finished rod. The goal of the simulation is to produce a finished rod that will satisfy the automotive supplier requirements for roundness and tolerance in accordance to ASTM standards.

The details of the finishing rolling stands and incoming stock for the case study are first discussed. An overview of the user-oriented Java program developed by the authors for carrying out the ABAQUS finite element analysis by a mill engineer is then presented. Subsequent sections discuss the finite element model and how full-scale mill testing was carried out. The finite element results are then compared to theoretical and full-scale mill testing. The final section compares the finite element results, theoretical results and fullscale mill testing results with customer requirements.

## Details of Finishing Rolling Stands and Incoming Stock

The specifications of the finishing rolling stands and the incoming stock are defined in Table I. The geometric details regarding the finishing rolling stands were provided by Morgan. There are four finishing stands with a pass sequence of oval-round-roundround in the reducing/sizing (RSM) mill. Stand \#1 consists of two oval grooved rolls and input stock is of circular cross-section. Stand \#2 consists of two round grooved rolls oriented at $90^{\circ}$ to the first stand and the output of Stand \#1 is used as input stock for this stand. Stand \#3 consists of two round grooved rolls oriented $90^{\circ}$ to Stand \#2 and the output of Stand \#2 is used as input stock for this stand. Stand \#4 consists of two round grooved rolls oriented $90^{\circ}$ to Stand \#3 and the output of Stand \#3 is used as input stock for this stand.

Table I. Details of finishing rolling stands and incoming stock

| Finishing Rolling Stands |  | INCOMING STOCK |  |
| :---: | :---: | :---: | :---: |
| Pass Sequence | Oval-round-round-round | Translational Speed | $19 \mathrm{~m} / \mathrm{s}$ |
| Stand Spacing (On-center) | Stands 1-2: 820 mm ; Stands 2-3: 966 mm ; Stands 3-4: 150 mm | Cross Section Profile | 16.395 mm Diameter |
|  |  | Section Length | The stock is continuously fed into the stands. |
| Roll Diameters | Stand \#1: 211.09 mm ; <br> Stand \#2: 211.09 mm ; <br> Stand \#3: 145.13 mm ; <br> Stand \#4: 145.14 mm | Material | AISI 1045 <br> Medium Carbon Steel |
| Roll Gaps | Stand \#1: 1.2 mm ; Stand \#2: 1.36 mm ; Stand \#3: 1.32 mm ; Stand \#4: 1.4 mm | Chemical Composition | $\begin{gathered} \text { C-0.45, Mn-0.75, } \\ \text { P-0.04, S-0.05 (wt. \%) } \end{gathered}$ |
| Roll Groove Geometries | Defined by Morgan [1] | Austenite Grain Size | Not Applicable |
| Roll Material | Tungsten Carbide | Temperature | Uniform at $910{ }^{\circ} \mathrm{C}$ |
| No-twist Rolling | Stands are Alternatively Oriented $90^{\circ}$ from Each Other |  |  |
| Roll Temperatures | Not Applicable | Strain Rate Range | $350-500 \mathrm{~s}^{-1}$ |
| Rotational Speed of Rolls | Defined by Morgan [1] | Specific Heat | $475 \mathrm{~J} / \mathrm{Kg} / \mathrm{K}$ [2] |
| Roll/Stock Friction | Friction due to contact between tungsten carbide roll and AISI 1045 stock surface with water present between as coolant. |  |  |

## Java Pre- and Post-processing Graphical User Interface

A Java pre- and post-processing graphical user interface (GUI) was developed by the authors so that a mill engineer can define a finite element model of the mill setup. The long range goal is that the Java interface could be used by a mill engineer with little or no finite element experience. Using the analysis results the engineer can determine whether or not the mill setup satisfies customer requirements. The major reason why the Java language was selected is that it is platform independent; therefore, code does not have to be recompiled. The GUI was developed using the Java ${ }^{\text {TM }} 2$ Platform Standard Edition
[3]. The mill engineer uses the Java pre-processor program to define the finishing rolling stand and incoming stock. The groove geometry module of the Java pre-processor is shown in Figure 1. The mill engineer can input groove geometry data, stock geometry data, stock material property data, element and mesh information, boundary and initial conditions, stock/roll friction, temperature related data, etc. Once the stands and stock are defined, the pre-processor creates a Python script file. Through the ABAQUS/CAE interface the Python script file is used to automatically generate an input file (preprocessing stage) of the finite element model. The finite element model is then solved using the ABAQUS solver (processing stage). Once the finite element solution is complete, a Python script post-processor code is run from the ABAQUS/CAE command line to generate ASCII result files from the ABAQUS output database (In the future the plan is to integrate this process into the Java program so that the mill engineer does not have to carry it out manually.). The Java post-processor then reads the ASCII files and calculates geometric and deformation parameters that can be used to evaluate whether or not customer requirements are satisfied. An in-depth discussion of the Java pre- and post-processing program can be found in Souvik [4]. The mill engineer can also view the finite element results in ABAQUS/CAE or ABAQUS/Viewer.


Figure 1: Screen layout of the groove geometry module in the Java pre-processing program.

## Finite Element Model

The commercial finite element code ABAQUS/Explicit [5] version 6.3 was used in this work. Table II states the assumptions, solution techniques and other modeling parameters used in the finite element simulation of the four-stand reducing/sizing mill. The actual rolling stand configuration is shown in Figure 2 and the finite element model considered all four stands as shown in Figure 3. The three-dimensional hexahedral brick finite element model was considered transient using explicit time integration and is based on a Lagrangian formulation. A convergence study was carried out to determine the appropriate mesh size as discussed in Souvik [4]. The constitutive equation for
determining the flow stress of steel for different strain rates and temperature employed Lee [6] since the strain rate range in this work is $350-500 \mathrm{~s}^{-1}$ (Table I). Lee's constitutive equation is valid for strain rate range of $1 \mathrm{~s}^{-1}$ to $3000 \mathrm{~s}^{-1}$ and is a modification of Shida [7] that has a strain range of $1 \mathrm{~s}^{-1}$ to $100 \mathrm{~s}^{-1}$. An in-depth review of the state-of-the-art for various experimental studies and empirical constitutive equations to predict flow stress behavior of steel at high temperature and strain rates can be found in Souvik [4].

Table II. Details of ABAQUS/Explicit finite element model for the incoming stock and rolling stands

| FORMULATION | Mesh Domain | Lagrangian |
| :---: | :---: | :---: |
|  | Time Dependence | Transient |
|  | Time Integration | Explicit, Dynamics, Adiabatic. Optimal time step is decided automatically by ABAQUS |
|  | Dimensionality | Three-Dimensional |
|  | Mass Scaling | None |
|  | Adaptive Meshing | Lagrangian Analysis: No |
|  | Hourglass | Artificial Stiffness |
| Roll | Material | Rigid |
|  | Finite Element Characterization | Analytic Rigid Surface |
|  | Boundary Conditions | Rotational Speed of Rolls (see Table I) |
| Stock | Element Type | Linear Hexahedral Brick (C3D8R), Deformable, Reduced Integration |
|  | Mesh Characteristics | $\begin{gathered} \text { \# of Nodes: 49,994 } \\ \text { \# of Elements: 48,820 } \\ \text { \# of DOF: } 147,030 \text { (including Lagrange Multipliers) } \\ \hline \text { (in } \end{gathered}$ |
|  | Material | Homogeneous and Isotropic |
|  | Length | $1.0 \mathrm{~m}^{1}$ |
|  | Rate Dependence | Yes |
|  | Spring Back Calculation | No |
|  | Plasticity Law | Lee (Modified Shida) ${ }^{2}$ [6] |
|  | Hardening Rate | Isotropic |
|  | \% Plastic Deformation Energy Converted to Heat | 0.90 [8] |
|  | Initial Conditions | Initial Velocity of the Stock; Initial Temperature of the Stock |
| Stock / Roll Interface | Contact Condition | Tangential: Penalty; Normal: Hard |
|  | Friction Model | Coulomb ( $\mu=0.3$ ) |
|  | Heat Transfer Effects | Not Applicable |
| Stand | Material | Rigid Pin Support at Roll |
|  | Model Spacing (On-center) ${ }^{1}$ | Stands 1-2: 250 mm ; Stands 2-3: 200 mm ; Stands 3-4: 200 mm |
|  | Orientation ${ }^{3}$ | Stand \#1: Vertical; Stand \#2: Horizontal; Stand \#3: Vertical; Stand \#4: Horizontal |

${ }^{1}$ The section length of the stock is kept 1.0 m in the finite element model to reduce the number of degrees of freedom. Inter stand distances are also minimized for the same reason.
${ }^{2}$ Appropriate models are being used based on the strain rates.
${ }^{3}$ Stand orientation for the finite element model was assumed oriented vertically and horizontally for simplicity in model creation.


Figure 2: Actual rolling stand configuration.


Figure 3: Finite element model of rolling stands.

## Full-scale Mill Testing

A series of tests were conducted on one of Morgan's RSM units installed in a rod production line in order to gather detailed dimensional data on the rolling stock for comparison with the finite element model and theoretical model in the next section. A standard size rod product of AISI 1045 carbon steel (Table I) was rolled in a series of tests in which the entry temperature to the RSM, the rolling rate and the entry dimensions were all held constant. The tests consisted of rolling a billet through four stands of the RSM to obtain rod samples.

Samples of the rolled product were obtained after the rod had passed through water cooling boxes, formed into continuous loops by the laying head and cooled on the aircooling conveyor. Short samples were cut from the coils produced from each test. For dimensional measurement, the samples were placed in a custom-made system for detailed off-line dimensional measurements of rod and bar products using a laser gauge and specialized analysis software. Diameter measurements were obtained for sixty diametrical locations, giving a detailed representation of the stock geometry profile.

## Results and Discussion

The finite element solution is verified with theoretical models and validated with fullscale mill testing (see previous section). Table III summarizes the finite element, theoretical and full-scale mill testing results for spread, cross-sectional area, percentage reduction in area, incremental plastic strain, total plastic strain and roll force at all four stands. An in-depth review of the state-of-the-art theoretical and empirical geometric and deformation models for steel rod and bar round-oval and oval-round pass rolling can be found in Souvik [4].

The finite-element, theoretical, and full-scale mill testing results for the cross-sectional profile at Stands \#1 through \#4 are compared in Figure 4. Figures 5 compares the finite-
element and theoretical results for the incremental plastic strain and total plastic strain at Stands \#1 through \#4. Finite element plots of the cross-sectional plastic strain distribution at Stands \#1 through \#4 are shown in Figure 6. A comparison of the finite element model and theoretical model for the roll force at Stands \#1 through \#4 is shown in Figure 7.

Table III. Comparison of finite element, theoretical and full-scale mill testing results at each stand

| Spread (mm) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 19.11 \\ (-2.3 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 13.58 \\ (-0.9 \% \mathrm{~T}) \\ (-1.5 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 14.45 \\ (3.1 \% \mathrm{~T}) \\ (3.0 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 12.81 \\ (-0.2 \% \mathrm{~T}) \\ (-0.1 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [9] ${ }^{1}$ | 19.57 | 13.70 | 13.98 | 12.84 |
| Full-scale Mill Testing | - | 14.01 | 14.02 | 12.82 |
| Cross-sectional Area (mm ${ }^{\text {a }}$ ) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 167.68 \\ (-2.8 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 145.72 \\ (0.1 \% \mathrm{~T}) \\ (-0.6 \% \mathrm{FST}) \end{gathered}$ | $\begin{gathered} 134.92 \\ (-0.7 \% \mathrm{~T}) \\ (0.2 \% \mathrm{FST}) \end{gathered}$ | 128.84 $(-1.3 \% \mathrm{~T})$ $(0.5 \% \mathrm{FST})$ |
| Theoretical Lee [9] | 172.50 | 146.60 | 135.94 | 130.59 |
| Full-scale Mill Testing | - | 145.66 | 134.66 | 128.15 |
| Percentage Reduction in Area (\%) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 18.67 \\ (2.1 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 13.10 \\ (-12.8 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 7.40 \\ (1.9 \% \mathrm{~T}) \\ (-2.0 \% \mathrm{FST}) \\ \hline \end{gathered}$ | $\begin{gathered} 4.51 \\ (14.5 \% \mathrm{~T}) \\ (-6.6 \% \mathrm{FST}) \\ \hline \end{gathered}$ |
| Theoretical Lee [9] | 18.28 | 15.02 | 7.27 | 3.94 |
| Full-scale Mill Testing | - | - | 7.55 | 4.83 |
| Incremental Plastic Strain ${ }^{2}$ (mm/mm) |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |
| FEM | $\begin{gathered} 0.399 \\ (5.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.280 \\ (-15.2 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.107 \\ (0.5 \% \mathrm{~T}) \end{gathered}$ | $\begin{gathered} 0.081 \\ (1.25 \% \mathrm{~T}) \end{gathered}$ |
| Theoretical Lee [10] ${ }^{3}$ | 0.380 | 0.331 | 0.107 | 0.08 |


| TOTAL PLASTIC STRAIN $^{\mathbf{2}}(\mathbf{m m} / \mathbf{m m})$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |  |
| FEM | 0.399 | 0.764 | 0.904 | 0.983 |  |
|  | $(5.2 \% \mathrm{~T})$ | $(7.6 \% \mathrm{~T})$ | $(11.2 \% \mathrm{~T})$ | $(13.1 \% \mathrm{~T})$ |  |
| Theoretical Lee $[10]^{3}$ | 0.380 | 0.710 | 0.814 | 0.869 |  |
| RoLL ForCe $(\mathbf{k N})$ |  |  |  |  |  |
| Method | Stand \#1 | Stand \#2 | Stand \#3 | Stand \#4 |  |
| FEM | 110.2 | 80.7 | 49.1 | 30.7 |  |
|  | $(-42.6 \% \mathrm{~T})$ | $(-48.3 \% \mathrm{~T})$ | $(7.7 \% \mathrm{~T})$ | $(20.5 \% \mathrm{~T})$ |  |
| Theoretical Lee $[11]^{4}$ | 191.9 | 156 | 46 | 26 |  |

$\mathrm{T}=\%$ Difference with theoretical method.
FST $=\%$ Difference with full-scale mill testing data.
${ }^{1}$ Spread factor $\beta=0.83$.
${ }^{2}$ All strains are measured at exit of each stand
${ }^{3}$ The theoretical strains are calculated by maximum width method [10].
${ }^{4}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.
Overall there is very good correlation between the finite element solution, theoretical solution and full-scale mill testing for spread and cross-sectional area of the stock. The percentage difference between finite element solution, theoretical solution and full-scale mill testing for spread and cross-sectional area is within $3 \%$ in the worst cases and in
most cases within $2 \%$. It can be concluded that for last three stands with round grooves, the finite element solution for cross-sectional area is greater than full-scale mill testing cross-sectional area and less than theoretical cross-sectional area for all four stands.

There is no full-scale mill testing data available for incremental plastic strain and total plastic strain, therefore, only the theoretical and finite element solutions are compared. The theoretical and finite element solutions for incremental plastic strain and total plastic strain are consistent for the initial stands. However, the difference between them increases with successive stands due to error accumulation from the previous stands. Both the incremental plastic strain and total plastic strain finite element solution are generally greater than the theoretical solution and the percentage difference is within $15 \%$ in the worst case. However, the finite element solution is more useful than the theoretical solution since it determines the strain distribution that can be used to find mechanical properties and microstructure in future work.

There is no full-scale mill testing data available for roll force, therefore, only the theoretical and finite element solutions are compared. The finite element solution for roll force is less $\approx 40-50 \%$ of the theoretical solution for the first two stands where $\%$ reduction is large. This appears very large and is probably due to the fact that the actual model for calculating roll force by Lee [11] uses two parameters that are experimentally determined. In absence of experimental data these two parameters were determined theoretically. For the last two stands, where $\%$ reduction in area is small, the finite element solution for roll force is $\approx 10-20 \%$ greater than the theoretical solution. We have observed that the roll force obtained by the finite element solution is consistent and within $\pm 10 \%$ of a proprietary Morgan model for evaluating roll force. The proprietary model employs a combination of empirical techniques that have been experimentally validated.

The results from Stand \#4 (last stand) are very important, because the geometric tolerances and roundness at the stand exit determines part quality. There is a strong correlation between full-scale mill testing, finite element solution and theoretical solution for spread and cross-sectional area.


Figure 4: Cross-sectional profile and area for finite element, theoretical and full-scale mill testing for Stands \#1 through \#4.


Figure 5: Incremental and total plastic strain for finite element and theoretical at Stands \#1 through \#4.


Figure 6: Finite element solution of total plastic strain ( $\mathrm{mm} / \mathrm{mm}$ ) distribution in stock at Stands \#1 through \#4.


Figure 7: Roll force for finite element and theoretical models at Stands \#1 through \#4.

## Customer Requirements

A Morgan rolling mill needs to manufacturer a finished rod of AISI 1045 medium carbon steel with a 12.75 mm diameter. The customer (rod user) is a U.S. automotive supplier who will manufacturer M12 $\times 1.25,4 \mathrm{~g}$ (high accuracy, fine fits) steel bolt of SAE class 4.6 from the finished rod. The geometric requirements of the finished rod for the U.S. automotive supplier are based on ASTM standards [12]. Tables IV and V demonstrate good correlation of the finite element model with the design objective to produce rod with a circular cross section in the mill on-line. Note that the theoretical model does give a very good geometric prediction in this case. However, the theoretical model cannot consider steel grade and coupling effects. Furthermore, this type of model cannot predict the distribution of microstructural and mechanical properties throughout the rod. This is very important where a steel mill must satisfy customer requirements for a uniform distribution of mechanical and microstructural properties for many products. Although the finite element results do not satisfy customer requirements fully in this case, it is expected that the predictions will improve as the finite element model includes all the coupling effects, i.e., thermo-deformation-microstructural. This work demonstrates the potential for development of a coupled thermo-deformation-microstructural simulation model in the future.

Table IV. Comparison of full-scale mill testing, finite element and theoretical geometric results
at exit of Stand \#4

| PARAMETER | FULL-SCALE MILL TESTING | FEM $^{\mathbf{1}}$ | THEORETICAL $^{\mathbf{1}}$ [9-11] |
| :---: | :---: | :---: | :---: |
| Maximum Diameter | 12.82 mm | 12.81 mm | 12.84 mm |
|  |  | $(-0.1 \%)$ | $(0.3 \%)$ |


| Minimum Diameter | 12.75 mm | 12.71 mm <br> $(-0.3 \%)$ | 12.79 mm <br> $(0.3 \%)$ |
| :---: | :---: | :---: | :---: |
| Cross-sectional Area | $128.15 \mathrm{~mm}^{2}$ | $128.84 \mathrm{~mm}^{2}$ <br> $(0.5 \%)$ | $130.59 \mathrm{~mm}^{2}$ <br> $(1.9 \%)$ |

${ }^{1}$ The quantity in parentheses represents the percentage difference between the parameter shown in the column and fullscale mill testing.

Table V. Geometry customer requirements and comparison with full-scale mill testing, finite element and theoretical model

| ASTM REQUIREMENTS [12] |  | FULL-SCALE MILL TESTING | FEM | THEORETICAL [9-11] |
| :---: | :---: | :---: | :---: | :---: |
| Roundness $^{\mathbf{1}}$ | 0.08 mm | 0.06 mm | 0.1 mm | 0.12 mm |
| Tolerance $^{\mathbf{2}}$ | $\pm 0.08 \mathrm{~mm}$ | +0.07 mm | +0.06 mm | +0.04 mm |

${ }^{1}$ Roundness is the difference between maximum diameter and minimum diameter.
${ }^{2}$ Tolerance is the allowable difference in diameter between what a customer orders and what the steel mill delivers.

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## Appendix J: Thesis Presentation

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[^0]:    ${ }^{1}$ Though it may be necessary to model the actual stand separation if the thermal and inter-stand tension/compression effects need to be modeled more effectively

[^1]:    ${ }^{2}$ Full-scale mill testing is carried out at Republic Engineered Products, Lorain, OH
    ${ }^{3}$ Calculation of incremental and total plastic strain at a given stand depends on the incremental and total plastic strain calculated at the previous stand. The differences between the finite element and theoretical solution increases due to a cumulative effect at a later stand.

[^2]:    ${ }^{4}$ Maximum contact length $\left(\mathrm{L}_{\max }\right)$ and the distance where the roll groove and the deformed stock are separated $\left(\mathrm{C}_{\mathrm{x}}\right)$ in [5.2] are calculated theoretically in this work.

[^3]:    ${ }^{1}$ Spread factor $\beta=0.83$
    ${ }^{2}$ The theoretical strains are calculated by maximum width method [5.9].
    ${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

[^4]:    ${ }^{1}$ Spread factor $\beta=0.83$
    ${ }^{2}$ The theoretical strains are calculated by maximum width method [5.9].
    ${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

[^5]:    ${ }^{1}$ Spread factor $\beta=0.83$
    ${ }^{2}$ The theoretical strains are calculated by maximum width method [5.9].
    ${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

[^6]:    ${ }^{1}$ The section length of the stock is 1.0 m in the finite element model to reduce the number of degrees of freedom in the model. Inter-stand distances are also minimized for the same reason.
    ${ }^{2}$ Appropriate models are used based on expected strain rate range in Table 5.2.
    ${ }^{3}$ Stand orientation for the finite element model was assumed oriented vertically and horizontally for simplicity in model creation

[^7]:    ${ }^{5}$ Calculation of incremental and total plastic strain at a given stand depends on the incremental and total plastic strain calculated at the previous stand. The differences between the finite element and theoretical solution increases due to a cumulative effect at a later stand.
    ${ }^{6}$ Maximum contact length $\left(\mathrm{L}_{\max }\right)$ and the distance where the roll groove and the deformed stock are separated $\left(\mathrm{C}_{\mathrm{x}}\right)$ in [5.2] are calculated theoretically in this work.

[^8]:    ${ }^{1}$ Spread factor $\beta=0.97$
    ${ }^{2}$ The theoretical strains are calculated by maximum width method [5.9].
    ${ }^{3}$ Intersection between free surface and groove surface is approximated theoretically in absence of full-scale mill testing data.

